

Recommended Practice

Methodologies for the Determination of Setpoints for Nuclear Safety-Related Instrumentation

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ISA-RP67.04-Part II — Methodologies for the Determination of Setpoints for Nuclear Safety-
Related Instrumentation

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Preface

This preface is included for informational purposes and is not part of ISA-RP67.04, Part II.

This recommended practice has been prepared as part of the service of ISA, the international society for measurement and control, toward a goal of uniformity in the field of instrumentation. To be of real value, this document should not be static but should be subject to periodic review. Toward this end, the Society welcomes all comments and criticisms and asks that they be addressed to the Secretary, Standards and Practices Board; ISA; 67 Alexander Drive; P. O. Box 12277; Research Triangle Park, NC 27709; Telephone (919) 549-8411; Fax (919) 549-8288; E-mail: standards@isa.org.

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The ISA Standards and Practices Department is aware of the growing need for attention to the metric system of units in general and the International System of Units (SI) in particular, in the preparation of instrumentation standards, recommended practices, and technical reports. However, since this recommended practice does not provide constants or dimensional values for use in the manufacture or installation of equipment, English units are used in the examples provided.

Before utilizing this recommended practice, it is important that the user understand the relevance of instrument channel uncertainty and safety-related setpoint determination for nuclear power plants. Safety-related instrument setpoints are chosen so that potentially unsafe or damaging process excursions (transients) can be avoided and/or terminated prior to exceeding safety limits (process-design limits). The selection of a setpoint requires that consideration be given to much more than just instrumentation.

Experience has shown that an operational limit should be placed on critical process parameters to ensure that, given the most severe operating or accident transient, the plant's design safety limits will not be exceeded. Performance of an accident analysis establishes the analytical limits for critical process parameters. Typically, the accident analysis models include the thermodynamic, hydraulic, and mechanical dynamic response of the processes as well as assumptions regarding the time response of instrumentation. The analytical limits, as established by an accident analysis, do not normally include considerations for the accuracy (uncertainty) of installed instrumentation. To ensure that the actual trip setpoint of an instrument channel is appropriate, additional analysis may be necessary.

Instrument channel uncertainty should be determined, based on the characteristics of installed instrumentation, the environmental conditions present at the plant locations associated with the instrumentation, and on process conditions. A properly calculated setpoint will initiate a plant protective action before the process parameter exceeds its analytical limit, which, in turn, ensures that the transient will be avoided and/or terminated before the process parameter exceeds the established safety limit.

ISA-S67.04 was initially developed in the middle 1970s by the industry in response to large numbers of licensee event reports (LER). These LERs were attributed to the lack of adequate consideration of equipment drift characteristics when establishing the trip setpoints for the limiting safety system settings (LSSS) and engineered safety features actuation system (ESFAS)

setpoints. These setpoints are included as part of a nuclear power plant's operating license in their technical specifications. Hence, bistable trip setpoints were found beyond the allowable values identified in the technical specifications.

The scope of the standard was focused on LSSS and ESFAS setpoints. As the standard evolved, it continued to focus on those key safety-related setpoints noted previously. It may also be noted that as the technical specifications have evolved, the values now included in the technical specifications may be the trip setpoint or the allowable value or both depending on the setpoint methodology philosophy used by the plant and/or the Nuclear Steam Supply Systems (NSSS) vendor. The methodologies, assumptions, and conservatism associated with performing accident analyses and setpoint determinations, like other nuclear power plant technologies, have also evolved. This evolution has resulted in the present preference for explicit evaluation of instrument channel uncertainties and resulting setpoints rather than implicitly incorporating such uncertainties into the overall safety analyses. Both the explicit and implicit approaches can achieve the same objective of assuring that design safety limits will not be exceeded. During the process of developing the 1988 revision of ISA-S67.04, it was determined that, because of the evolving expectations concerning setpoint documentation, additional guidance was needed concerning methods for implementing the requirements of the standard. In order to address this need, standard Committees SP67.15 and SP67.04 were formed and have prepared this recommended practice. It is the intent of the Committees that the scope of the recommended practice be consistent with the scope of the standard. The recommended practice is to be utilized in conjunction with the standard. The standard is 67.04, Part I, and the recommended practice is 67.04, Part II.

During the development of this recommended practice, a level of expectation for setpoint calculations has been identified, which, in the absence of any information on application to less critical setpoints, leads some users to come to expect that all setpoint calculations will contain the same level of rigor and detail. The lack of specific treatment of less critical setpoints has resulted in some potential users expecting the same detailed explicit consideration of all the uncertainty factors described in the recommended practice for all setpoints. It is not the intent of the recommended practice to suggest that the methodology described is applicable to all setpoints. Although it may be used for most setpoint calculations, it is by no means necessary that it may be used for all setpoints. In fact, in some cases, it may not be appropriate.

Setpoints associated with the analytical limits determined from the accident analyses are considered part of the plant's safety-related design since they are critical to ensuring the integrity of the multiple barriers to the release of fission products. This class of setpoints and their determination have historically been the focus of ISA-S67.04 as discussed above.

Also treated as part of many plants' safety-related designs are setpoints that are not determined from the accident analyses and are not required to maintain the integrity of the fission product barriers. These setpoints may provide anticipatory inputs to, or reside in, the reactor protection or engineered safeguards initiation functions but are not credited in any accident analysis. Alternatively, there are setpoints that support operation of, not initiation of, the engineered safety features.

In applying the standard to the determination of setpoints, a graduated or "graded" approach may be appropriate for setpoints that are not credited in the accident analyses to initiate reactor shutdown or the engineered safety features.

While it is the intent that the recommended practice will provide a basis for consistency in approach and terminology to the determination of setpoint uncertainty, it is acknowledged that the recommended practice is not an all-inclusive document. Other standards exist that contain principles and terminology, which, under certain circumstances, may be useful in estimating instrument uncertainty. It is acknowledged therefore that concerns exist as to whether the recommended practice is complete in its presentation of acceptable methods. The user is

encouraged to review several of the references in the recommended practice that contain other principles and terminology.

The uncertainty and setpoint calculations discussed in this recommended practice may be prepared either manually or with a computer software program. The documentation associated with these calculations is discussed in [Section 10](#); however, the design control and documentation requirements of manual calculations or computer software are outside the scope of the recommended practice.

This recommended practice is intended for use primarily by the owners/operating companies of nuclear power plant facilities or their agents (NSSS, architects, engineers, etc.) in establishing setpoint methodology programs and preparing safety-related instrument setpoint calculations.

This recommended practice utilizes statistical nomenclature that is customary and familiar to personnel responsible for nuclear power plant setpoint calculations and instrument channel uncertainty evaluation. It should be noted that this nomenclature may have different definitions in other statistical applications and is not universal, nor is it intended to be. Furthermore, in keeping with the conservative philosophy employed in power plants calculations, the combination of uncertainty methodology for both dependent and independent uncertainty components is intended to be bounding. That is, the resultant uncertainty should be correct or overly conservative to ensure safe operation. In cases where precise estimation of measurement uncertainty is required, more sophisticated techniques should be employed.

ISA Standard Committee SP67.04 operates as a Subcommittee under SP67, the ISA Nuclear Power Plant Standards Committee, with H. R. Wiegles as Chairman.

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1 Scope

This recommended practice provides guidance for the implementation of ISA-S67.04, Part I in the following areas:

- a) Methodologies, including sample equations to calculate total channel uncertainty
- b) Common assumptions and practices in instrument uncertainty calculations
- c) Equations for estimating uncertainties for commonly used analog and digital modules
- d) Methods to determine the impact of commonly encountered effects on instrument uncertainty
- e) Application of instrument channel uncertainty in setpoint determination
- f) Sources and interpretation of data for uncertainty calculations
- g) Discussion of the interface between setpoint determination and plant operating procedures, calibration procedures, and accident analysis
- h) Documentation requirements

2 Purpose

The purpose of this recommended practice is to present guidelines and examples of methods for the implementation of ISA-S67.04, Part I in order to facilitate the performance of instrument uncertainty calculations and setpoint determination for safety-related instrument setpoints in nuclear power plants.

3 Definitions

3.1 allowable value: A limiting value that the trip setpoint may have when tested periodically, beyond which appropriate action shall be taken.

3.2 analytical limit: Limit of a measured or calculated variable established by the safety analysis to ensure that a safety limit is not exceeded.

3.3 abnormally distributed uncertainty: A term used in this recommended practice to denote uncertainties that do not have a normal distribution. [See 6.2.1.2.2](#) for further information.

3.4 as found: The condition in which a channel, or portion of a channel, is found after a period of operations and before recalibration (if necessary).

3.5 as-left: The condition in which a channel, or portion of a channel, is left after calibration or final setpoint device setpoint verification.

3.6 bias: An uncertainty component that consistently has the same algebraic sign and is expressed as an estimated limit of error.

3.7 bistable:¹ A device that changes state when a preselected signal value is reached.

3.8 dependent uncertainty: Uncertainty components are dependent on each other if they possess a significant correlation, for whatever cause, known or unknown. Typically, dependencies form when effects share a common cause.

3.9 drift: An undesired change in output over a period of time where change is unrelated to the input, environment, or load.

3.10 effect: A change in output produced by some outside phenomena, such as elevated temperature, pressure, humidity, or radiation.

3.11 error: The algebraic difference between the indication and the ideal value of the measured signal.

3.12 final setpoint device: A component or assembly of components, that provides input to the process voting logic for actuated equipment. (See IEEE Standard 603.)

NOTE: Examples of final actuation devices are bistables, relays, pressure switches, and level switches.

3.13 independent uncertainty: Uncertainty components are independent of each other if their magnitudes or algebraic signs are not significantly correlated.

3.14 instrument channel: An arrangement of components and modules as required to generate a single protective action signal when required by a plant condition. A channel loses its identity where single protective action signals are combined. (See IEEE Standard 603.)

3.15 instrument range: The region between the limits within which a quantity is measured, received, or transmitted, expressed by stating the lower and upper range values.

3.16 limiting safety system setting (LSSS): Limiting safety system settings for nuclear reactors are settings for automatic protective devices related to those variables having significant safety functions. (See CFR Reference.)

3.17 margin: In setpoint determination, an allowance added to the instrument channel uncertainty. Margin moves the setpoint farther away from the analytical limit.

3.18 module: Any assembly of interconnected components that constitutes an identifiable device, instrument, or piece of equipment. A module can be removed as a unit and replaced with a spare. It has definable performance characteristics that permit it to be tested as a unit. A module can be a card, a drawout circuit breaker, or other subassembly of a larger device, provided it meets the requirements of this definition. (See IEEE Standard 603.)

¹ As an example of the intended use of the term "bistable" in the context of this document, electronic trip units in BWRs are considered "bistables."

3.19 nuclear safety-related instrumentation: That which is essential to the following:

- a) Provide emergency reactor shutdown
- b) Provide containment isolation
- c) Provide reactor core cooling
- d) Provide for containment or reactor heat removal, or
- e) Prevent or mitigate a significant release of radioactive material to the environment; or is otherwise essential to provide reasonable assurance that a nuclear power plant can be operated without undue risk to the health and safety of the public.

3.20 primary element: The system element that quantitatively converts the measured variable energy into a form suitable for measurement.

3.21 process measurement instrumentation: An instrument, or group of instruments, that converts a physical process parameter such as temperature, pressure, etc., to a usable, measurable parameter such as current, voltage, etc.

3.22 random:² Describing a variable whose value at a particular future instant cannot be predicted exactly but can only be estimated by a probability distribution function. (See ANSI C85.1.)

3.23 reference accuracy (also known as "accuracy rating" as defined in ISA-S51.1): A number or quantity that defines a limit that errors will not exceed when a device is used under specified operating conditions.

3.24 safety limit: A limit on an important process variable that is necessary to reasonably protect the integrity of physical barriers that guard against uncontrolled release of radioactivity. (See CFR Reference.)

3.25 sensor: The portion of an instrument channel that responds to changes in a plant variable or condition and converts the measured process variable into a signal; e.g., electric or pneumatic. (See IEEE Standard 603.)

3.26 signal conditioning: One or more modules that perform signal conversion, buffering, isolation, or mathematical operations on the signal as needed.

3.27 signal interface: The physical means (cable, connectors, etc.) by which the process signal is.

3.28 span: The algebraic difference between the upper and lower values of a calibrated range.

3.29 test interval: The elapsed time between the initiation (or successful completion) of tests on the same sensor, channel, load group, safety group, safety system, or other specified system or device. (See ANSI C85.1.)

3.30 tolerance: The allowable variation from a specified or true value. (See IEEE Standard 498.)

3.31 trip setpoint: A predetermined value for actuation of the final actuation device to initiate protective action.

² In the context of this document, "random" is an abbreviation for random, approximately normally distributed. The algebraic sign of a random uncertainty is equally likely to be positive or negative with respect to some median value. Thus, random uncertainties are eligible for square-root-sum-of-squares combination propagated from the process measurement module through the signal conditioning module of the instrument channel to the module that initiates the actuation.

3.32 uncertainty: The amount to which an instrument channel's output is in doubt (or the allowance made therefore) due to possible errors, either random or systematic, that have not been corrected for. The uncertainty is generally identified within a probability and confidence level.

Additional definitions related to setpoints or instrument terminology and uncertainty may be found in ANSI/ISA-S37.1-1975, ANSI/ISA-S51.1-1979, and ISA-S67.04, Part I-1994.

4 Using this recommended practice

The recommended practice is primarily focused on calculating a setpoint for a single instrument channel using acceptable statistical methods, where use of these methods is important to assuring the plant operates within the envelope of the accident analyses and maintains the integrity of the fission product release barriers. There are a number of different approaches that are acceptable for use in establishing nuclear safety-related setpoints. The statistical method presented in the recommended practice is the most common approach in use at this time. The recommended practice is intended to identify areas that should be evaluated when one does a setpoint calculation, to present some examples of present thinking in the area of setpoint calculations, and to provide some recommendations for a setpoint methodology. The methods discussed in the recommended practice are not intended to be all-inclusive. The recommended practice includes many terms used in probability and statistics. Since it is not the purpose of the recommended practice to be a text on these subjects, it is recommended that the user review a text on statistics to establish a knowledge of some of the terminology in conjunction with the use of the recommended practice.

Additionally, it is recognized that some safety-related setpoints are not tied to the safety analyses and do not, even from a system's standpoint, have an explicit limiting value. Thus a graded approach may be applied to the plant's safety-related setpoints. A graded approach might include a method of classifying setpoints according to their contribution to plant safety. Based on the method of classification, the approach would provide guidance on the method to be used to determine the channel uncertainty. Specific criteria for establishing a graded approach or the level of analysis used as part of this type of approach are outside the scope of the recommended practice. For an example of a graded approach, see the R.C. Webb Reference.

The remainder of the recommended practice is structured to mimic the process one would follow to determine an instrument channel setpoint. A method for calculating instrument channel uncertainties is discussed in [Section 5](#), and a method for calculating the trip setpoint when one has analytical limit for the process is discussed in [Section 6](#).

The recommended practice starts in [Section 5](#) with the preparation of a block diagram of the instrument channel being analyzed. Uncertainty equations and discussions on sources of uncertainty and interpretation of uncertainty data are presented in [6.1](#) and [6.2](#). The basic equations for calculating total instrument channel uncertainty are presented in [6.3](#). Methods to determine the instrument channel allowable value and trip setpoint for an instrument channel are presented in [Section 7](#). Selected subjects related to determining setpoints for nuclear plant instrumentation are discussed in [Section 8](#).

It is prudent to evaluate setpoint calculations to assure they are not overly conservative. Overly conservative setpoints can be restrictive to plant operation or may reduce safety by unnecessarily increasing the frequency of safety system actuation. The evaluation should assure that there are no overlapping, redundant, or inconsistent values or assumptions. Conservatism

may result from the many interfaces between organizations that can have an input to the calculation. These interfaces are discussed in [Section 9](#).

Documentation considerations are discussed in [Section 10](#). The appendices provide in-depth discussions concerning the theory and background for the information presented in Sections 5 through 7, as well as extensive and comprehensive examples of setpoint calculations and discussions of unique topics in setpoint determination.

5 Preparation for determining instrument channel setpoints

The following discussion provides a suggested sequence of steps to be performed when developing an instrument channel uncertainty or setpoint analysis. The intent is to guide the reader through the basics of the channel layout, functions provided, sources of uncertainty that may be present, etc., with references to the appropriate section(s) for detailed discussions of particular topics of interest.

5.1 Diagramming instrument channel layout

When preparing an uncertainty or setpoint calculation, it is helpful to generate a diagram of the instrument channel being analyzed in a manner similar to that shown in [Figure 1](#). A diagram aids in developing the analysis, classifying the uncertainties that may be present in each portion of the instrument channel, determining the environmental parameters to which each portion of the instrument channel may be exposed, and identifying the appropriate module transfer function.

[Figure 1](#) shows a typical instrument channel that could be used to provide a nuclear safety-related protection function. It also shows interfaces, functions, sources of error, and different environments.

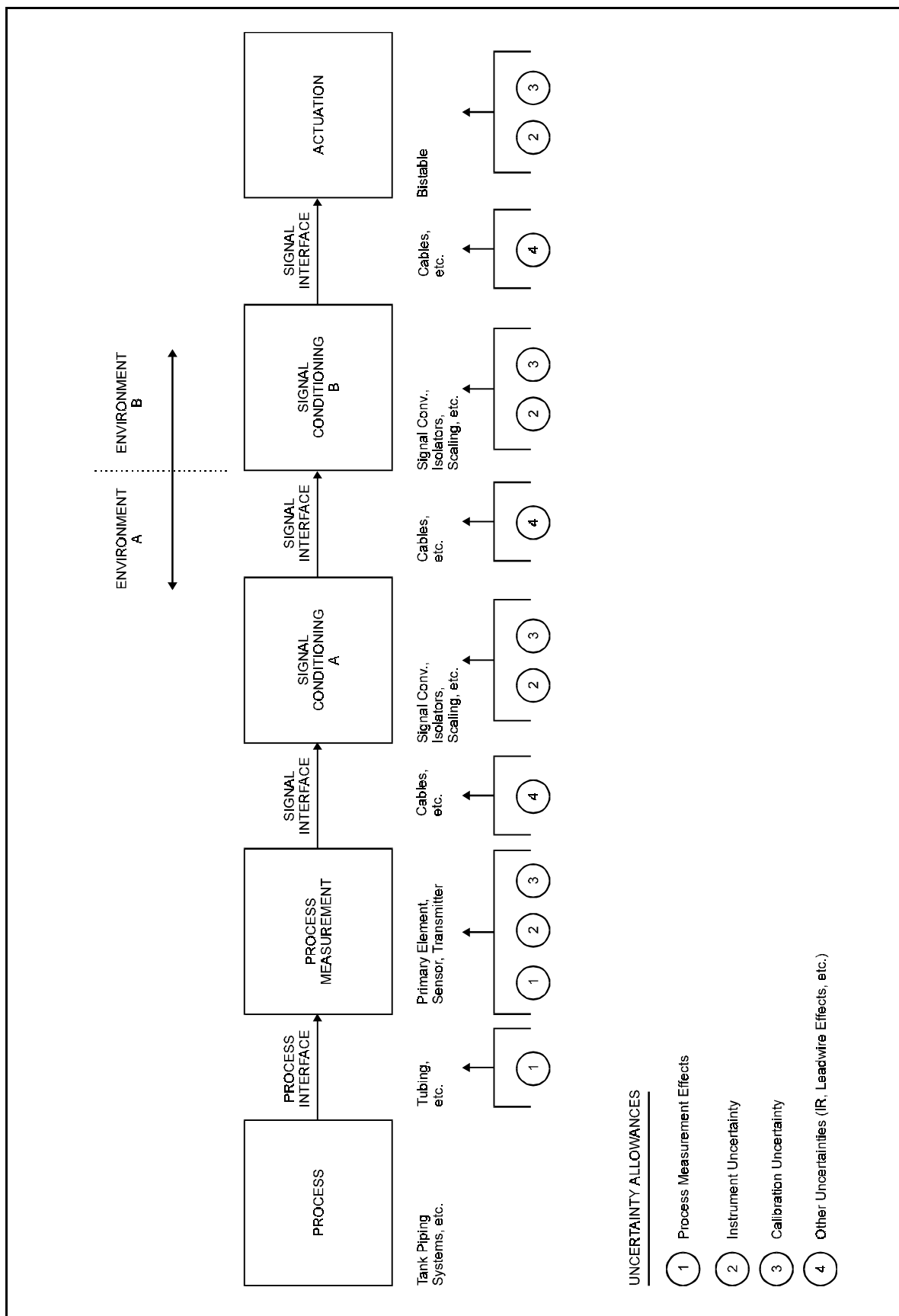


Figure 1. Typical instrument channel layout

A typical instrument channel consists of the following major sections:

- a) Process
- b) Process interface
- c) Process measurement
- d) Signal interface
- e) Signal conditioning
- f) Actuation

5.2 Identifying design parameters and sources of uncertainty

The functional requirements, actuation functions, and operating times of the instrument channel, as well as the postulated environments that the instrument could be exposed to concurrent with these actuations, should be identified. Many times the instrument channel uncertainty is dependent on a particular system operating mode, operating point (i.e., maximum level, minimum flow, etc.), or a particular sequence of events. A caution that should be considered when the same setpoint is used for more than one actuation function, each with possibly different environmental assumptions, is that the function with the most limiting environmental conditions should be used. Where a single instrument channel has several setpoints, either the most limiting set of conditions should be used or individual calculations for each setpoint should be performed, each with the appropriate set of conditions.

Environmental boundaries can then be drawn for the instrument channel as shown in [Figure 1](#). For simplicity, two sets of environmental conditions are shown. Typically, the process measurement, process interface, some of the signal conditioning (if applicable), and some of the signal interface components are located in areas of the plant that may have a significantly different local environment from the remainder of the instrument channel. Typically, most signal conditioning components and other electronics are located in a controlled environment not subject to significant variations in temperature or to post-accident environments. Therefore, two sets of environmental conditions are defined, with conditions in Environment A normally more harsh than conditions in Environment B. Normally, larger environmental uncertainty allowances will be used with those portions of the instrument channel exposed to Environment A. Environmental effects and assumptions pertaining to environmental conditions are discussed in [6.2.4](#).

After the environmental conditions are determined, the potential uncertainties affecting each portion of the instrument channel should be determined. For example, the process interface portion is normally affected only by process measurement effects and not by equipment calibration or other uncertainties. Also, cables in the mild conditions of Environment B would not be appreciably affected by insulation resistance (IR) effects.

[Figure 1](#) shows where each major class of uncertainty typically will be present. Each major class is listed below along with a further breakdown into particular types and the particular section(s) where each is discussed in the recommended practice. This list is not meant to be all-inclusive.

Process measurement effects

- Vessel/reference leg temperature effects ([Appendix B](#))
- Fluid density effects on flow measurement ([Appendix C](#))
- Piping configuration effects on flow measurement ([Appendix C](#))
- Line pressure loss/head pressure effects ([Appendix F](#))

Instrument uncertainty:

- Reference accuracy ([3, 6.2.6](#))
- Temperature effects ([6.2.2](#))
- Pressure effects ([6.2.3](#))
- Drift ([6.2.7](#))
- Module power supply variations ([6.2.8](#))
- Digital signal processing ([6.2.9](#))
- RTD accuracy confirmation ([Appendix G](#))
- Environmental effects - Accident ([6.2.4](#))

Calibration uncertainty: ([6.2.6](#))

Other:

- Insulation resistance effects ([Appendix D](#))
- Lead wire effects

The uncertainty allowances must then be identified. These may come from any number of sources; such as NSSS vendor's analysis for a process measurement effect, the manufacturer's product specifications and test reports, or actual plant data. Also, various assumptions may need to be made when data is not available and to limit the conditions under which the calculation results may be considered valid. Once identified, the uncertainties should be classified as either random, biases, or abnormally distributed.

When the instrument channel diagram is developed and the uncertainty allowances are known, a mathematical expression of the total instrument channel uncertainty from the process through the bistable can be developed from the individual module input/output relationships. Then, the total instrument channel uncertainty can be determined. The methods for combining individual uncertainties into total module and/or instrument channel allowances are discussed extensively in [6.3](#).

Finally, the trip setpoint and allowable value can be determined once the instrument channel uncertainty and analytical limit are known. This is discussed in [Section 7](#).

A flowchart of the setpoint determination process is provided in [Figure 2](#). Example calculations that depict this process are contained in [Appendix L](#).

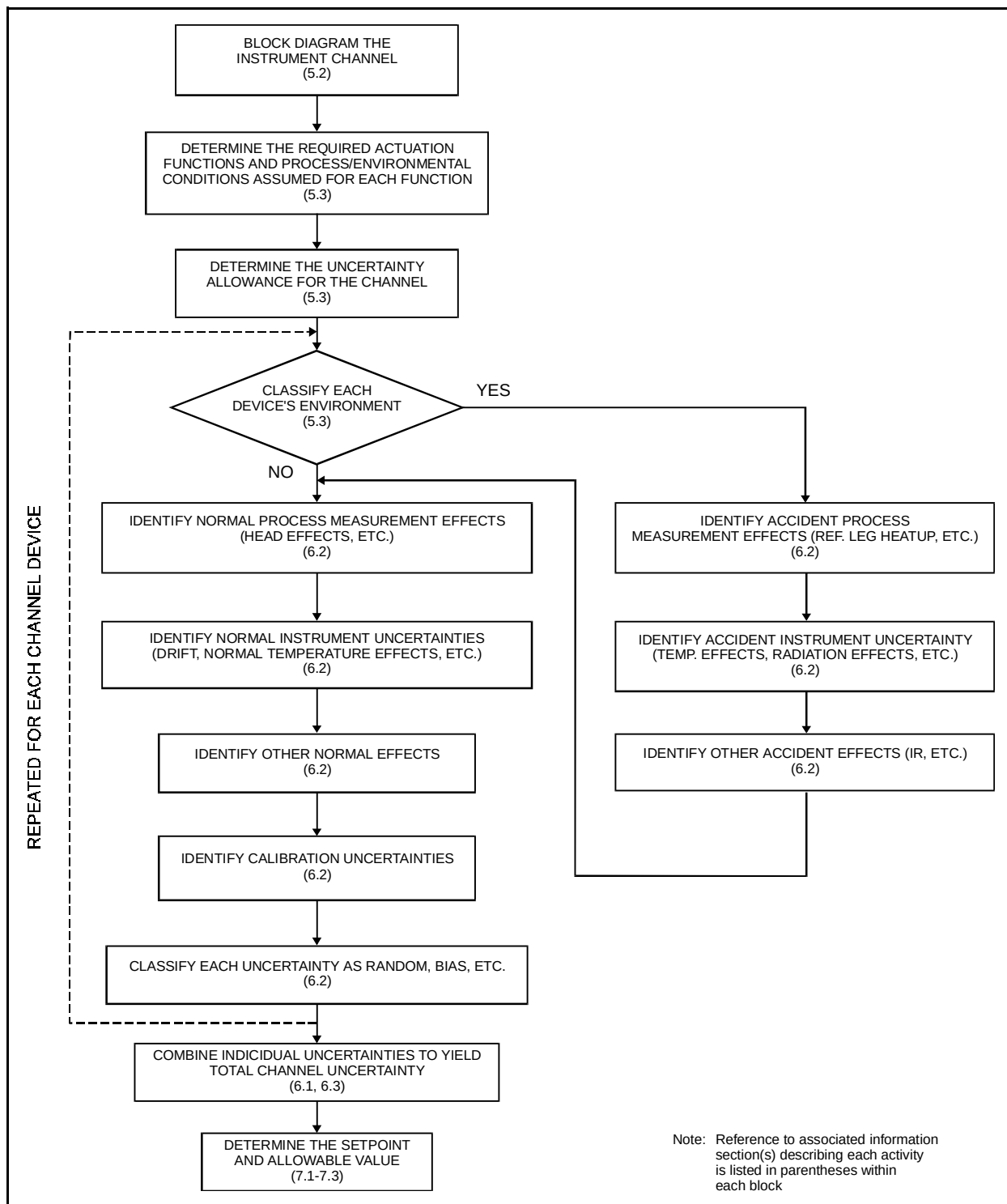


Figure 2. Setpoint calculation flowchart

6 Calculating instrument channel uncertainties

6.1 Uncertainty equations

Since all measurements are imperfect attempts to ascertain an exact natural condition, the actual magnitude of the quantity can never be known. Therefore, the actual value of the error in the measurement of a quantity is also unknown. The amount of the error should therefore be discussed only in terms of probabilities; i.e., there may be one probability that a measurement is correct to within a certain specified amount and another probability for correctness to within another specified amount. For the purpose of this recommended practice, the term "uncertainty" will be utilized to reflect the distribution of possible errors.

There are a number of recognized methods for combining instrumentation uncertainties. The method discussed by this recommended practice is a combination of statistical and algebraic methods that uses statistical square root sum of squares (SRSS) methods to combine random uncertainties and then algebraically combine the nonrandom terms with the result. The formulas and discussion below present the basic principles of this methodology. Another recognized methodology to estimate instrument measurement uncertainty is described in ANSI/ASME PTC 19.1. Additional discussion of this methodology is provided in J.1 of Appendix J.

The basic formula for uncertainty calculation takes the form:

$$Z = \pm[(A^2 + B^2 + C^2)]^{1/2} \pm |F| + L - M \quad (\text{Eq. 6.1})$$

where

- A,B,C = random and independent terms. The terms are zero-centered, approximately normally distributed, and indicated by a $\pm$ sign.
- F = abnormally distributed uncertainties and/or biases (unknown sign). The term is used to represent limits of error associated with uncertainties that are not normally distributed and do not have known direction. The magnitude of this term (absolute value) is assumed to contribute to the total uncertainty in a worst-case direction and is also indicated by a $\pm$ sign.
- L & M = biases with known sign. The terms can impact an uncertainty in a specific direction and, therefore, have a specific + or - contribution to the total uncertainty.
- Z = resultant uncertainty. The resultant uncertainty combines the random uncertainty with the positive and negative components of the nonrandom terms separately to give a final uncertainty. The positive and negative nonrandom terms are not algebraically combined before combination with the random component.

The addition of the F, L, and M terms to the A, B, and C uncertainty terms allows the formula to account for influences on total uncertainty that are not random or independent. For biases with known direction, represented by L and M, the terms are combined with only the applicable portion (+ or -) of the random uncertainty. For the uncertainty represented by F, the terms are combined with both portions of the random uncertainty. Since these terms are uncertainties themselves, the positive and negative components of the terms cannot be algebraically combined into a single term. The positive terms of the nonrandom uncertainties should be summed separately, and the negative terms of the nonrandom uncertainties should be summed separately and then individually combined with the random uncertainty to yield a final value. Individual nonrandom uncertainties are independent probabilities and may not be present simultaneously. Therefore, the individual terms cannot be assumed to offset each other³.

If R equals the resultant random uncertainty $(A^2 + B^2 + C^2)^{1/2}$, the maximum positive uncertainty is

$$+Z = +R + |F| + L$$

and the maximum negative uncertainty is

$$-Z = -R - |F| - M$$

SRSS combination for bias uncertainties is inappropriate since by their nature, they do not satisfy the prerequisites for SRSS. Bias uncertainties are not random and are not characterized by a normal probability distribution. Since the number of known biases is typically small and they may or may not be present simultaneously, the recommended practice conservatively endorses algebraic summation for bias uncertainties.

In the determination of the random portion of an uncertainty, situations may arise where two or more random terms are not totally independent of each other but are independent of the other random terms. This dependent relationship can be accommodated within the SRSS methodology by algebraically summing the dependent random terms prior to performing the SRSS determination. The formula takes the following form:

$$Z = \pm [A^2 + B^2 + C^2 + (D + E)^2]^{1/2} \pm |F| + L - M \quad (\text{Eq. 6.2})$$

where

D and E = random dependent uncertainty terms that are independent of Terms A, B, and C.

The uncertainty terms of Equation 6.2 and their associated relationships are depicted in [Figure 3](#).

³ The purpose of the setpoint calculation is to ensure that protective actions occur 95 percent of the time with a high degree of confidence before the analytical limits are reached. A conservative philosophy applies the SRSS technique only to those uncertainties that are characterized as independent, random, and approximately normally distributed (or otherwise allowed by versions of the central-limit theorem). All other uncertainty components are combined using the maximum possible uncertainty treatment; i.e., algebraic summation of absolute values as necessary.

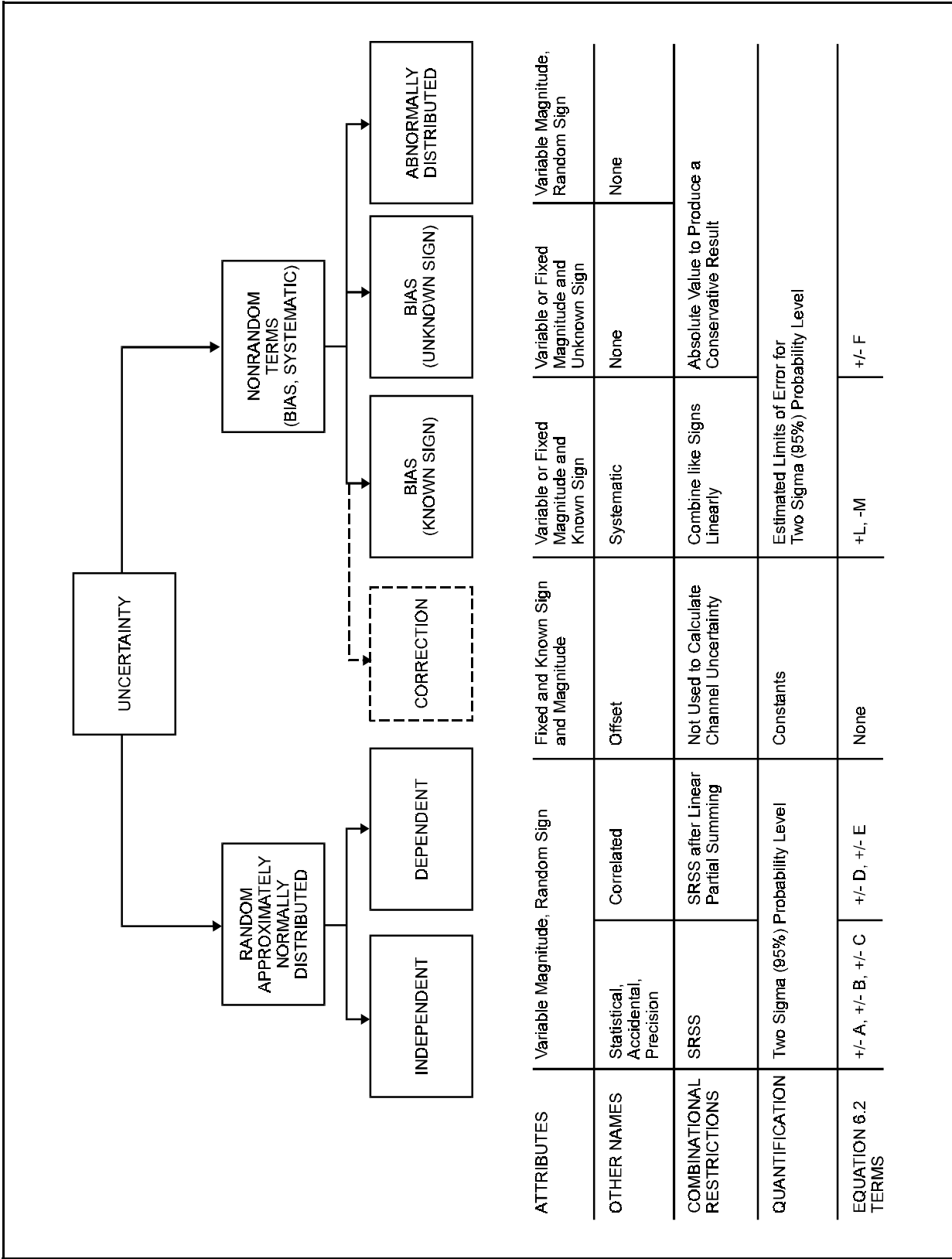


Figure 3. Uncertainty model

While the basic uncertainty formula can be used for any instrumentation application, care should be taken when applying the formula in applications containing nonlinear modules or functions. While the term can still be random and independent, its magnitude is a function of the input and the transfer function of the module. This requires the calculation of uncertainty for instrument channels containing nonlinear modules to be performed for specific values of the input signal.

The most common of these in instrumentation and control systems is the square root extractor in a flow channel. For these channels, the uncertainty value changes with the value of flow and, therefore, should be determined for each specific flow of interest.

The basic uncertainty combination formula can be applied to the determination of either a module uncertainty or a total instrument channel uncertainty. The results are independent of the order of combination as long as the dependent terms and bias terms are accounted for properly. For example, the uncertainty of a module can be determined from its individual terms and then combined with other module uncertainties to provide an instrument channel uncertainty, or all of the individual module terms can be combined in one instrument channel uncertainty formula. The result will be the same. The specific groupings and breakdown of an uncertainty formula can be varied for convenience of understanding.

6.2 Uncertainty data

The basic model used in this methodology requires that the user categorize instrument uncertainties as random, bias, or random abnormally distributed bias. Guidelines for combining these categories of uncertainties to determine the module or overall instrument channel uncertainty are provided in 6.3. It is the purpose of this section to provide an understanding of categories of instrument uncertainty and some insight into the process of categorizing instrumentation based on performance specifications, test reports, and the utility's own calibration data.

The determination of uncertainty estimates is an iterative process that requires the development of assumptions and, where possible, verification of assumptions based on actual data. Ultimately, the user is responsible for defending the assumptions that affect the basis of the uncertainty estimates.

It should not be assumed that, since this methodology addresses three categories of uncertainty, all three should be used in each uncertainty determination. Additionally, it should not be assumed that instrument characteristics should fit neatly into a single category. Data may require, for example, that an instrument's static pressure effect be represented as a random uncertainty with an associated bias.

6.2.1 Categories of uncertainty

6.2.1.1 Random uncertainties

In ANSI/ISA-S51.1-1979, random uncertainties are referred to as a quantitative statement of the reliability of a single measurement or of a parameter, such as the arithmetic mean value, determined from a number of random trial measurements. This is often called the statistical uncertainty and is one of the so-called precision indices. The most commonly used indices, usually in reference to the reliability of the mean, are the standard deviation, the standard error (also called the standard deviation of the mean), and the probable error.

It is usually expected that those instrument uncertainties that a manufacturer specifies as having a $\pm$ magnitude are random uncertainties. However, the uncertainty must be zero-centered and approximately normally distributed to be considered random. The hazards of assuming that the $\pm$ in vendor data implies that the instrument's performance represents a normal statistical

distribution are addressed in [6.2.12](#). After uncertainties have been categorized as random, any dependencies between the random uncertainties should be identified.

6.2.1.1.1 Independent uncertainties

Independent uncertainties are those uncertainties for which no common root cause exists. It is generally accepted that most instrument channel uncertainties are independent of each other.

6.2.1.1.2 Dependent uncertainties

Because of the complicated relationships that may exist between the instrument channels and various instrument uncertainties, a dependency may exist between some uncertainties. The methodology presented here provides a conservative means for addressing these dependencies. If, in the user's evaluation, two or more uncertainties are believed to be dependent, then, under this methodology, these uncertainties should be added algebraically to create a new, larger independent uncertainty.

Dependent uncertainties are those for which the user knows or suspects that a common root cause exists that influences two or more of the uncertainties with a known relationship.

6.2.1.2 Nonrandom uncertainties

6.2.1.2.1 Bias (known sign)

A bias is a systematic instrument uncertainty that is predictable for a given set of conditions because of the existence of a known direction (positive or negative).

For example, the static pressure effect of differential pressure transmitters, which exhibits a predictable zero shift because of changes in static pressure, is considered a bias. Additional examples of bias include head effects, range offsets, reference leg heatup or flashing, and changes in flow element differential pressure because of process temperature changes. A bias error may have an uncertainty associated with the magnitude.

6.2.1.2.2 Abnormally distributed uncertainties

Some uncertainties are not normally distributed. Such uncertainties are not eligible for SRSS combinations and are categorized as abnormally distributed uncertainties. Such uncertainties may be random (equally likely to be positive or negative with respect to some value) but extremely non-normal.

This type of uncertainty is treated as a bias against both the positive and negative components of a module's uncertainty. Refer to Appendix J on the use of the central limit theorem. Because they are equally likely to have a positive or a negative deviation, worst-case treatment should be used.

6.2.1.2.3 Bias (unknown sign)

Some bias effects may not have a known sign. Their unpredictable sign should be conservatively treated by algebraically adding the bias in the worse direction.

6.2.1.2.4 Correction

Errors or offsets that are of a known direction and magnitude should be corrected for in the calibration of the module and do not need to be included in the setpoint calculation. See also [6.2.6.4](#).

6.2.2 Module temperature effects

Most instruments exhibit a change in output as the ambient temperature to which they are exposed varies during normal plant operation above or below the temperature at which they were last calibrated. As this change or temperature effect is an uncertainty, it should be accounted for

in instrument uncertainty calculations. To estimate the magnitude of the effect, the operating temperature (OT) extremes above or below the calibration temperature (CT) should be defined. Many times these temperatures should be assumed, based on conservative insight of guidance, if documented operating experience or design-basis room temperature calculations are not available. For example, it would be conservative to assume the maximum OT coincident with the minimum CT to maximize the temperature shift.

Once the temperatures are defined, the temperature effect uncertainty (TE) for each module can be calculated using the manufacturer's published temperature effect specification. Commonly, the temperature effect is stated in vendor literature in one of the following two ways (expression in parentheses is an example). In each expression the temperature component (i.e., per 100°F) is a change in temperature within the vendor's specified range.

Either

$$\begin{aligned} \text{a)} \quad \text{TE} &= \pm X\% \text{ span per } Y^\circ\text{F} \\ &\quad (\text{for example, } \pm 1.0\% \text{ span per } 100^\circ\text{F}) \end{aligned}$$

or

$$\begin{aligned} \text{b)} \quad \text{TE} &= \pm X_1\% \text{ span at minimum span per } Y^\circ\text{F} \\ &\quad (\text{for example, } \pm 5.0\% \text{ span at minimum span per } 100^\circ\text{F}) \end{aligned}$$

and

$$\begin{aligned} \text{TE} &= \pm X_2 Y\% \text{ span at maximum span per } Y^\circ\text{F} \\ &\quad (\text{for example, } \pm 1.0\% \text{ span at maximum span per } 100^\circ\text{F}) \end{aligned}$$

If the temperature effect cannot be approximated by a linear relationship with temperature, a conservative approach is to use the bounding value for a temperature shift less than $Y^\circ\text{F}$. If the relationship is linear, then the uncertainty can be calculated as shown below. For the TE as expressed in (a),

$$\text{TE} = \pm X\% (\Delta T)/Y \quad (\text{Eq. 6.3})$$

where

$$\Delta T = OT_{\max} - CT \text{ or } \Delta T = CT - OT_{\min}, \text{ whichever is greater.}$$

For example, using Equation 6.3 and the example value of TE of (a) above, if OT varies from 50°F to 120°F and CT = 70°F,

$$\begin{aligned} \text{TE} &= \pm (1.0\%) (120 - 70)/100 \\ &= \pm 0.5\% \text{ span} \end{aligned}$$

Note that in the example above, the maximum operating temperature that the module will see (120°F) is a conservative value.

For (b), the uncertainty is not only temperature-dependent but span-dependent as well. To find the temperature effect for the span of interest, assuming the temperature effect is a linear function of span and temperature, it is necessary to interpolate using the following expression:

$$\frac{X - X_1}{X_2 - X_1} = \frac{\text{Span} - \text{Min Span}}{\text{Max Span} - \text{Min Span}} \quad (\text{Eq. 6.4})$$

Solving Equation 6.4 for X,

$$X = \frac{(\text{Span} - \text{Min Span})}{\text{Max Span} - \text{Min Span}} (X_2 - X_1) + X_1 \quad (\text{Eq. 6.5})$$

If, for example, the span is 55 psi for a transmitter with an adjustable span range of 10-100 psi, the uncertainty in (b) for the same temperature conditions assumed in the previous example can be calculated using Equation 6.5 and then Equation 6.3 as follows. In this case, however, X_1 and X_2 should be converted to process units so that units are the same.

$$\begin{aligned} X_1 &= (\pm 5.0\% \text{ span per } 100^\circ\text{F})(10 \text{ psi/span}) \\ &= \pm 0.5 \text{ psi per } 100^\circ\text{F} \\ X_2 &= (\pm 1.0\% \text{ span per } 100^\circ\text{F})(100 \text{ psi/span}) \\ &= \pm 1.0 \text{ psi per } 100^\circ\text{F} \\ X &= \frac{(55 - 10)(1.0 - 0.5)}{(100 - 10)} + 0.5 \\ &= \frac{(45)(0.5)}{90} + 0.5 \\ &= \pm 0.75 \text{ psi per } 100^\circ\text{F} \\ \text{TE} &= (0.75)(120 - 70)/100 \\ &= \pm 0.375 \text{ psi} \end{aligned}$$

Or in percent span

$$\begin{aligned} \text{TE} &= \pm 0.375 \text{ psi}/55 \text{ psi} \times 100\% \\ &= \pm 0.68\% \text{ span.} \end{aligned}$$

This section dealt with module ambient temperature influence under normal conditions. Accident effects and ambient-induced process uncertainties (such as reference leg heatup) are discussed in [6.2.4](#) and [Appendix B](#). If the particular instrument exhibits uncertainties under varying process temperatures, a range of expected process temperatures needs to be included as an assumption and the actual uncertainty calculated.

6.2.3 Module pressure effects

Some devices exhibit a change in output because of changes in process or ambient pressure. A typical static pressure effect expression applicable to a differential pressure transmitter, where the listed pressure specification is the change in process pressure, may look like

$$\pm 0.5\% \text{ span per } 1000 \text{ psi within the vendor's specified range.}$$

This effect can occur when an instrument measuring differential pressure (dP) is calibrated at low static pressure conditions but operated at high static pressure conditions. The manufacturer gives instructions for calibrating the instrument to read correctly at the normal expected operating pressure, assuming calibration was performed at low static pressure. This normally involves offsetting the span and zero adjustments by a manufacturer-supplied correction factor at the low-pressure (calibration) conditions so that the instrument will output the desired signal at the high-pressure (operating) conditions. To calculate the static pressure effect uncertainty (SP), an operating pressure (OP) for which the unit was calibrated to read correctly and a pressure variation (PV) above or below the OP should be determined. Once these points are defined, an expression similar to Equation 6.3 can be used to calculate the static pressure effect (assuming the effect is linear). Normally, the manufacturer lists separate span and zero effects.

A caution needs to be discussed here concerning proper use of this uncertainty in calculations. The effect shown above is random. However, additional bias effects may need to be included due to the way the static pressure calibration correction is done. For example, some instruments read low at high static pressure conditions. If they have not been corrected for static pressure effects, a negative bias would need to be included in the uncertainty calculation.

Another effect related to pressure extremes is the overpressure effect. This uncertainty is due to overranging the pressure sensor.

Ambient pressure variations will cause gage pressure instruments to shift up or down scale depending on whether the ambient pressure at the instrument location decreases or increases without a related change in the measured (process) variable. This occurs if the reference side of the process instrument is open to ambient pressure and the process is a closed system or if the process is open to atmosphere in an area with a different ambient pressure. This effect is a bias. The magnitude and direction will depend upon the variations in atmospheric pressure at the instrument location. This may be a concern for gage pressure instruments in enclosed areas such as reactor containment or containment enclosures.

6.2.4 Environmental effects - accident

For accident conditions, additional uncertainties associated with the high temperature, pressure, humidity, and radiation environment, along with the seismic response, may be included in the instrument uncertainty calculations, as required.

Qualification reports for safety-related instruments normally contain tables, graphs, or both, of accuracy before, during, and after radiation and steam/pressure environmental and seismic testing. Many times, manufacturers summarize the results of the qualification testing in their product specification sheets. More detailed information is normally available in the equipment qualification report.

Because of the limited sample size typically used in qualification testing, the conservative approach to assigning uncertainty limits is to use the worst-case uncertainties. Discussions with the vendor may be helpful to gain insight into the behavior of the uncertainty (i.e., should it be considered random or a bias?).

Using data from the qualification report (or module-specific temperature compensation data) in place of design performance specifications, it is often possible to justify the use of lower uncertainty values that may occur at reduced temperature or radiation dose levels. Typically, qualification tests are conducted at the upper extremes of simulated DBE environments so that the results apply to as many plants as possible, each with different requirements. Therefore, it is not always practical or necessary to use the results at the bounding environmental extremes when the actual requirements are not as limiting. Some cautions are needed, however, to preclude possible misapplication of the data.

- a) The highest uncertainties of all the units tested at the reduced temperature or dose should be used. This is to ensure that bounding uncertainties are used in the absence of a statistically valid sample size. When extrapolating test data to lower than tested environmental data, a margin may need to be applied. Again, discussions with the vendor may provide helpful insight for performing these extrapolations.
- b) The units tested should have been tested under identical or equivalent conditions and test sequences.
- c) If a reduced temperature is used, ensure that sufficient "soak time" existed prior to the readings at that temperature to ensure sufficient thermal equilibrium was reached within the instrument case. In other words, if a transmitter case takes one minute to reach thermal

equilibrium, ensure that the transmitter was held at the reduced temperature at least one minute prior to taking readings.

Finally, it is sometimes possible to delete or reduce accident uncertainties from calculations based on the timing of the actuation function. For example, accident effects would not have to be considered for a primary reactor trip on low reactor coolant pressure if the trip function is credited for the design-basis, large break loss-of-coolant accident (LOCA) only. This is true because the trip signal occurs very rapidly during the large immediate pressure decrease. Therefore, the trip function can be accomplished long before the environment becomes harsh enough to begin to affect equipment performance significantly or affect the analysis results. Care should be taken in using this technique to verify that the most limiting conditions for all of the applicable safety analyses are used.

6.2.5 Process measurement effects (PM)

Another source of instrument channel uncertainty that is not directly caused by equipment is process measurement effects. These are uncertainties induced by the physical characteristics or properties of the process that is being measured. The decisions related to classifying process measurement uncertainties as random or bias should follow the guidance presented in [6.2.1](#).

Several types of process uncertainties may be encountered in instrumentation design. A few of the most common process uncertainty terms are discussed in the appendices. The applicability of all possible process measurement effects should be considered when preparing uncertainty calculations.

6.2.6 Calibration uncertainty (CE)

Calibration is performed to verify that equipment performs to its specifications and, to the extent possible, to eliminate bias uncertainties associated with installation and service; for example, head effects and density compensations. Calibration uncertainty refers to the uncertainties introduced into the instrument channel during the calibration process. This includes uncertainties introduced by test equipment, procedures, and personnel.

This section deals only with calibration uncertainties and how they should be included in the total instrument channel uncertainty calculation. However, other effects, such as installation effects (if the instrument is removed from the field for calibration and then reinstalled), should be accounted for. Also, this recommended practice assumes that the calibration of a module is performed at approximately the same temperature, so that temperature effects between calibrations are minimized.

6.2.6.1 Measuring and test equipment (M&TE) uncertainty

Several effects should be considered in establishing the overall magnitude of the M&TE uncertainty. These include the reference accuracy of the M&TE, the uncertainty associated with the calibration of the M&TE, and the readability of the M&TE by the technician. Frequently, a standard M&TE uncertainty (such as $\pm 0.5\%$) is assumed. This approach is acceptable provided care is taken to ensure the M&TE is bounded by the standard number.

The reference accuracy (RA) of the M&TE is generally available from the M&TE vendor. Note that the RA may be different for different scales on the M&TE.

M&TE should be periodically calibrated to controlled standards to maintain their accuracies. Typically, the RA of these standards is such that there is an insignificant effect on the overall channel uncertainty. However, if a standard does not meet the guidelines of IEEE Standard 498; i.e., 4 to 1 better than the M&TE, this effect may need to be evaluated. If the RA of the standard is included in the uncertainty calculation, it may be combined with the RA of the M&TE using the SRSS techniques to establish a single value for the uncertainty of that piece of M&TE.

For example,

$$MTE = (RA_{MTE}^2 + RA_{STD}^2)^{1/2} \quad (\text{Eq. 6.6})$$

where

MTE = uncertainty of the M&TE

RA_{MTE} = reference accuracy of the M&TE

RA_{STD} = reference accuracy of the controlled standard

The technician performing an instrument calibration (or the periodic calibration of M&TE) introduces additional uncertainty into the instrument loop. This uncertainty is introduced from reading the instruments used in the calibration process. If the piece of M&TE has an analog scale, in addition to the movement uncertainty, the specific use of the scale should be considered to assess the uncertainty. If the calibration process is arranged such that the scale divisions are always used and there is no parallax, it is reasonable to assume no technician uncertainty since the pointer can be easily aligned with the fixed markings. If the points to be read lie between divisions, it is reasonable to assign an uncertainty. This turns into a judgment call on the part of the preparer. For example, if the scale spacing is "wide," $\pm 20\%$ of the difference between divisions could be assigned to the technician's uncertainty. Where the divisions are more closely spaced, $\pm 50\%$ of the difference may be a better choice.

As before, any uncertainty assigned because of uncertainties in reading during the calibration process should be converted to the appropriate units and combined with the M&TE uncertainty to obtain a more correct representation of the calibration process uncertainty. SRSS techniques may be used.

For example,

$$MTE = (RA_{MTE}^2 + RD^2)^{1/2} \quad (\text{Eq. 6.7})$$

where

RD = reading uncertainty

If the M&TE has an uncertainty due to the standard used in its calibration and has a reading uncertainty, the uncertainty of the M&TE would be

$$MTE = (RA_{MTE}^2 + RA_{STD}^2 + RD^2)^{1/2} \quad (\text{Eq. 6.8})$$

The same units used to calculate the overall M&TE uncertainty should be used to calculate the instrument channel uncertainty. If the instrument channel uncertainty calculation uses units of percent span, the M&TE uncertainty should be converted to percent span of the instrument channel. For example, if a piece of M&TE has a reference accuracy of 0.025 percent of its span, if its span is 0 to 3,000 psi, and if it is used in an instrument channel with a span of 1,000 psi, the M&TE reference accuracy is

$$(3,000 \text{ psi}) / (1,000 \text{ psi}) \times 0.025\% = 0.075\% \text{ span of the instrument channel.}$$

The M&TE uncertainty for a module should include the uncertainty of both the input and the output test equipment. Typically, both the input and output calibration test equipment are considered independent. These individual uncertainties may be combined by the SRSS method to establish the overall M&TE uncertainty.

For example, using the diagram of [Figure 4](#), the sensor M&TE uncertainty (SMTE) may be calculated as follows:

$$SMTE = [(MTE_1)^2 + (MTE_2)^2]^{1/2} \quad (\text{Eq. 6.9})$$

where

MTE_1 = the uncertainty associated with the sensor input test equipment (M&TE labeled Number 1 in [Figure 4](#))

and

MTE_2 = the uncertainty associated with the sensor output test equipment (M&TE labeled Number 2 in [Figure 4](#))⁴.

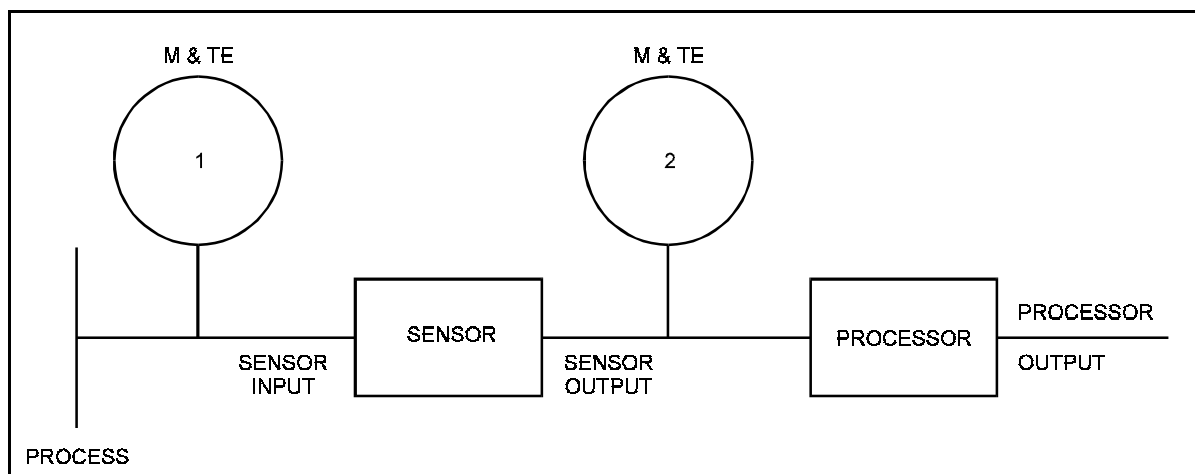


Figure 4. Combining measuring and test equipment uncertainty

If the overall uncertainty of the M&TE used in a calibration of a module is less than 1/10th of the reference accuracy of the module being tested, the uncertainty associated with the M&TE is negligible and may be disregarded (See CFR Reference)⁵. For example, if the reference accuracy of a sensor is ± 0.5 percent of span, the overall accuracy of the M&TE may be disregarded if it is better than ± 0.05 percent of the sensor span. If the M&TE is not that accurate, the uncertainty should be taken into account.

M&TE uncertainty should be considered for each separate calibration in an instrument channel. If an entire instrument channel is calibrated at one time, sometimes called a "string calibration," only one M&TE uncertainty value need be included. However, if each individual module in an instrument channel is calibrated separately without a channel verification, an M&TE uncertainty should be associated with each module.

The M&TE uncertainties used in the calculation should consider the M&TE module reference accuracy, the M&TE calibration standard, uncertainties associated with reading the M&TE, and any additional uncertainties introduced during the calibration process. The values should be consistent with the uncertainties associated with the actual M&TE specified in the calibration

⁴ The module transfer function is assumed to be linear. Refer to 6.3.1 for the treatment of nonlinear modules.

⁵ This recommended practice does not establish accuracy requirements for M&TE. This discussion simply identified an accuracy for M&TE that is mathematically insignificant.

procedure. This is to allow the technicians performing instrument calibrations to remain within the assumptions of the setpoint uncertainty calculation. In practice, this may mean specifying in the procedures and in the calculation the specific model of test equipment to be used and the scale on which the test equipment is to be read. An alternative to this would be to establish a bounding reference accuracy for the M&TE in the calibration procedure and then establish a bounding assumption with appropriate justification for the M&TE uncertainty in the setpoint uncertainty calculation.

6.2.6.2 Calibration tolerance

Calibration tolerance is the acceptable parameter variation limits above or below the desired output for a given input standard associated with the calibration of the instrument channel. Typically, this is referred to as the setting tolerance of the width of the "as-left" band adjacent to the desired response. To minimize equipment wear and to provide for human factor considerations, a band rather than a single value should be specified in the calibration procedure. This may be a symmetrical band about a setpoint; e.g., 109% $\pm 1\%$, or, in some cases, a nonsymmetrical band about a setpoint; e.g., 110% +0%, -2%. This calibration tolerance is usually based on the reference accuracy of the module being calibrated. However, individual plant calibration philosophies may specify a smaller or larger calibration tolerance. The size of the calibration tolerance should be established based on the reference accuracy of the module, the limitations of the technician in adjusting the module, and the need to minimize maintenance time.

Depending on the method of calibration or performance verification, an allowance for the calibration tolerance may need to be included in the setpoint uncertainty calculation. If the method of calibration or performance verification verifies all attributes of reference accuracy^{6,7} and the calibration tolerance is less than or equal to the reference accuracy, then the calibration tolerance does not need to be included in the total instrument channel uncertainty. In this case, the calibration or performance verification has explicitly verified the instrument channel performance to be within the allowance for the instrument channel's reference accuracy in the setpoint uncertainty calculation. If the method of calibration or performance monitoring verifies all attributes of the reference accuracy and the calibration tolerance is larger than the reference accuracy, the larger value for the calibration tolerance may be substituted for the reference accuracy in the setpoint uncertainty calculation as opposed to inclusion of the calibration tolerance as a separate term. For example, if the vendor's stated reference accuracy for a particular module is 0.25%, but the calibration tolerance used in the procedure is 0.5%, the value of 0.5% may be used for the reference accuracy of the module in the setpoint uncertainty calculation with no additional allowance for calibration tolerance. In these cases, the calibration tolerance is simply the term used to represent reference accuracy in the test's performance, and it does not represent a separate uncertainty term in the setpoint uncertainty calculation.

If the method of calibration or performance verification does not verify all attributes of the reference accuracy, the potential exists to introduce an offset in the instrument channel's performance characteristics that is not identified in the calibration or performance verification of the instrument channel. Usually, the offset is very small; however, the upper limit would be the calibration tolerance. In this case, the reference accuracy and calibration tolerance are separate terms, and, therefore, both should be accounted for in the setpoint uncertainty calculation. Several methods are possible to account for the combination of reference and calibration tolerance. The following discussion provides some examples of these methods but is not intended to be all-inclusive:

⁶ Reference accuracy is typically assumed to have four attributes: linearity, hysteresis, dead band, and repeatability.

⁷ ANSI/ISA-S51.1 indicates that an instrument channel should be exercised up and down a number of times to verify reference accuracy.

- a) One bounding method is to account for not verifying all attributes of reference accuracy by the calibration or performance verification by including allowances for both in the setpoint uncertainty calculation as explicit terms.
- b) Another method is to establish a calibration tolerance that is less than the reference accuracy. If the difference between calibration tolerance and reference accuracy accounts for the uncertainty of the various attributes that are not verified during calibration or performance verification, only reference accuracy would be included in the setpoint uncertainty calculation.
- c) A third method is to determine an allowance based on uncertainty algorithms or magnitudes that are known to be conservative. This may result in sufficient margin to provide a bounding allowance for reference accuracy and calibration tolerance without explicit terms for them in the setpoint uncertainty calculation. An example of this method would be to algebraically add the reference accuracy, drift, and M&TE uncertainties for a module rather than taking the SRSS (which assumes that these uncertainties are independent) of these uncertainties. However, the availability of this margin should be demonstrated prior to implicit reliance on this method.
- d) A fourth method is to include a specific allowance in the setpoint uncertainty calculation for the attributes of reference accuracy that are not verified in the calibration or performance verification. For example, if the calibration or performance verification does not exercise an instrument channel more than once to demonstrate repeatability, it may be appropriate to include an allowance for repeatability in the setpoint uncertainty calculation. If a channel performs functions in both the increasing and decreasing directions and the calibration or performance verification does not check the accuracy in both directions, it may be appropriate to provide an allowance for hysteresis in the setpoint uncertainty calculation. If the calibration or performance verification does not check accuracy in the area of the trip functions, it may be appropriate to provide an allowance for linearity in the setpoint uncertainty calculation.

6.2.6.3 "As-found/as-left" calibration values

During calibration of a module, "as-found" and "as-left" data are typically obtained and recorded. If practicable, the "as-found" data should be taken without previously exercising the module, thereby providing a better indication of how the module would have performed if called upon by changes in the process. The difference between the "as-found" data of the current calibration and the "as-left" data from the previous calibration represents the net effects of several uncertainties, including the repeatability (reference accuracy) and drift of the module over the calibration interval. If the ambient temperature in the area of the module was not the same for the two calibrations, part of the difference between the "as-found" and "as-left" data may be due to temperature effects. "As-found" and "as-left" data may be analyzed to estimate a value for drift for the module, recognizing that variations in environmental conditions and other uncertainties may be present at the time of the calibration and, if appropriate, accounted for when analyzing "as-found" and "as-left" data.

Nominal values and generic module performance data may be used for calculating module uncertainties to establish setpoints for initial plant operation. These nominal values may be refined after sufficient operating experiences and plant-specific data are available. Plant-specific data is more representative of each module's performance within its unique installation and applications characteristics and can be used to calculate smaller module drift uncertainties. Reducing module drift uncertainties allows one to revise setpoints to provide increased margin between the setpoint and expected process conditions during normal plant operating conditions. However, care should be taken to ensure that the use of plant-specific data is based on generally accepted statistical principles since limited sample sets may be unnecessarily conservative.

6.2.6.4 Calibration corrections

Frequently, calibration procedures include corrections to account for the difference in instrument performance or readings between calibration conditions and normal operating conditions, such as static pressure and head pressure corrections. If these corrections have been made, the setpoint uncertainty calculation does not need to include them (however, the uncertainty of these corrections should be included). The fact that these corrections are made during calibration should be identified in the setpoint uncertainty calculation.

6.2.7 Drift

An assumption for the time intervals between recalibration of each instrument should be included in the setpoint uncertainty calculation. This time interval is used to calculate the drift uncertainty (DR) for the instrument using manufacturer's specifications such as:

$\pm 0.25\%$ URL for a six-month period.

This example illustrates how uncertainties in (% URL) percent upper range limit can be converted to percent span (% span). For example, assume a pressure transmitter with a URL of 1000 psig is calibrated to 0-500 psig. With an 18-month test interval, the drift uncertainty is calculated as follows:

$$\begin{aligned}\text{DR} &= [\pm(0.25\%)(\text{URL})/(\text{span})] (18 \text{ months}/6 \text{ months}) \\ &= (\pm 0.25\%)(1000 \text{ psig}/500 \text{ psig})(3) \\ &= \pm 1.5\% \text{ span}\end{aligned}$$

This assumes the drift term is a linear function of time. In the absence of other data, it is considered reasonable, and perhaps conservative, to make this assumption.

Other methods for extending drift data may be used. If one assumes that drift during each drift period is random and independent, the SRSS of the individual drift periods between calibrations may be used. In this case, it would be

$$\text{DR} = \pm[(0.25\% \text{ URL})^2 + (0.25\% \text{ URL})^2 + (0.25\% \text{ URL})^2]^{1/2}$$

since there are three 6-month periods in the 18-month calibration interval; or

$$\begin{aligned}\text{DR} &= \pm[(3)(0.25\% \text{ URL})^2]^{1/2} \\ \text{DR} &= \pm 0.433\% \text{ URL}\end{aligned}$$

Some vendor data has also suggested that the majority of an instrument's drift will occur in the first several months following a calibration, and that the instrument output will not drift significantly after the "settle in period." In this case, the 6-month value provided by the vendor may be acceptable for the 18-month calibration interval.

Whichever method is used, it should be listed as an assumption to the setpoint uncertainty calculation, and some justification should be provided. The term (URL/span) is a dimensionless quantity commonly referred to as the turndown factor (TDF). It can be multiplied by an uncertainty term in % URL to convert directly to % span. Note that drift may be stated in % URL or % span. It was given in % URL previously simply to illustrate the use of the TDF.

It should also be noted that the test interval is the time between calibrations, including any allowed extensions, and is not necessarily equivalent to the time between refueling outages. This should be considered in estimating the value to be used for drift.

6.2.8 Module power supply variations

Most electronic instruments exhibit a change in output because of variations in power supply voltage. A typical manufacturer's specifications may read

$\pm 0.01\%$ span per volt variation.

To calculate the uncertainty associated with the power supply effect (PS), a normal operating voltage (OV), and voltage variation (VV) should be determined. Once these points are defined, if the effect is linear, an expression similar to Equation 6.3 can be used to calculate the uncertainty associated with the power supply effect. Typically, this uncertainty is very small in comparison to other instrument channel uncertainties.

6.2.9 Additional considerations for digital signal processing

In channels using digital processing equipment, uncertainties are introduced by hardware for conversions between analog and digital domains and by the algorithms for digital arithmetic operations. Values for analog to digital (A/D) and digital to analog (D/A) conversion uncertainties may be obtained from the module manufacturers or through testing. Sources of uncertainty may include: precision of computation, rounding or truncation uncertainties, process variable changes during the deadband between data acquisition sampling scans, and inaccuracies of algorithms for transcendental functions or empirical curve fitting. The nature of the uncertainties contributed by the software (that is, whether they are statistical or algebraic) should be identified by the software designer. When the uncertainties are characterized and quantified, they can be combined with propagated uncertainties by the methods described in 6.3. Further discussion is provided in [Appendix H](#).

6.2.10 Insulation resistance effects

Under the conditions of high humidity and temperature associated with high energy line breaks (HELB), cables, splices, connectors, terminal blocks, and penetrations experience a reduction in insulation resistance (IR). Reduction in IR causes an increase in leakage currents between conductors and from individual conductors to ground. Leakage currents are negligibly small under normal conditions. These currents are essentially calibrated out during instrument channel calibrations. However, under the HELB event, the leakage currents may increase to a level that causes significant uncertainty in measurement. The effect is particularly a concern for sensitive, low signal level circuits such as current transmitters, RTDs, and thermocouples. For a more detailed discussion on determining the IR effect, [see Appendix D](#).

6.2.11 Sources of uncertainty data

The most reliable method of developing and substantiating uncertainty data is to perform controlled tests on the devices that impose the conditions that have the potential to cause uncertainties in the device, or to analyze the performance data gained from operation and maintenance of the equipment. This method has been widely applied to determine the uncertainties due to extreme temperature, pressure, and radiation levels. The allowances derived from the test should consider the ability of the test to replicate the conditions and the accuracy and thoroughness of the test as discussed in 6.2.4.

A more common source of data is from the instrument supplier. Performance specifications should be provided by instrument or reactor vendors. Data should include reference accuracy, drift (stability), environmental effects, and reference conditions. Since performance specifications often describe a product line, any single instrument may perform significantly better than the group specification. Performance specifications may be obtained through the review of published information or through communication with the vendor. Test data may or may not be available to support the performance specifications since this data is generally applied to conditions under

which the device routinely operates. Therefore, the performance specifications may have been informally validated through the use and maintenance of the equipment.

If performance summary data is not available or if it does not satisfy the needs of the users, raw test data may need to be reevaluated or created from additional testing.

Occasionally, the situation arises when the data necessary for a setpoint calculation is not readily available; that is, test results or vendor literature do not exist. Several approaches may be taken in these cases. If possible, it is usually best to obtain a recommendation from the manufacturer or other utility/customer based on its experience with the instrumentation. Another approach might include performing circuit analysis of electronic circuits and/or using data associated with an instrument with similar principles of operation, made by another manufacturer. In some cases there may be no prudent alternative but the common practice of using engineering judgment, in lieu of vendor literature or test data. The use of engineering judgment in these cases must be tempered by the importance of the setpoint, which can be defined in a graded approach setpoint program. With any of these approaches it is appropriate to apply some conservatism to the uncertainty values and to provide written justification for the values utilized.

6.2.12 Interpretation of uncertainty data

The proper interpretation of uncertainty information is necessary to ensure the validity of the setpoint calculation. Historically, there have been many different methods of representing numerical uncertainty. Almost all suffer from the ambiguity associated with shorthand notation. The symbol $\pm$, for example, without further explanation, is often interpreted as the symmetric probability interval associated with a random, normally distributed uncertainty. Further, the probability level may be assumed to be 50% (probable error), 68.27% (one sigma), 95.45% (two sigma), or 99.73% (three sigma). Still others may assume that the $\pm$ symbol defines the limits of error (reasonable bounds) of bias or non-normally distributed uncertainties. Discussions with the vendor may provide helpful insight for interpreting performance specifications or test results.

It is the user's responsibility to avoid improper use of the vendor performance data. If a vendor-published value of an uncertainty term (source) is believed to contain a significant bias uncertainty, then the $\pm$ value should be treated as estimated limit of error. Simple field tests (repeated measurement) by the user can give an indication of the random component of the published value, if separation of components is desirable. If based on engineering judgment, the term is believed to represent only random uncertainties (no significant bias uncertainties), then the $\pm$ value may be treated as a value suitable for inclusion in the SRSS combination.

One source of performance data that requires careful interpretation is that obtained during harsh environment testing. Often such tests are conducted only to demonstrate functional capability of a particular instrument in a particular harsh environment. This usually requires only a small sample size and invokes inappropriate rejection criteria for a probabilistic determination of instrument uncertainties. This type of data base typically results in limits of error (reasonable bounds) associated with bias or non-normally distributed uncertainties.

The sample size should be considered prior to adjusting the measured net effects for normal environmental uncertainties, reference accuracies, etc. The results of such tests describe several mutually exclusive categories of uncertainty. For example, the results of a severe environment test contain uncertainty contributions from the instrument reference accuracy, M&TE uncertainty, calibration uncertainty, and others, in addition to the severe environment effects. A conservative practice is to treat the measured net effects as only uncertainty contributions due to the harsh environment.

Occasionally, select test data may appear inconsistent with the majority of the test data collected. In this situation it may be possible to justify the inconsistent data as outliers. Analytical

techniques for this purpose are discussed in ANSI N15.15, ANSI/ASME PTC 19.1, and ANSI/ASTM E 178. Additionally, Appendix J provides further discussion on statistical analysis.

6.3 Calculating total channel uncertainty

The calculation of an instrument channel uncertainty should be done in a clear, straightforward process. The actual calculation can be done with a single-loop equation that contains all potential uncertainty values or by a series of related term equations. Either way, a specific instrument channel calculation should be laid out to coincide with a channel's layout from process measurement to final output module or modules.

The actual technique and layout of the calculation is influenced by the type of instrument channel being analyzed. While many channels can be analyzed using the basic formulas defined in 6.1, channels that contain modules with transfer functions such as an amplifier, summer, square root extractor, etc., require special consideration. This is due to the effect the transfer function can have on the incoming signal and its associated uncertainty. The module's transfer function will act on both the true signal and its uncertainty to develop an output. Thus, the uncertainty within a signal may be increased or decreased by a module's transfer function, with respect to the true signal.

A detailed look at the propagation of uncertainty through functional modules is provided in 6.3.1. Both the equations developed using the techniques of 6.3.1 and the basic equations of 6.1 must be used to analyze a channel's uncertainty. A discussion on the application of the basic statistical equations for an instrument channel that does not contain modules with transfer functions is provided in 6.3.2, while 6.3.3 provides a discussion on the application of the uncertainty propagation equations.

6.3.1 Equations for the propagation of uncertainties through functional modules

If signal conditioning modules such as scalars, amplifiers, summers, square root extractors, multipliers, etc., are used in the instrument channel, the module's transfer function should be accounted for in the instrument setpoint/uncertainty calculation. The uncertainty of a signal conditioning module's output can be determined when the uncertainty of the input signal and the uncertainty associated with the module, as well as the module's transfer function, are known. Using partial derivatives or perturbation techniques (refer to Appendix K for a detailed discussion of these techniques), equations have been developed to determine the output signal uncertainties for several common types of signal conditioning modules and are presented in Table 1. The equations are applicable to all signal conditioning modules of that type, regardless of the manufacturer.

The attributes of uncertainties such as randomness or independence are discussed in detail in 6.2.1. For simplicity, the equations presented in Table 1 are based on the assumption that the input uncertainties consist of either all random or all biased uncertainties. The user must take care in applying these equations to individual instrument channel uncertainty calculations to ensure that the probability and confidence levels of the data and resulting uncertainty values are maintained. In balancing the requirements of calculation conservatism, probabilities, and operating margins, it may be beneficial to optimize the uncertainty determination by computer simulation techniques. The more general case of uncertainties with both random and biased components is addressed in Appendix K.

It is important to note that the method of calibration or testing may directly affect the use of the information presented in this section. If, for example, a group of the modules for a particular instrument channel is always tested and calibrated together, it may be treated as a single module. The uncertainties associated with the output of the group treated as a single module

would be equal to or less than the uncertainties calculated by combining each of the individual modules' uncertainties.

6.3.2 Application of basic uncertainty propagation equations

For single instrument channels that do not have transfer functions or that have linear transfer functions, the formulas of 6.1 can be used directly to calculate instrument channel uncertainty. The basic formulas may also be applied to multiple signal channels that have linear transfer functions, as long as the transfer functions have a unity gain. The instrument channel equation would take the form:

$$CU^+ = +[PM^2 + PE^2 + module_1^2 + module_2^2 + module_n^2]^{1/2} + B_t^+ \quad (\text{Eq. 6.10a})$$

$$CU^- = -[PM^2 + PE^2 + module_1^2 + module_2^2 + module_n^2]^{1/2} - B_t^- \quad (\text{Eq. 6.10b})$$

where

CU = channel uncertainty. The CU is the total uncertainty at a designated point in the channel. The CU can be calculated for any point in a channel from module 1 to module n, as needed.

PM = process measurement uncertainty. PM accounts for the variation in actual process conditions that influence the measurement, such as temperature stratification, density variations, pressure variations, etc.

PE = primary element accuracy. PE is the accuracy of a component, piece of equipment, or installation used as a primary element to obtain a given process measurement. The PE includes the accuracy of flow nozzle and/or the accuracy achievable in a specific flowmetering run.

Module_n = total random uncertainty of each module that makes up the loop from module 1 through module n.

B_t⁺ = total of all positive biases associated with an instrument channel, including any uncertainties from PM, PE, or the modules that could not be combined as a random term (biases and abnormally distributed uncertainties as discussed in 6.1).

B_t⁻ = total of all negative biases associated with an instrument channel, including any uncertainties from PM, PE, or the modules that could not be combined as a random term (biases and abnormally distributed uncertainties as discussed in 6.1).

The individual module random uncertainties are in themselves a statistical combination of uncertainties. Depending on the type of module, its location, and the specific factors that can affect its accuracy, the determination of the module uncertainty will vary. For example, the module uncertainty may be calculated as

$$e^+ = +[RA^2 + DR^2 + TE^2 + RE^2 + SE^2 + HE^2 + SP^2 + MTE^2]^{1/2} + B^+ \quad (\text{Eq. 6.11a})$$

$$e^- = -[RA^2 + DR^2 + TE^2 + RE^2 + SE^2 + HE^2 + SP^2 + MTE^2]^{1/2} - B^- \quad (\text{Eq. 6.11b})$$

where

e = uncertainty of module.

RA = module reference accuracy (usually specified by the manufacturer).

DR = drift of the module over a specific period.

TE = temperature effect for the module; the effect of ambient temperature variations on module accuracy; the TE may be a normal operating TE or an accident TE, as required.

- RE = radiation effect for the module; the effect of radiation exposure on module accuracy; the RE may be a normal operating RE, an accident RE, or time of trip RE as required.
- SE = seismic effect or vibration effect for the module; the effect of seismic or operational vibration on the module accuracy.
- HE = humidity effect for the module; the effect of changes in ambient humidity on module accuracy, if any.
- SP = static pressure effects for the module; the effect of changes in process static pressure on module accuracy.
- MTE = measurement and test equipment effect for the module; this accounts for the uncertainties in the equipment utilized for calibration of the module.
- B = biases associated with the module, if any.

For the purposes of the previous example, most of the uncertainties have been considered as random and independent. However, the user must determine the actual characteristics of each uncertainty term and combine them based on the criteria discussed in 6.1. Additional terms may have to be included for a particular application. The terms shown are the most common ones encountered for a module.

The individual module uncertainty formulas would contain all appropriate terms for a specific module including any bias terms. The final instrument channel formula bias terms, B^+ and B^- , would be the sum of the individual biases. For example, for the total instrument channel, if PM contained a +3.0%, -0.0% reference leg bias, module 1 contained a $\pm 0.5\%$ calibration abnormally distributed uncertainty, and the instrument channel could experience a +1.0% insulation resistance (IR) degradation effect

$$B^+ = B_{PM}^+ + B_{IR}^+ + B_1^+ = 3.0\% + 1.0\% + 0.5\% = + 4.5\%$$

$$B^- = B_1^- = -0.5\%$$

Table 1. Equations for propagation of input uncertainties through modules for various mathematical functions

FUNCTION/EQUATION (Notes 1, 2, 3, 4, and 7)

Fixed Gain Amp

$$C = K * A$$

$e_{C(ALG)} = K * e_{A(B)}$	Eq. (6.12)
$e_{C(SRSS)} = K * e_{A(R)}$	Eq. (6.13)

Summation

$$C = (K1 * A) + (K2 * B)$$

$e_{C(ALG)} = (K1 * e_{A(B)}) + (K2 * e_{B(B)})$	Eq. (6.14)
$e_{C(SRSS)} = [(K1 * e_{A(R)})^2 + (K2 * e_{B(R)})^2]^{1/2}$	Eq. (6.15)

Multiplication

$$C = (K1 * A) * (K2 * B)$$

$e_{C(ALG)} = (K1 * K2) * [(A * e_{B(B)}) + (B * e_{A(B)}) + (e_{A(B)} * e_{B(B)})]$ $\approx (K1 * K2) * [(A * e_{B(B)}) + (B * e_{A(B)})]$	Eq. (6.16)
$e_{C(SRSS)} = (K1 * K2) * [(A * e_{B(R)})^2 + (B * e_{A(R)})^2 + (e_{A(R)} * e_{B(R)})^2]^{1/2}$ $\approx (K1 * K2) * [(A * e_{B(R)})^2 + (B * e_{A(R)})^2]^{1/2}$	Eq. (6.17)

Division

$$C = (K1 * A) / (K2 * B)$$

$e_{C(ALG)} \approx \frac{K1}{K2} * \left(\frac{(B * e_{A(B)}) - (A * e_{B(B)})}{B^2} \right)$	Eq. (6.18)
$e_{C(SRSS)} \approx \frac{K1}{K2} * \left(\frac{[(B * e_{A(R)})^2 + (A * e_{B(R)})^2]^{1/2}}{B^2} \right)$	Eq. (6.19)

Logarithmic Amplification $C = K1 + (K2 * \text{Log } A)$

$e_{C(\text{ALG})} \approx \left(\frac{K2 * \text{Log}(e)}{A} \right) * e_{A(B)}$	Eq. (6.20)
$e_{C(\text{SRSS})} \approx \left(\frac{K2 * \text{Log}(e)}{A} \right) * e_{A(R)}$	Eq. (6.21) Note 6

Squaring $C = A^2$

$e_{C(\text{ALG})} \quad A = (2A * e_{A(B)}) + (e_{A(B)})^2$ $\text{for } \frac{e_{A(B)}}{A} < 1, \quad e_{C(\text{ALG})} \approx 2(A * e_{A(B)})$	Eq. (6.22)
$e_{C(\text{SRSS})} \approx 2A * e_{A(R)}$	Eq. (6.23) Note 6

Multiplication with Division $C = (K * A * B) / D$

$e_{C(\text{ALG})} \approx K * \left(\left(\frac{B}{D} * e_{A(B)} \right) + \left(\frac{A}{D} * e_{B(B)} \right) - \left(\frac{A * B}{D^2} * e_{D(B)} \right) \right)$	Eq. (6.24)
$e_{C(\text{SRSS})} \approx K * \left(\left(\frac{B}{D} * e_{A(R)} \right)^2 + \left(\frac{A}{D} * e_{B(R)} \right)^2 + \left(\frac{A * B}{D^2} * e_{D(R)} \right)^2 \right)^{\frac{1}{2}}$	Eq. (6.25)

Square Root Extraction $C = (A)^{1/2}$

$e_{C(\text{ALG})} = (A + e_{A(B)})^{1/2} - (A)^{1/2}$ $\text{for } \frac{e_{A(B)}}{A} < 1, \quad e_{C(\text{ALG})} \approx \frac{e_{A(B)}}{2(A)^{1/2}}$	Eq. (6.26)
$e_{C(\text{SRSS})} \approx \frac{e_{A(R)}}{2(A)^{1/2}}$	Eq. (6.27) Note 6

Square Root with Multiplier

$$C = K * (A * B)^{1/2}$$

$e_{C(ALG)} \approx \frac{K}{2} * \frac{(B * e_{A(B)}) + (A * e_{B(B)})}{(A * B)^{1/2}}$	Eq. (6.28)
$e_{C(SRSS)} \approx \frac{K}{2} * \frac{[(B * e_{A(R)})^2 + (A * e_{B(R)})^2]^{1/2}}{(A * B)^{1/2}}$	Eq. (6.29)

LEGEND

A, B, D	=	input signals (in signal units).
C	=	output signals (in signal units).
$e_{A(R)}, e_{B(R)}, e_{D(R)}$	=	random-normal input uncertainties (in signal units).
$e_{A(B)}, e_{B(B)}, e_{D(B)}$	=	biased input uncertainties (in signal units).
$e_{C(ALG)}$	=	algebraic (biased) output uncertainty (in signal units).
$e_{C(SRSS)}$	=	random-normal (or nearly normal) distributed output uncertainty (in signal units).
K, K1, K2	=	arbitrary multipliers of input signals (dimensionless gains or attenuations).

NOTES:

1) The equations in this table describe the propagation of one or more input signal errors through functional modules. Where multiple inputs are involved, the equation also accounts for combination of the input errors. For the derivation of the equations for error propagation through multiple variable functions, see Section 6 of ANSI/ASME PTC 19.1.

2) Equations marked (ALG) must be used for bias errors or for errors with non-normal distributions when the SRSS method would yield non-conservative results.

3) Equations marked (SRSS) may be used when input signal errors are random with a normal distribution. When input signal errors' distributions are not normal, these equations should not be used unless it can be demonstrated that results are conservative.

4) For single-input functions (e.g., Fixed Gain Amplifier), the "SRSS" designation means that a normal input error distribution results in normal (or near normal) output error that can be combined with other random-normal error terms using the SRSS method.

For multiple-input functions (e.g., Multiplier), the "SRSS" designation means that the output error is calculated using the SRSS method for combining the input errors that are random-normally distributed, and that output errors with this designation may be combined with other error terms using the SRSS method.

5) Equation 6.13 is valid for input errors of any magnitude. The output distribution will be the same as the input distribution because the transfer function is linear. The output error can be combined with other normally distributed error terms using the SRSS method.

6) Equations 6.21, 6.23, and 6.27 are valid if input errors are sufficiently small so that the output error distribution is nearly normal. Output errors can then be combined with other normally distributed error terms using the SRSS method.

7) In some cases it may be more convenient to use the relative form of the error propagation equations, that is e_c/C . Since the derivation of these equations is beyond the scope of this recommended practice, refer to ANSI/ASME PTC 19.1 for more information.

An instrument channel calculation should account for the effects of each module in the channel on total uncertainty as well as the external (noninstrument-induced) effects that act on the total uncertainty.

The individual instrument channel module terms would be derived based on the module type. These terms account for both the effect a module has on instrument channel uncertainty due to its own inaccuracies as well as its effect on instrument channel uncertainty due to its manipulation of incoming uncertainty values.

As with any engineering calculation, proper determination and accounting of engineering units is essential. This can become a major stumbling block to an analysis due to the myriad of ways uncertainty is specified. The basic formula is not affected by units as long as they are consistent. Either actual process measurement units or a representative unit such as percent span may be used. This document uses percent span as the base unit. This affords a universal appeal to the examples and provides for ease of comparison between different types of instrument channels. Specific examples of calculating total instrument channel uncertainty are provided in [Appendix L](#).

6.3.3 Application of uncertainty propagation equations for multiple signals or non-linear channels

For channels that contain multiple signals that interact or for channels that contain nonlinear transfer function modules, the instrument channel uncertainty may be calculated using the equations of [Table 1](#). The instrument channel uncertainty calculation uses the equations of [6.1](#) to combine all uncertainties prior to and downstream of the transfer function module and the equations of [Table 1](#) to determine the uncertainty through the function.

A typical instrument channel calculation for an instrument channel containing a square root module could take the form

$$\begin{aligned}
 a &= (PM^2 + PE^2)^{1/2} \\
 CU^+ &= + \left\{ \left[\frac{a}{(2 * A^{1/2})} \right]^2 + \text{module}_1^2 + \text{module}_2^2 + \text{module}_N^2 \right\}^{1/2} + \\
 &\quad \dots [(A + B_i^+)^{1/2} - A^{1/2}] + B_{TD}^+ \\
 CU^- &= - \left\{ \left[\frac{a}{(2 * A^{1/2})} \right]^2 + \text{module}_1^2 + \text{module}_2^2 + \text{module}_N^2 \right\}^{1/2} - \\
 &\quad \dots [A^{1/2} - (A - B_i^-)^{1/2}] - B_{TD}^-
 \end{aligned}$$

where

- PM, PE, & CU = are as defined in 6.3.2.
- module 1 = random uncertainty of the square root module.
- module 2, N = total random uncertainties of each of the remaining modules that make up the loop.
- a = random uncertainty in the input signal entering the square root module (module 1).

- A = magnitude of the input signal to the square root module.
- B_i^+, B_i^- = positive and negative biases associated with the input signal, if any.
- B_{TD}^+, B_{TD}^- = total positive and negative biases associated with the modules downstream of square root module, if any.

In dealing with channels that contain nonlinear transfer functions, the uncertainty value is dependent on the relative magnitude of the input signal. This can be seen in the above equations. With the input uncertainty held constant, the instrument channel will increase as the input signal decreases and vice versa. As a result, it is generally advantageous to calculate the uncertainty of loops containing nonlinear modules in terms of specific readings and not percent span. The above square root extractor equation assumes an input magnitude of at least 50 percent. For smaller values, a more rigid equation must be used to maintain the probability and confidence levels of the data. Care must be taken in establishing the proper uncertainty transfer function for nonlinear devices since the nonlinear devices can skew both the probability levels and the confidence levels of the resulting uncertainty value.

One common method used in engineering calculations is to linearize a nonlinear function over a relatively small range of interest. Then errors can be propagated through the device using relatively simple linear techniques. When using this method, care must be taken to account for any modelling uncertainties generated by the linear approximation. One must also ensure that the uncertainty to be propagated is contained in the linearized range.

7 Establishment of setpoints

7.1 Setpoint relationships

The establishment of setpoints and the relationships between trip setpoint, allowable value, analytical limit, and safety limit are discussed in ISA-S67.04-1994. A thorough understanding of these terms is important in order to properly utilize the total instrument channel uncertainty in the establishment of setpoints. [Figure 5](#) presents the relative position of the safety limit, analytical limit, allowable value, and the trip setpoint with respect to the normal operating point.

Safety limits are chosen to protect the integrity of physical barriers that guard against the uncontrolled release of radioactivity. The safety limits are typically provided in the plant technical specifications and safety analyses.

The analytical limit is established to ensure that the safety limit is not exceeded. The analytical limit is developed from event analyses models that consider parameters such as process delays, rod insertion times, reactivity changes, instrument response times, etc. The development of the analytical limit is outside the scope of this recommended practice; however, the use of the analytical limit to obtain the allowable value and the trip setpoint will be discussed.

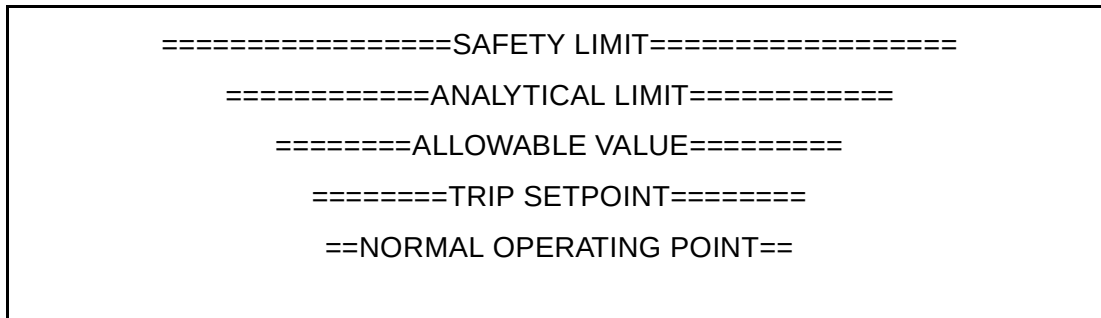


Figure 5. Setpoint relationships

The allowable value is a value that the trip setpoint might have when tested periodically, beyond which the instrument channel should be evaluated for operability. An "as-found" trip setpoint within the allowable value ensures that sufficient allocation exists between this actual setpoint and the analytical limit to account for instrument uncertainties, such as design-basis accident temperature and radiation effects or process-dependent effects, that either are not present or are not measured during periodic testing. This will provide assurance that the analytical limit will not be exceeded if the allowable value is satisfied. The allowable value also provides a means to identify unacceptable instrument performance that may require corrective action.

The trip setpoint is a predetermined value at which a bistable module changes state to indicate that the quantity under surveillance has reached the selected value. The trip setpoint is established to ensure that an instrument channel trip signal occurs before the analytical limit is reached and to minimize spurious trips close to the normal operating point of the process.

7.2 Trip setpoint determination

Several methods are available for determining the trip setpoint. Alternative methods can be used whenever documented justification is provided. One such method of calculating the trip setpoint is by adding or subtracting the instrument channel uncertainties to the analytical limit, dependent upon the conservative direction of the process variable with respect to the analytical limit:

$$TS = AL \pm (CU + \text{margin}) \quad (\text{Eq. 7.1})$$

where

TS = trip setpoint;

AL = analytical limit;

CU = channel uncertainty;

margin = an amount chosen, if desired, by the user for conservatism of the trip setpoint.

For process variables that decrease toward the analytical limit, the instrument channel uncertainty and margin terms are added to the analytical limit. For process variables that increase toward the analytical limit, the instrument channel uncertainty and margin terms are subtracted from the analytical limit.

EXAMPLE 1

The analytical limit used in a safety analysis for a high pressurizer pressure trip during a feed line break event is 2470 psia. Using the methods in [Section 6](#), the instrument channel uncertainty for the instrument loop was determined to be as follows:

CU = +100 psi — the resulting uncertainty after combining all of the positive components;
and

-85 psi — the resulting uncertainty after combining all of the negative components.

Since the process is increasing toward the analytical limit, the resulting uncertainty after combining the negative components is used. With a margin of zero, then

$$TS = 2470 - (85 + 0) = 2385 \text{ psia.}$$

The positive channel uncertainty of +100 psi is not used since the process is increasing toward the analytical limit.

7.3 Allowable value

Several methods for determining the allowable value have been developed and are presently in use. Three methods are illustrated in [Figure 6](#). The allowance between the allowable value and the trip setpoint should contain that portion of the instrument channel being tested for the surveillance interval (monthly, quarterly, or refueling) and should account for no more than

- a) drift (based on surveillance interval);
- b) instrument calibration uncertainties for the portion of the instrument channel tested; and
- c) instrument uncertainties during normal operation that are measured during testing (see Appendix I).

In [Figure 6](#) and the discussion that follows, it is assumed that the process increases toward the analytical limit. If the process decreases toward the analytical limit, the directions given would be reversed.

In the first and second methods shown in [Figure 6](#), the allowable value (AV) is determined by calculating the instrument channel uncertainty without including those items identified previously in 7.3 (drift, calibration uncertainties, and uncertainties observed during normal operations). This result is then subtracted from the analytical limit (AL) to establish the AV. In the first method the trip setpoint is then determined by subtracting from the AV the combination of the uncertainties: drift, calibration uncertainties, and uncertainties observed during normal operation. In the second method shown in [Figure 6](#), the trip setpoint is calculated as described in [7.2](#).

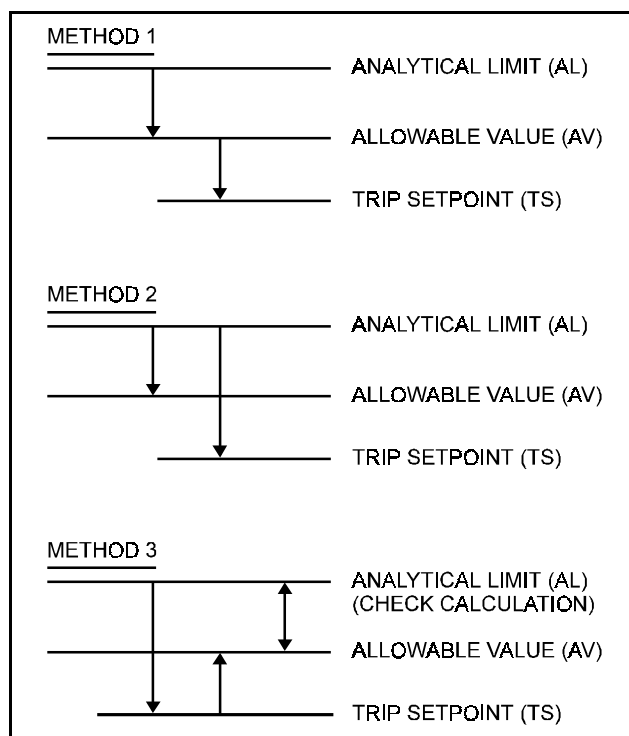


Figure 6. Methods for determining the allowable value

The third method to calculate the AV illustrated in [Figure 6](#) first calculates the trip setpoint as described in [7.2](#). Then, an allowance for the three categories of instrument uncertainty (drift, calibration uncertainty, and uncertainties during normal operation) is calculated. This allowance is then added to the trip setpoint to establish the AV. If the allowance is not determined in a method that is consistent with the method used for the determination of the trip setpoint, a check calculation should be performed. For example, if an SRSS combination is used for determining the trip setpoint and an algebraic combination is used for the allowance between the trip setpoint and the AV, a check calibration should be performed. The check calculation should provide assurance that the purpose of the AV is still satisfied by providing a large enough allowance to account for those uncertainties not measured during the test. If the check calculation identifies that there is not enough allowance between the AL and AV, the AV must be changed to provide the necessary allowance. In all cases the difference between the AV and the trip setpoint must be at least as large as the calibration tolerance discussed in [6.2.6.2](#), and, if it is not, the trip setpoint must be adjusted.

8 Other considerations

This section discusses selected subjects that may occasionally arise in instrument channel setpoint/uncertainty calculations.

8.1 Correction for setpoints with a single side of interest

For many safety-related setpoints, interest is only in the probability that a single value of the process parameter is not exceeded, and the single value is approached only from one direction. In such situations, the uncertainty value associated with single-sided distributions is smaller than the value associated with double-sided distributions. The method to calculate these smaller uncertainties values is given below.

For normally distributed 95% probability uncertainties, standardized area distribution tables (see M.R. Spiegel Reference), show that 95% of the population will have uncertainties between ± 1.96 sigma, with 2.5% falling below -1.96 sigma and 2.5% falling above $+1.96$ sigma. If there are increasing and decreasing trip limits, the appropriate limits to use are ± 1.96 sigma.

For normally distributed uncertainties, the same tables show that 95% of the population will have uncertainties less than $+1.645$ sigma (50% below the median and 45% between the median and $+1.645$ sigma) and that 95% of the population will have uncertainties greater than -1.645 sigma. If interest is only in the probability that a single value of the process parameter is not exceeded and the single value is approached only from one direction, the appropriate limit to use for 95% probability is $+1.645$ sigma or -1.645 sigma as appropriate.

Using this technique, a positive uncertainty that has been calculated for a symmetrical case can be reduced while maintaining 95% coverage of the population when a single parameter is approached from only one direction. For example, if the original symmetric value was based on 2 sigma members, the reduction factor is $1.645/2.00 = 0.8225$; if the original symmetric value was based on 1.96 sigma values, the reduction factor is $1.645/1.96 = 0.839$.

EXAMPLE 2

$$CU_{\pm} = \pm 2.00\% \text{ span (2 sigma value)}$$

The trip occurs at a single point when the process parameter is decreasing. Decreasing trips are only delayed by positive errors, errors that could make the indicated trip parameter higher than the actual trip parameter.

$$CU_{+} = 2.0 \times 0.8225 = +1.645\% \text{ span}$$

$$CU_{-} = \text{not of concern}$$

9 Interfaces

Setpoints for automatic actuation of safety equipment in nuclear power plants affect different functional organizations and are affected by many plant activities. It is important that these interfaces be fully recognized in order to maintain the plant instrument settings in full support of appropriate safety analysis and plant operational requirements. The following discussion identifies organizations and activities that typically exist in commercial nuclear power plants. These are not intended to be all-inclusive but are representative of areas where communications are necessary between organizations responsible for some aspect of safety equipment setpoint determination or control.

The safety analysis group is initially responsible for utilizing uncertainty allowances in the appropriate analysis, which would include the uncertainty of the analysis simulation. Typically, in

the past, few instrument characteristics were needed to generate analytic limits from safety limits. However, analytical methods are now taking into account the history and interrelationships of equipment performance.

The thermohydraulic and neutronic models usually require a system response time limit that is affected by both process and instrument response times. The determination for dynamic effects such as response-time limits is typically addressed in the accident analysis and is not included within the scope of this recommended practice. If dynamic effects were not accounted for in this safety analysis, additional uncertainty terms may be needed to account for them. Any design modification that changes the instrument dynamic characteristics or relocates sensors (or sensing-line taps) should be evaluated for safety-analysis impact.

The group(s) responsible for the generation of the plant-technical specification limiting safety system settings decide on appropriate allowances for instrument safety channels. If hardware allowances cannot be met by available vendors, iterations of the safety analysis or setpoint determination may be necessary.

Any design modifications that affect the measurement process should be evaluated for effects on setpoint determination. This can happen in a direct way, such as module replacement, or in a more subtle manner, such as through a support system (e.g., a modification to a room air conditioning unit/flow path). Proper module selection is important to match the ratings and performance of the module to the instrument channel application and design requirements. Another activity that causes a reexamination of the safety analysis is the periodic fuel reload. During the reload process, a safety evaluation is performed to verify that the existing analysis remains applicable. If it is determined that the existing analyses are no longer valid, additional safety analyses are performed. At this point, the assumptions and results of the safety analyses should be reviewed to determine their impact on the instrumentation setpoint determination.

The plant maintenance/instrumentation group is usually responsible for instrument calibration and the collection of performance data. The authors of maintenance procedures should ensure that appropriate limits are placed on the use of test equipment. This should include the M&TE itself, as well as any additional uncertainties covered by the calibration procedure or technique.

The setting tolerances specified in a maintenance procedure should also be checked for consistency with the "as-left" tolerances in the setpoint determination calculation. Also, the methods of performance monitoring and the period between monitoring should agree with the assumptions in the setpoint calculations. In short, the operations and maintenance activities at the plant should be consistent with the basis and assumptions in the uncertainty/setpoint calculation.

Trip setpoint values usually require transformation from process parameters to voltage or current values. For example, an analog pressure transmitter loop may contain an electronic comparator whose trip setting is measured and set in milliamperes of current. This conversion or scaling process can typically be described as a simple linear equation that relates process variable units to measurement signal units. Thus, changes to trip setpoints may result in comparator setting changes. Also, any changes to the linear transfer equation (such as the calibrated span, zero suppression/elevation) may also result in a module setting change. In some cases, the scaling conversion may account for some effects that are variable during severe environment conditions. If so, care should be taken to account for the variance, preferably in the setpoint determination calculation. For example, a hydrostatic head may be considered constant in a scaling calculation but may be subject to an elevated temperature during a design-basis accident. In this case, an additional uncertainty term should describe changes from the normal operating condition.

In the continuing process of design allowance verification, personnel evaluating instrument performance should be cognizant of allowances used in the setpoint determination. Traditionally, the verification process has been directed toward module drift, which may include reference

accuracy, M&TE, temperature effects, etc. Observations of deteriorating performance should result in equipment repair or replacement or a setpoint change. The latter action requires interfacing with the group responsible for the setpoint determination and documentation.

The plant operations group should participate in the review of setpoint determinations to ensure that sufficient operational margins exist for operationally limiting setpoints. Inadequate margins may result in inadvertent (unnecessary) actuations of safety equipment during operational transients. Setpoint changes may also alter the accident sequence of events, which may require reanalysis, emergency procedure changes, or retraining. For plants with simulator facilities, it may be appropriate to install the setpoint change on the simulator to evaluate the effect on plant operation before the setpoint is installed in the plant.

Any modification that results in a technical specification setpoint change is typically processed through a plant licensing group or the equivalent liaison with the USNRC. A close relationship with that group is important to determine if a nonsetpoint change to the technical specifications or some other regulatory change affects the assumptions of a setpoint calculation. Similar relationships may exist for the interface with other governmental agencies; for example, those concerning environmental discharge limits.

There is also an interface with vendors. The interpretation of the results from vendor publications and reports should be consistent with the allowances of the appropriate setpoint determination calculation. Information concerning unexpected product performance should be discussed with vendor personnel in order to evaluate the impact on a plant's particular application. It is particularly important that recommended maintenance practices be clearly and formally communicated to the product user.

10 Documentation

Uncertainty analysis and setpoint determination documentation for safety-related instrument channels forms a part of a facility's overall design-basis documentation. As such, the analysis and final determination should be included under the facility's nuclear quality assurance and design control programs.

The actual form of the uncertainty analysis may vary from plant to plant, but the level of documentation required should not. Documented calculations for safety-related setpoints include the following information:

- a) Setpoint identification
- b) Function
- c) Analytical limit
- d) Plant operating conditions under which setpoint is required
- e) Design basis event conditions under which setpoint is required
- f) Instrument channel or channels for which setpoint must be calculated
- g) Portion of instrument channel required for setpoint
- h) Identification of all uncertainty terms that affect setpoint determination

- i) Assumptions used in conjunction with the uncertainty analysis
- j) Method of uncertainty calculation
- k) Trip setpoint and allowable value determination
- l) References

The uncertainty analysis should use plant design documents as the source of input. The design input should be included in the plant's design control process. Each source of design input should be clearly noted within the uncertainty analysis.

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P.O. Box 1331
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ISA

SAMA PMC 20.1 (For informational purposes only)

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P.O. Box 12277

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Appendix A: Glossary

The following terms have been used in this recommended practice to define types and sources of instrument channel uncertainties that should be considered in an uncertainty analysis. The numbers in parentheses refer to the specific sections of RP67.04, Part II, that discuss the term.

A/D:	analog to digital conversion accuracy (6.2.9, Appendix H)
AL:	analytical limit (3 and 7)
AV:	allowable value (3 and 7)
B:	biases (6.3)
B _{TD} :	total bias (6.3)
CE:	calibration effect. The calibration effect may be included to account for additional uncertainties allowed in the calibration of devices (6.2.6).
CT:	calibration temperature. The ambient temperature at which the device is calibrated (6.2.2).
CU:	channel uncertainty. The channel uncertainty is the total uncertainty for a channel at a designated point in the channel (6.3).
D/A:	digital to analog conversion accuracy (6.2.9, Appendix H)
DR:	drift (3, 6.2, 6.2.7, 6.3)
e:	uncertainty of module (6.3.2)
HE:	humidity effect. The humidity effect term accounts for uncertainties due to a change in ambient humidity from calibration to normal operating conditions or DBA humidity conditions (6.3).
HELB:	high energy line break (6.2.10)
HU:	level uncertainty (Appendix B)
IR:	insulation resistance degradation effect. The insulation resistance degradation effect accounts for biases imposed in a loop due to changes in signal cable, terminal block, containment penetration, etc., insulation resistance. This term is used only in determining instrument channel uncertainty under high-energy linebreak conditions (6.2.10, Appendix D).
IS:	current source (Appendix D)
LOCA:	loss of coolant accident
M&TE:	measurement and test equipment (6.2.6.1)
MTE:	measurement and test equipment effect. The measurement and test equipment term accounts for uncertainties in the equipment utilized for calibration of channel devices. The MTE term includes the effects from voltage meters, dead weight testers, decade boxes, etc. (6.2.6.1, 6.3).
NSSS:	Nuclear Steam Supply System

OP:	operating pressure. The normal process static pressure at which the device operates (6.2.3).
OT:	operating temperature. The maximum or minimum normal ambient temperature at which the device may operate (6.2.2).
OV:	operating voltage. The normal voltage of the power supply (6.2.8).
PE:	primary element accuracy. The primary element accuracy is the accuracy of a component, piece of equipment, or installation used as a primary element to obtain a given process measurement. This would include the accuracy of a flow nozzle and/or the accuracy achievable in a specific flowmetering run (6.3).
PL:	process-design limit
PM:	process measurement uncertainty. The process measurement uncertainty is the basis ability to accurately measure the parameter of concern. This term is not governed by the accuracy of the instrumentation but by variation in actual process conditions that influence the measurement. Process influences such as temperature stratification, density variation, pressure variations, etc., which cause the basic measurement to be inaccurate, would all be considered in the PM term (6.2.5, Appendices B and C).
PS:	power supply variation effect. The power supply variation effect is used to account for the potential effects or variations in the power supply for a module (6.2.8).
PT:	pressure transmitter (Appendix D)
PV:	pressure variation. The difference between the normal static pressure of the process and the static pressure at which the module is calibrated (6.2.3).
R:	resultant random uncertainty (6.1)
RA:	reference accuracy (3, 6.2.6.1)
RD:	reading error (6.2.6.1)
RE:	radiation effect. The radiation effect term would be used to account for uncertainties caused by either normal operating or DBE-induced radiation exposure (6.2.4, 6.3).
REQ:	equivalent resistance (Appendix D)
RP:	recommended practice
RT:	total resistance (Appendix D)
RTD:	resistance temperature detector
SE:	seismic/vibratory effects. The seismic/vibratory term would be used to account for any uncertainties associated with a safe shutdown or operating basis earthquake, physical equipment vibration-induced inaccuracies, etc. (6.3).
SMTE:	sensor measurement and test equipment effect is the effect of the measurement and test equipment on the accuracy of the calibration of the sensor. See also the definition of MTE (6.2.6.1).
SP:	static pressure effect. The static pressure effect would be included to account for potential transmitter or sensor effects due to process static pressure differences between calibration and normal operating conditions (6.2.3, 6.3).

SRSS:	square root of the sum of the squares (6.1, 6.2, Appendix J)
STD:	reference accuracy of the controlled standard
TDF:	turndown factor. The upper range limit divided by the calibrated span of the device (6.2.7).
TE:	temperature effect. The ambient temperature effect term would be used to account for uncertainties due to the change in ambient temperature from calibration to normal operating conditions or DBA ambient temperature effects (6.2.2, 6.2.4, 6.3).
TS:	trip setpoint (3 and 7)
URL:	upper range limit. The maximum allowable span of the device (6.2.7).
VS:	voltage source (Appendix D)
VV:	voltage variation. The variation between normal voltage of the power supply and the limits of voltages for the power supply (6.2.8).

Appendix B: Vessel/reference leg temperature effects on differential pressure transmitters used for level measurement

When differential pressure transmitters are used to measure liquid level in vessels, changes in density of the reference leg fluid, the vessel fluid, or both, it can cause uncertainties if the level measurement system is not automatically compensated for density changes. This occurs because differential pressure transmitters respond to hydrostatic (head) pressures, which are directly proportional to the height of the liquid column multiplied by the liquid density. Therefore, measurement uncertainty may be induced because, while the actual level in the vessel or reference leg remains constant, the liquid density changes as a function of pressure and temperature. This changes the pressure delivered to the differential pressure transmitter, which makes the indicated level appear different from the actual level. The transmitter cannot distinguish that the difference in pressure is caused by the density effect.

In level-measuring applications, two situations are frequently encountered. Although other situations are common, it is not practical to cover the details of all of them. Instead, the situations described herein encompass the basic theory and methodology that can be applied to the other situations. These are

- a) Type A: The level measuring system is calibrated for assumed normal operating conditions. No automatic vessel or reference leg density compensation is provided; and
- b) Type B: The level measuring system is automatically compensated for density variations of the fluid in the vessel, but no reference leg compensation is provided.

It is further assumed that the vessels are closed (non-vented) and contain a saturated mixture of steam and water; the reference leg is water-filled and saturated, and no temperature gradient exists along the length of the reference leg. Often the reference leg fluid is a compressed liquid, but, for the purpose of this discussion, it is assumed to be saturated. Use densities and specific volumes as appropriate (e.g., subcooled, superheated). For simplicity, vessel growth is not considered in this example.

Before deriving the uncertainty equations for the situations described above, a review of level measurement theory is presented. [Figure B-1](#) shows a closed vessel containing a saturated steam/water mixture along with the explanations of the symbols used. From [Figure B-1](#) the differential pressure supplied to the transmitter is obtained as follows:

$$dP = \text{Pressure (HI)} - \text{Pressure (LO)} \quad (\text{Eq. B.1})$$

Now,

$$\text{Pressure (HI)} = H_R(\text{SGR}) + \text{Static Pressure} \quad (\text{Eq. B.2})$$

$$\text{Pressure (LO)} = H_W(\text{SGW}) + H_S(\text{SGS}) + \text{Static Pressure} \quad (\text{Eq. B.3})$$

Substituting Equations B.2 and B.3 into B.1,

$$dP = H_R(\text{SGR}) - H_W(\text{SGW}) - H_S(\text{SGS}) \quad (\text{Eq. B.4})$$

Substituting $(H_R - H_W)$ for H_S in Equation B.4 yields

$$dP = H_R(\text{SGR}) - H_W(\text{SGW}) - (H_R - H_W)(\text{SGS}) \quad (\text{Eq. B.5})$$

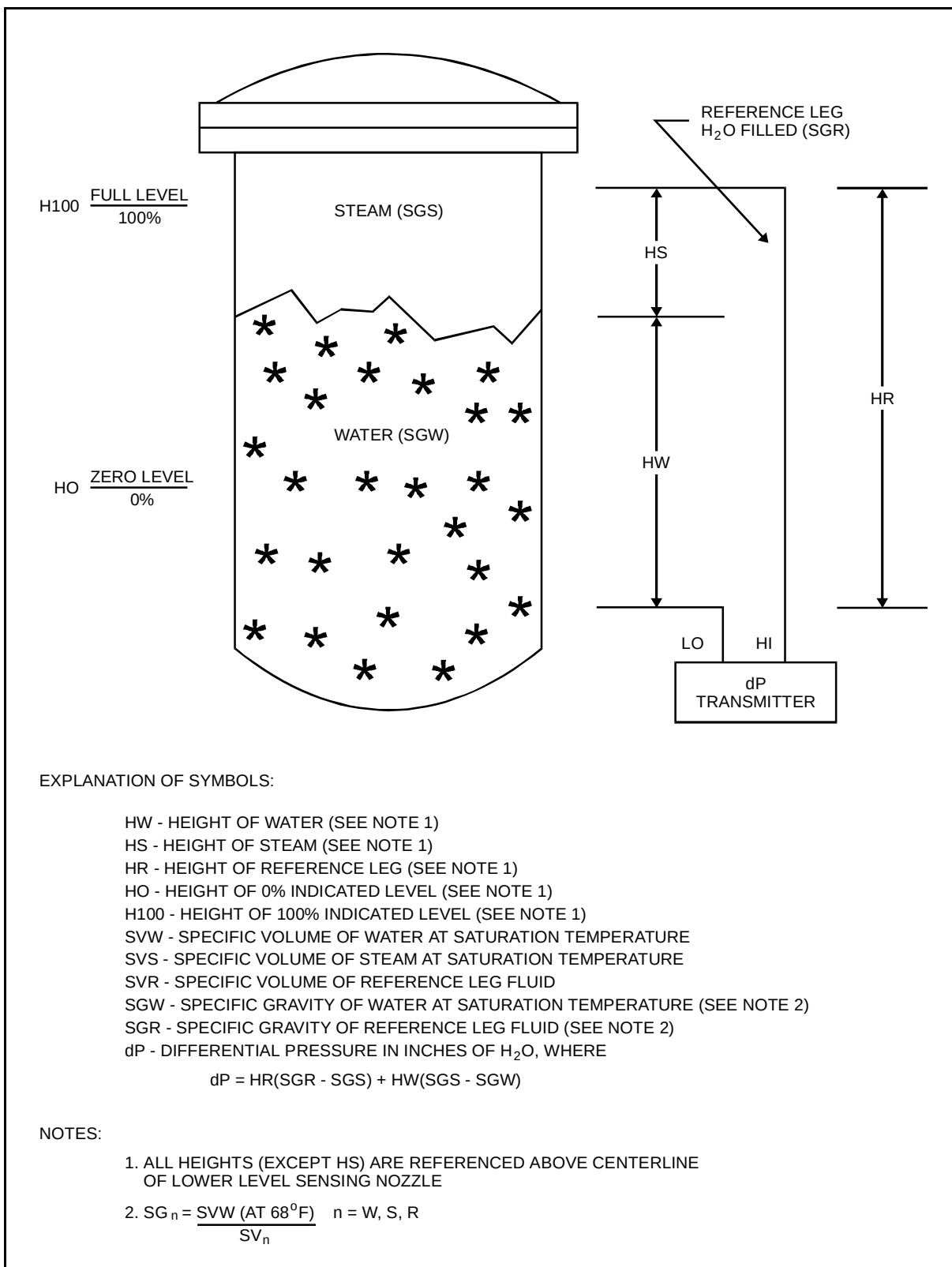


Figure B-1. Saturated liquid/vapor level measurement

or

$$dP = HR(SGR - SGS) + HW(SGS - SGW) \quad (\text{Eq. B.6})$$

Using Equation B.6 and substituting in for HW the height of water when at 0% of indicated scale (HO) and at 100% of indicated scale (H100), the differential pressures at 0% (dPO) and at 100% (dP100), respectively, can be determined. Note that HR, HW, HO, and H100 are normally stated in inches above the lower level sensing nozzle centerline. It is normally assumed that the fluid in both sensing lines below the lower level sensing nozzle are at the same density if they contain the same fluid and are at equal temperature. Because SGW, SGR, and SGS are unitless quantities, dP, dPO, and dP100 are normally stated in "inches of water" (in. H₂O) based on 68°F water. To calibrate the transmitter to read correctly, it is necessary to establish a base set of operating conditions in the vessel and reference leg from which SGW, SGR, and SGS can be determined using thermodynamic steam tables. After the specific gravity terms are defined, they can be plugged into Equation B.6 along with HR, HO, and H100, and the equation can be solved for dPO and dP100. These values of dP are then used to calibrate the transmitter (assuming in an ideal situation that the transmitter static pressure effect correction is neglected).

As long as the actual vessel and reference leg conditions (SGWA, SGSA, etc.,) remain the same as the base conditions for the Type A system, the indicated level is a linear function of the measured differential pressure, and no vessel/reference leg density effects are created. Therefore, the following proportionality can be written:

$$\frac{HW - HO}{H100 - HO} = \frac{dP - dPO}{dP100 - dPO} \quad (\text{Eq. B.7})$$

Solving for HW yields

$$HW = \frac{(H100 - HO)(dP - dPO)}{dP100 - dPO} + HO \quad (\text{Eq. B.8})$$

To assess the effects of varying vessel/reference leg conditions, assume an erroneous differential pressure, dPU, and erroneous water level, HU, are generated due to an off-base operating condition. Equation B.8 can then be rewritten as

$$HW \pm HU = \frac{(H100 - HO)\{(dP \pm dPU) - dPO\}}{dP100 - dPO} + HO \quad (\text{Eq. B.9})$$

Substituting Equation B.8 into Equation B.9 and solving for HU yields

$$HU = \frac{(H100 - HO)(dPU)}{dP100 - dPO} \quad (\text{Eq. B.10})$$

The denominator of Equation B.10 can be rewritten using Equation B.6 as

$$\begin{aligned} dP100 - dPO &= [HR(SGR - SGS) + H100(SGS - SGW)] - [HR(SGR - SGS) + HO(SGS - SGW)] \\ &= (H100 - HO)(SGS - SGW) \end{aligned} \quad (\text{Eq. B.11})$$

Equation B.11 can be substituted into Equation B.10 yielding

$$HU = \frac{dPU}{SGS - SGW} \quad (\text{Eq. B.12})$$

The numerator of Equation B.12 is simply the difference in the differential pressure measured at the actual conditions (dPA), less the differential pressure measured at the base condition (dPB), or

$$dPU = dPA - dPB \quad (\text{Eq. B.13})$$

Using Equation B.6 and assuming HR and HW are constant, we can substitute

$$dPA = HR(SGRA - SGSA) + HW(SGSA - SGWA) \quad (\text{Eq. B.14})$$

and

$$dPB = HR(SGRB - SGSB) + HW(SGSB - SGWB) \quad (\text{Eq. B.15})$$

into Equation B.13, yielding

$$dPU = HR(SGRA - SGSA - SGRB + SGSB) + HW(SGSA - SGWA - SGSB + SGWB) \quad (\text{Eq. B.16})$$

The denominator in Equation B.12 is equivalent to (SGSB - SGWB). Substituting this and Equation B.16 into Equation B.12 yields

$$HU = \frac{HR(SGRA - SGSA - SGRB + SGSB) + HW(SGSA - SGWA - SGSB + SGWB)}{(SGSB - SGWB)} \quad (\text{Eq. B.17})$$

Equation B.17 defines the uncertainty induced by changes in liquid density in the vessel, reference leg, or both for Type A situations. For Type B situations, SGSA = SGSB and SGWA = SGWB as the vessel conditions are automatically compensated. In other words, a Type B system measures the temperature of the vessel fluid and effectively modifies the base calibration point of the transmitter to be equivalent to the measured or actual temperature. Therefore, reference leg density effects must be determined, but the vessel density effects are eliminated. Typically, the signal compensation is done with a network of function generators and signal multipliers programmed with correction factors, based on density, that multiply the correction factor times the dP input from the level transmitter to get the true level. As equipment uncertainties may be present in the compensation circuitry, which may effectively multiply the dP as well, it is necessary to calculate the reference leg heatup effect in terms of dP, using Equation B.16, and plug dPU in the channel uncertainty equation in a similar fashion as a dP equipment uncertainty (see 6.3.3). Therefore, the reference leg bias in the Type B system is derived from Equation B.16 and reduces to

$$dPU = HR(SGRA - SGRB) \quad (\text{Eq. B.18})$$

By using the propagation techniques described in [6.3.3](#) and [Appendix K](#) for the modules that perform the compensation algorithm, this error is automatically converted from dP to units of level.

Equation B.18 shows that dP uncertainty becomes increasingly negative as the actual temperature increases above the base temperature. This is expected due to the way dPU is defined and the fact that the hydrostatic pressure contributed by the reference leg decreases with increasing temperature. The dP magnitude decreases as vessel level rises. Thus, dPU will cause a positive level uncertainty. It is also worth noting that the module errors associated with the compensation circuits normally are very small. Therefore, the approximate magnitude of the reference leg density effect can be estimated by

$$HU = \frac{HR(SGRA - SGRB)}{SGSB - SGWB} \quad (\text{Eq. B.19})$$

This equation was developed from Equation B.17 letting $SGSA = SGSB$ and $SGWA = SGWB$. Although the Type B system eliminates the process density effects, one should be cautioned that other uncertainties will be present in the density compensation modules, sensor, and signal transmission portions of the system. The net effect is that the dP signal will be compensated for conditions not exactly equal to the actual process conditions. Therefore, the propagation techniques discussed in 6.3.3 and Appendix K should be used to ensure conservative uncertainty allowances.

As previously discussed, the Type B system compensation equipment effectively "adjusts" the base calibration conditions to match the actual vessel conditions. Therefore, when using Equation B.19 the level error, HU, is determined at the vessel condition of interest by plugging in the specific gravity steam and specific gravity water values for that condition, not the base condition for which the transmitter is calibrated.

If the high pressure (HI) side of the transmitter had been connected to the lower nozzle and the low pressure (LO) side had been connected to the upper nozzle, it can be shown by similar derivation that Equations B.17 and B.19 still apply. Equation B.18 becomes

$$dPU = HR(SGRB - SGRA) \quad (\text{Eq. B.20})$$

Because the denominator term in Equations B.17 and B.19 decreases with increasing temperature, it is evident that the effect increases with rising vessel temperature. Furthermore, examination of the numerator of Equation B.17 reveals that the effect is maximized when HW is equal to H100. Examination of Equation B.19 reveals that an increasing reference leg temperature above the base conditions results in an increasing positive effect, assuming vessel conditions remain constant.

The equations above calculate uncertainties in actual engineering units. If it is desired to work in percent span, the quantities HU and dPU can be converted to percent span by dividing each by $(H100 - HO)$ or $(dP100 - dPO)$, respectively, and multiplying the results by 100 percent. As previously discussed, the sign of dPU must be considered based on which way the high and low pressure sides of the dP transmitter are connected to the vessel.

Assume, for example, that a Type A system configured as shown in Figure B-1 has the following conditions:

- a) $HR = 150$ inches
- b) $HO = 50$ inches
- c) $H100 = 150$ inches
- d) $HW = 100$ inches
- e) Base conditions: Vessel = 532°F (saturated water)
Reference leg = 68°F (saturated water)
- f) Actual conditions: Vessel = 500°F (saturated water)
Reference leg = 300°F (saturated water)

It is desired to determine HU using Equation B.17.

First, the specific gravity terms are found using the specific volumes of water (SVW) and specific volumes of steam (SVS) from the thermodynamic steam tables. The following values are determined:

$$SGWA = \frac{SVW(68^{\circ}F)}{SVW(500^{\circ}F)} = \frac{0.016046 \text{ ft}^3/\text{lbm}}{0.02043 \text{ ft}^3/\text{lbm}} \quad (\text{Eq. B.21})$$

$$= 0.78541$$

$$SGSA = \frac{SVW(68^{\circ}F)}{SVS(500^{\circ}F)} = \frac{0.016046 \text{ ft}^3/\text{lbm}}{0.67492 \text{ ft}^3/\text{lbm}} \quad (\text{Eq. B.22})$$

$$= 0.02377$$

$$SGRA = \frac{SVW(68^{\circ}F)}{SVW(300^{\circ}F)} = \frac{0.016046 \text{ ft}^3/\text{lbm}}{0.01745 \text{ ft}^3/\text{lbm}} \quad (\text{Eq. B.23})$$

$$= 0.91954$$

$$SGWB = \frac{SVW(68^{\circ}F)}{SVW(532^{\circ}F)} = \frac{0.016046 \text{ ft}^3/\text{lbm}}{0.02123 \text{ ft}^3/\text{lbm}} \quad (\text{Eq. B.24})$$

$$= 0.75582$$

$$SGSB = \frac{SVW(68^{\circ}F)}{SVS(532^{\circ}F)} = \frac{0.016046 \text{ ft}^3/\text{lbm}}{0.50070 \text{ ft}^3/\text{lbm}} \quad (\text{Eq. B.25})$$

$$= 0.03205$$

$$SGRB = \frac{SVW(68^{\circ}F)}{SVW(68^{\circ}F)} = \frac{0.016046 \text{ ft}^3/\text{lbm}}{0.016046 \text{ ft}^3/\text{lbm}} \quad (\text{Eq. B.26})$$

$$= 1.0$$

Next we substitute $HW = 100$ inches, $HR = 150$ inches, and quantities from Equations B.21 through B.26 above into Equation B.17 and solve for HU ; thus

$$HU = \frac{HR(SGRA - SGSA - SGRB + SGSB) + HW(SGSA - SGWA - SGSB + SGWB)}{(SGSB - SGWB)}$$

$$= \frac{150(0.91954 - 0.02377 - 1.0 + 0.03205)}{0.03205 - 0.75582} + \frac{100(0.02377 - 0.78541 - 0.03205 + 0.75582)}{0.03205 - 0.75582}$$

$$= +20.2 \text{ inches} \quad (\text{Eq. B.27})$$

In percent of indicated span,

$$HU(\%) = \frac{HU}{H_{100} - H_O} \times 100\%$$

$$= \frac{20.2}{150 - 50} \times 100\%$$

$$= +20.2\% \text{ span}$$

(Eq. B.28)

The preceding examples are typical for PWR steam generator level measurement. For BWR vessel level measurement, it is not uncommon for the reference and variable legs to traverse several temperature zones, and the assumption that the reference leg and variable leg see the same temperature below the variable leg tap may not be valid. In these cases, the principles described in the examples are the same, but the equations become more complicated.

Appendix C: Effects on flow measurement accuracy

C.1 General flow measurement uncertainty

A detailed review of flow measurement is beyond the scope of this document; however, some topics warrant discussion. ASME MFC-3M, plus H.S. Bean and R.W. Miller References address how to combine the different flow measurement uncertainties using the appropriate weighing factors that indicate the impact of each uncertainty on the overall flow measurement uncertainty equation. These uncertainties include density effects, bore tolerances, pipe diameters, thermal expansion of the pipe and/or orifice, and coefficient uncertainty among other contributors. For calibrated installations, density changes may be the only significant source of uncertainty that needs to be addressed in addition to accuracy. Examples of accepted treatment of some of these uncertainties follow.

C.2 Varying fluid density effects on flow orifice accuracy

In many nuclear plant applications, process liquid and gas flows are measured using orifice plates and differential pressure transmitters. The measurement of concern is either the volumetric flow rate or the mass flow rate. Many reference books and standards have been written using a wide variety of terminology to describe the mathematics of flow measurement, but in basic, simplified form the governing equations are

$$Q = K * (dP/Density)^{1/2} \quad (Eq. C.1)$$

and

$$W = K * (dP * Density)^{1/2} \quad (Eq. C.2)$$

where

Q = volumetric flow rate;

W = mass flow rate;

dP = differential pressure measured across the orifice;

Density = density of the fluid;

K = constant related to the beta ratio, units of measurement, and various correction factors.

As shown in Equations C.1 and C.2, the density of the fluid has a direct influence on the flow rate. Normally, a particular flow metering installation is calibrated or sized for an assumed normal operating density condition. As long as the actual flowing conditions match the assumed density, related process errors should not be created. However, some systems, such as safety injection, perform dual roles in plant operation. During normal operation these systems can be aligned to inject makeup to the reactor coolant system from sources of relatively low-temperature water. During the recirculation phase of a LOCA, the pump suction is shifted to the containment sump, which contains water at much higher temperatures.

If the flow measuring system has been calibrated for the normal low-temperature condition, significant process uncertainties can be induced under accident conditions, when the higher temperature water (lower density) is flowing. Of course, the flow measurement could be automatically compensated for density variations, but this is not the usual practice except on systems such as feedwater, steam, or reactor coolant flow.

To examine the effects of changing fluid density conditions, a liquid flow process shall be discussed. Examining Equation C.1, it is observed for all practical purposes that K is a constant. Actually, temperature affects K due to thermal expansion of the orifice, but this is assumed to be constant for this discussion to quantify the effects of density alone. If the volumetric flow rate, Q, is held constant, it is seen that a decrease in density will cause a decrease in differential pressure (dP), which causes an uncertainty. This occurs because the differential pressure transmitter has been calibrated for a particular differential pressure that corresponds to that flow rate. The lower dP causes the transmitter to indicate a lower flow rate.

Assuming Q remains constant between a base condition (Density 1, that for which the instrument is calibrated) and an actual condition (Density 2), an equality can be written between the base flow rate (Q1) and actual flow rate (Q2) as shown below.

$$Q^2 = Q^1 \quad (\text{Eq. C.3})$$

or

$$K * (dP^2/\text{Density } 2)^{1/2} = K * (dP^1/\text{Density } 1)^{1/2} \quad (\text{Eq. C.4})$$

or

$$dP^2/\text{Density } 2 = dP^1/\text{Density } 1 \quad (\text{Eq. C.5})$$

$$\frac{dP^2}{dP^1} = \frac{\text{Density } 2}{\text{Density } 1} \quad (\text{Eq. C.6})$$

Because density is the reciprocal of specific volume of fluid (SVF), Equation C.6 may be rewritten as

$$\frac{dP^2}{dP^1} = \frac{\text{SVF}^1}{\text{SVF}^2} \quad (\text{Eq. C.7})$$

This equation shows that for an increasing temperature from condition 1 to condition 2, the differential pressure decreases. Therefore, the uncertainty, dP^U , is equal to

$$dP^U = dP^2 - dP^1 \quad (\text{Eq. C.8})$$

Rewriting dP^2 from Equation C.7 as

$$dP^2 = dP^1 (\text{SVF}^1/\text{SVF}^2) \quad (\text{Eq. C.9})$$

and substituting in Equation C.8 yields

$$dP^U = dP^1 [(\text{SVF}^1/\text{SVF}^2) - 1] \quad (\text{Eq. C.10})$$

It is observed in Equation C.10, which is the equation for density effect on volumetric flow, that the absolute effect is maximized when dP^1 is maximized. This occurs at the upper end of the calibrated differential pressure span for which the transmitter is calibrated. This is also maximum

calibrated flow. The effect varies from negative values for temperatures above the base value ($SVF^2 > SVF^1$) to zero for temperatures equal to the base value ($SVF^2 = SVF^1$) and finally to positive values for temperatures below the base value ($SVF^2 < SVF^1$). For mass flow, the equation can be derived in a similar fashion. Note that this method derives the differential pressure error, which can be converted to a flow rate error using the flow versus differential pressure relationship for the orifice.

As an example of the use of Equation C.10, assume an orifice plate is used to measure flow in a water system that is normally at 120°F. The orifice is sized to produce 100 inches of water at 100 gpm flow at 120°F. Assume further that under accident conditions the temperature rises to 300°F at an actual flow of 50 gpm. It is desired to find dP^U and the indicated flow.

The first step is to determine the relationship between Q and dP. Referring to Equation C.1 we reduce it to

$$Q = (\text{Constant})(dP)^{1/2} \quad (\text{Eq. C.11})$$

assuming K and Density are constants for the particular situation. Plugging $dP = 100$ and $Q = 100$ into Equation C.11 yields

$$100 = (\text{Constant})(100)^{1/2} \quad (\text{Eq. C.12})$$

or

$$\text{Constant} = \frac{100}{10} = 10 \quad (\text{Eq. C.13})$$

Thus,

$$Q = 10(dP)^{1/2} \quad (\text{Eq. C.14})$$

Therefore, using Equation C.14 at the accident flow rate of 50 gpm, we can solve for dP^1 as follows:

$$Q = 10(dP^1)^{1/2}$$

$$50 = 10(dP^1)^{1/2}$$

or

$$dP^1 = \frac{(50)^2}{(10)^2} = 25 \text{ inches of water} \quad (\text{Eq. C.15})$$

Using thermodynamic steam tables, assuming saturation conditions,

$$SVF^1 (\text{at } 120^\circ\text{F}) = 0.016204 \text{ ft}^3/\text{lbm} \quad (\text{Eq. C.16})$$

$$SVF^2 (\text{at } 300^\circ\text{F}) = 0.01745 \text{ ft}^3/\text{lbm} \quad (\text{Eq. C.17})$$

Substituting Equations C.15, C.16, and C.17 into Equation C.10 yields

$$\begin{aligned} dP^U &= 25 [(0.016204/0.01745) - 1] \\ &= -1.8 \text{ inches of water} \end{aligned} \quad (\text{Eq. C.18})$$

This can be converted to percent span, of course, by dividing dP^U by the calibrated dP span and multiplying the result by 100%.

Therefore, the rise in temperature reduces the actual differential pressure input to the transmitter to $25 - 1.8 = 23.2$ inches of water. Substituting this value for dP into Equation C.14 yields an indicated flow of

$$Q = 10(23.2)^{1/2} = 48.2 \text{ gpm} \quad (\text{Eq. C.19})$$

C.3 Effects of piping configuration on flow accuracy

Bends, fittings, and valves in piping systems cause flow turbulence. This can cause process measurement uncertainties to be induced in flow elements. ASME has published guidance for various types of installation examples to show the minimum acceptable upstream/downstream lengths of straight pipe before and after flow elements. Following this ASME guidance helps reduce the effect of this turbulence. The piping arrangement showing locations of valves, bends, fittings, etc., can usually be obtained from piping isometric drawings. ASME MFC-3M states that, if the minimum upstream and downstream straight-pipe lengths are met, the resultant flow measurement uncertainty for the piping configuration (not including channel equipment uncertainty) should be assumed to be 0.5% of the discharge coefficient. If the minimum criteria cannot be met, additional uncertainty (at least 0.5%, per H.S. Bean Reference) should be assumed for conservatism based on an evaluation of the piping configuration and field measurement data, if available.

Appendix D: Insulation resistance effects

D.1 Theory

Under conditions of high humidity and temperature associated with high energy line breaks (HELB), cables, splices, connectors, terminal blocks, and penetrations may experience a reduction in insulation resistance (IR). The reduction in IR causes an increase in leakage currents between conductors and from individual conductors to ground. Leakage currents are negligibly small under normal, nonaccident conditions. If channel calibrations are made, such currents are essentially calibrated out. However, under HELB events the leakage currents may increase, causing an uncertainty in measurement. The effect can be a concern for circuits with sensitive, low level signals such as current transmitters, RTDs, thermocouples, etc. It is especially of concern for channels with logarithmic signals (excore detectors, radiation monitors). For further details see NUREG/CR-3691.

The components of the instrument signal transmission system (cable, splices, connectors, etc.) are all constructed of insulating materials between electrical conductors. These insulators normally are characterized by a low conductivity due to low concentration and low mobility of ions. However, under elevated temperature and humidity conditions, the ionic mobility increases, which leads to increased leakage current. The relationship between conductivity and temperature for the insulator is given as

$$C = CO * e^{(-B/T)} \quad (\text{Eq. D.1})$$

where

C = the ionic conductivity in ohms;

T = the temperature in degrees Kelvin (°K);

CO & B = constants.

It is observed in Equation D.1 that the conductivity increases exponentially with increasing temperature. As insulation resistance is the reciprocal of conductivity, IR decreases with increasing temperature. The rise in moisture also increases the surface conductivity effects, particularly with respect to exposed conductor surfaces such as in terminal blocks.

There also are instrument channels where lead wire resistance may be a contributor to the total channel uncertainty, such as thermocouples or RTD instrument channels. However, this appendix addresses only IR effects.

D.2 Sources of IR data

Insulation resistance measurements are normally taken before, during, and after the LOCA simulation phase of a qualification test. Normally, the IR data during the LOCA simulation is the data of interest. Therefore, the IR data usually will be published within the qualification test report. LOCA simulation tests may report cable IR based on IR or leakage current tests conducted on various cable types (e.g., shielded, unshielded, 2/c, 7/c, etc.) and measurement configurations (e.g., conductor-to-conductor, conductor-to-shield, multiple conductor-to-conductor/shield, etc.). The cable IR values extracted from the simulation tests for use in channel

uncertainty calculations should bound those expected for the particular channel's application. If necessary, calculations can be performed, using the test configuration measured IR values, to obtain IR values for the channel cable configuration.

Usually the qualification test gives data for cable samples longer than 1 foot. This is because practical considerations normally require lengths longer than 1 foot for qualification testing due to the size of the environmental chamber, mandrel size, etc. When calculating IR it is necessary to determine an "ohms-foot" value for IR such that total resistance, R_T , for actual installed cable lengths that vary in length can be easily calculated. As an example, assume a cable test sample 25 feet in length exhibited a tested conductor-to-conductor resistance of 1.0×10^6 ohms. The 25-foot sample may be considered to be the lumped parallel resistance combination of 25 one-foot samples or

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_{25}} \quad (\text{Eq. D.2})$$

where $R_1 = R_2 = \dots = R_{25}$, each resistance equal to the resistance (R) of a 1-foot sample. Thus, Equation D.2 becomes

$$\frac{1}{R_T} = \frac{25}{R} \quad (\text{Eq. D.3})$$

$$R = 25(R_T) \quad (\text{Eq. D.4})$$

Thus, the individual 1-foot resistance is equal to $R = 25 \times (1.0 \times 10^6)$ or 2.5×10^7 ohms - ft.

Typically, qualification tests use a bounding temperature profile so that the report will be applicable to as many plants as possible, each with different peak accident temperatures. It is conservative but not always practical to use the IR values measured at the peak tested temperature. It is acceptable to extrapolate or use actual tested IR values at lower temperatures that more closely bound or equal the user's peak temperature. However, as discussed earlier in 6.2.4 and 6.2.11, caution must be applied when extrapolating test data.

D.3 IR effect example: Current source channel

A great majority of pressure, flow, level, etc., sensors used in the nuclear industry act essentially like ideal or constant current sources; that is, for a given process input, their output remains at a constant current value, insensitive to loop resistance within a specified range. [Figures D-1\(a\) and D-1\(b\)](#) show a typical pressure transmitter (PT) and signal transmission system (blocks 1-5) to an indicator. The signal transmission components are in a harsh environment and, therefore, are subject to IR degradation during an accident. The system is shielded up to component 2. However, the shield drain wire is included but not terminated to anything in the splice. The shield is single-point grounded outside containment. The connector and penetration case are grounded.

An equivalent circuit schematic showing IR leakage paths and currents is shown in [Figure D-1\(c\)](#). Note that R_{11} , R_{21} , R_{31} , etc., are the conductor-to-conductor IR values. Also, R_{12} , R_{13} , R_{22} , R_{23} , R_{32} , R_{33} , etc., are the conductor-to-shield values. The pressure transmitter is represented by current source, I_S . The power supply is equivalent to voltage source, V_S , and the indicator is equivalent to the load resistor, R_L . Note that although the loop shown in [Figure D-1\(b\)](#) is ungrounded, an air leakage path, R_{AIR} , is shown to provide a return path for leakage currents I_{12} , I_{13} , I_{22} , I_{23} , I_{32} , I_{33} , etc.

Referring to [Figure D-1\(c\)](#) and [D-1\(d\)](#) the following equalities can be written:

$$\frac{1}{REQ1} = \frac{1}{R11} + \frac{1}{R21} + \frac{1}{R31} + \frac{1}{R41} + \frac{1}{R51} \quad (\text{Eq. D.5})$$

$$\frac{1}{REQ2} = \frac{1}{R12} + \frac{1}{R22} + \frac{1}{R32} + \frac{1}{R42} + \frac{1}{R52} \quad (\text{Eq. D.6})$$

$$\frac{1}{REQ3} = \frac{1}{R13} + \frac{1}{R23} + \frac{1}{R33} + \frac{1}{R43} + \frac{1}{R53} \quad (\text{Eq. D.7})$$

These equations can be solved for REQ1, REQ2, and REQ3 and substituted into [Figure D-1\(d\)](#) for analysis. If we assume RAIR is several orders of magnitude larger than REQ2 and REQ3, the circuit further simplifies to that shown in [Figure D-1\(e\)](#). This means

$$\frac{1}{REQ} = \frac{1}{REQ1} + \frac{1}{REQ2 + REQ3} \quad (\text{Eq. D.8})$$

Thus Equation D.8 can be solved for RE. This leakage path gives rise to leakage current IE, which is also the error current. Under ideal conditions with no leakage due to IR degradation, the transmitter current (IS) and load current (IL) would be equivalent. As shown in [Figure D-1\(e\)](#); however, IL and IS differ by the error current, IE.

Summing voltages in a clockwise fashion around the right-hand loop of the circuit, the following equality can be written

$$VS = IE(REQ) + IL(RL) \quad (\text{Eq. D.9})$$

Solving for IE,

$$IE = \frac{VS - IL(RL)}{REQ} \quad (\text{Eq. D.10})$$

At node 1 of [Figure D-1\(c\)](#),

$$IL = IE + IS \quad (\text{Eq. D.11})$$

Substituting Equation D.11 into Equation D.10 yields

$$IE = \frac{VS - (IE + IS)(RL)}{REQ} \quad (\text{Eq. D.12})$$

Rearranging Equation D.12,

$$IE(REQ) = VS - IE(RL) - IS(RL) \quad (\text{Eq. D.13})$$

$$IE(REQ + RL) = VS - IS(RL) \quad (\text{Eq. D.14})$$

$$IE = \frac{VS - IS(RL)}{REQ + RL} \quad (\text{Eq. D.15})$$

Using Equations D.5, D.6, D.7, D.8, and D.15, the error current I_E can be determined for a given transmitter output current (Equation D.15). Examination of Equation D.15 reveals the following facts:

- a) The IR effect for a current loop is a positive bias with respect to current.
- b) The larger the V_S , the larger the IR error.
- c) The smaller the I_S , the larger the IR error.
- d) The smaller the R_L , the larger the IR error.
- e) The smaller the R_E , the larger the IR error.

The error in percent span can be determined by

$$I_E(\%) = \frac{I_E}{I_{S_{MAX}} - I_{S_{MIN}}} \times 100\% \quad (\text{Eq. D.16})$$

Note that the resistance paths shown apply to a typical configuration. More or less leakage paths may be present in a particular situation. As an example, assume the circuit shown in [Figure D-1\(b\) and D-1\(c\)](#) has the following values:

$$R_{11} = R_{21} = R_{41} = 5.0 \times 10^6 \text{ ohms} \quad (\text{Eq. D.17})$$

Cable length = 300 ft (sample tested was 25 ft in length with measured conductor-to-conductor resistance = 1.0×10^7 ohms and conductor-to-shield resistance = 0.5×10^7 ohms).

$$R_{51} = R_{52} = R_{53} = 1.0 \times 10^6 \text{ ohms} \quad (\text{Eq. D.18})$$

$$R_{12} = R_{13} = R_{22} = R_{23} = R_{42} = R_{43} = 2.5 \times 10^6 \text{ ohms} \quad (\text{Eq. D.19})$$

$$I_S = 12.0 \text{ mA} \quad (\text{Eq. D.20})$$

$$I_{S_{MAX}} = 20.0 \text{ mA} \quad (\text{Eq. D.21})$$

$$I_{S_{MIN}} = 4.0 \text{ mA} \quad (\text{Eq. D.22})$$

$$V_S = 30 \text{ V dc} \quad (\text{Eq. D.23})$$

$$R_L = 250 \text{ ohms} \quad (\text{Eq. D.24})$$

Using the measured conductor-to-conductor resistance = 1.0×10^7 ohms for a 25-foot sample of cable, the "ohms-foot" value of R_{31} is determined by

$$R = 25(1.0 \times 10^7) = 2.5 \times 10^8 \text{ ohms} \cdot \text{ft} \quad (\text{Eq. D.25})$$

Thus

$$R_{31} = \frac{2.5 \times 10^8 \text{ ohms} \cdot \text{ft}}{300 \text{ ft}}$$

$$R_{31} = 8.33 \times 10^5 \text{ ohms} \quad (\text{Eq. D.26})$$

Similarly

$$R_{32} = R_{33} = \frac{(25 \text{ ft})(0.5 \times 10^7 \text{ ohms})}{300 \text{ ft}}$$

$$R_{32} = R_{33} = 4.17 \times 10^5 \text{ ohms} \quad (\text{Eq. D.27})$$

Using Equations D.5, D.6, D.7, and D.8,

$$\frac{1}{REQ1} = \frac{1}{5.0 \times 10^6} + \frac{1}{5.0 \times 10^6} + \frac{1}{8.33 \times 10^5} + \frac{1}{5.0 \times 10^6} + \frac{1}{1.0 \times 10^6}$$

$$REQ1 = 3.57 \times 10^5 \text{ ohms} \quad (\text{Eq. D.28})$$

$$\frac{1}{REQ2} = \frac{1}{2.5 \times 10^6} + \frac{1}{2.5 \times 10^6} + \frac{1}{4.17 \times 10^5} + \frac{1}{2.5 \times 10^6} + \frac{1}{1.0 \times 10^6}$$

$$REQ2 = REQ3 = 2.17 \times 10^5 \text{ ohms} \quad (\text{Eq. D.29})$$

$$\frac{1}{REQ} = \frac{1}{3.57 \times 10^5} + \frac{1}{2.17 \times 10^5 + 2.17 \times 10^5}$$

$$REQ = 1.96 \times 10^5 \text{ ohms} \quad (\text{Eq. D.30})$$

Thus, substituting Equations D.20, D.23, D.24, and D.30 into Equation D.15

$$IE = \frac{30 - 0.012(250)}{1.96 \times 10^5 + 250}$$

$$IE = 1.38 \times 10^{-4} \text{ A}$$

$$IE = 0.138 \text{ mA} \quad (\text{Eq. D.31})$$

$$IE(\%) = \frac{0.138}{20.0 - 4.0} \times 100\%$$

$$IE(\%) = + 0.86\% \text{ span} \quad (\text{Eq. D.32})$$

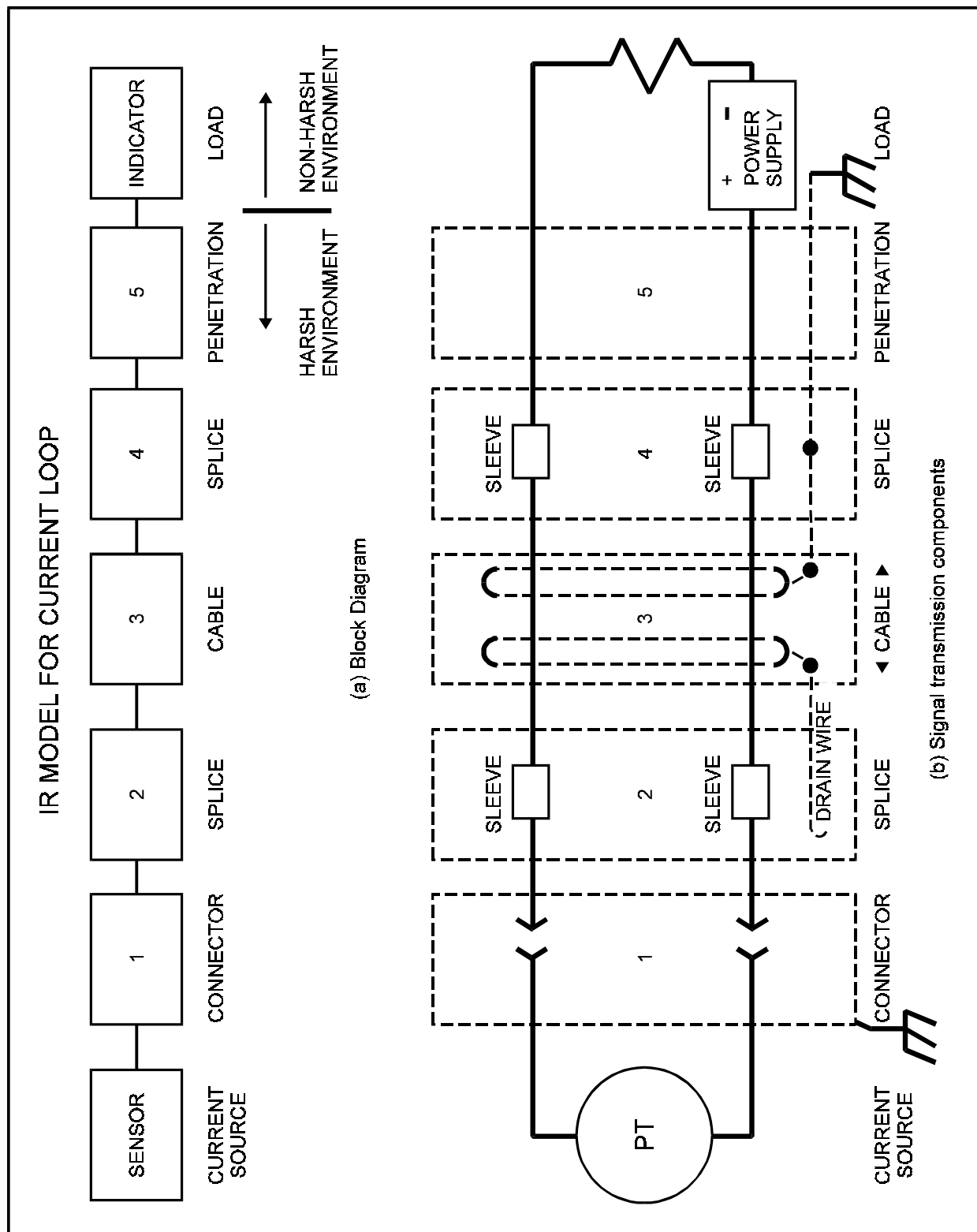


Figure D-1. IR model for current loop

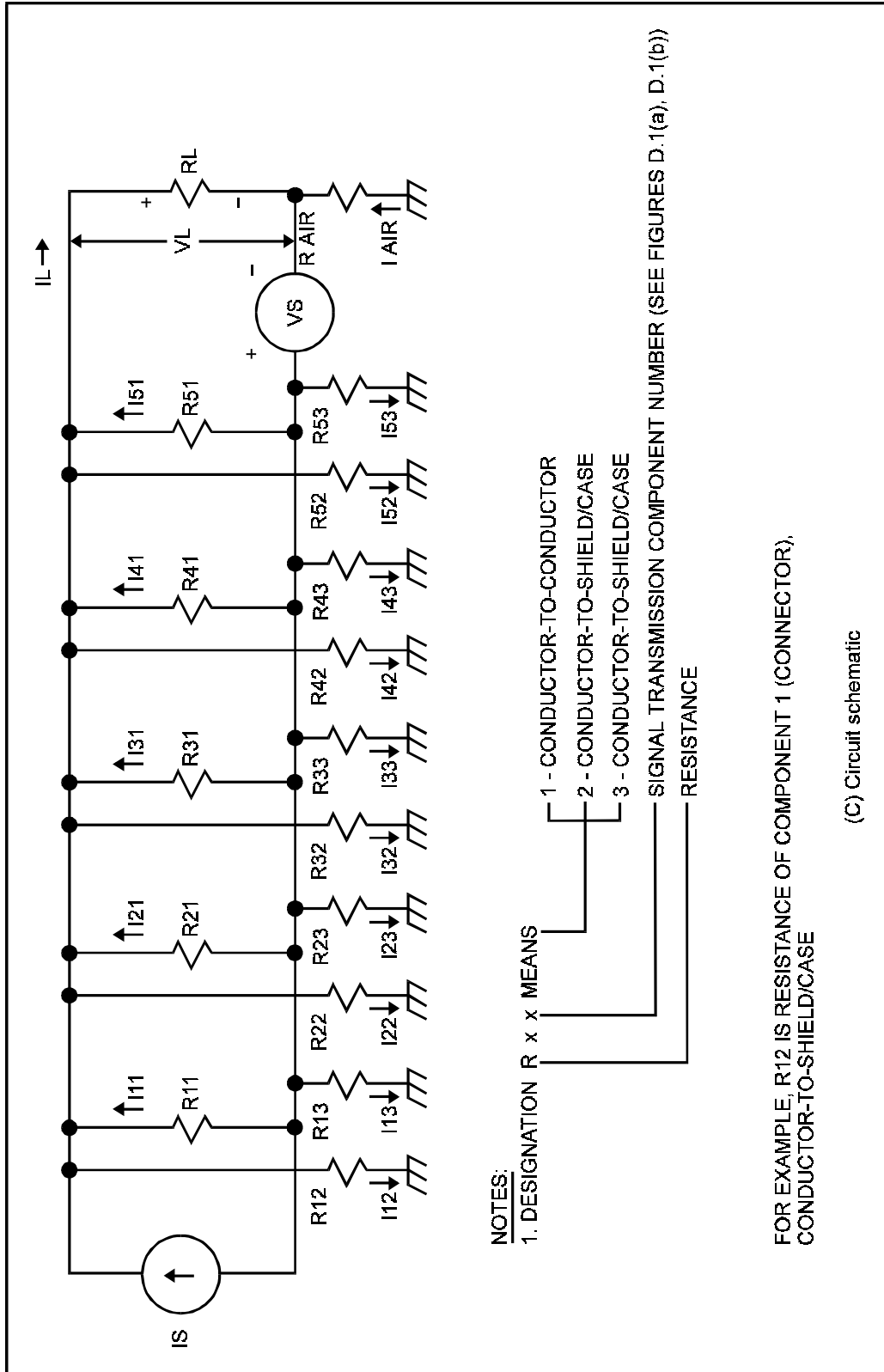


Figure D-1 (Cont'd). IR model for current loop

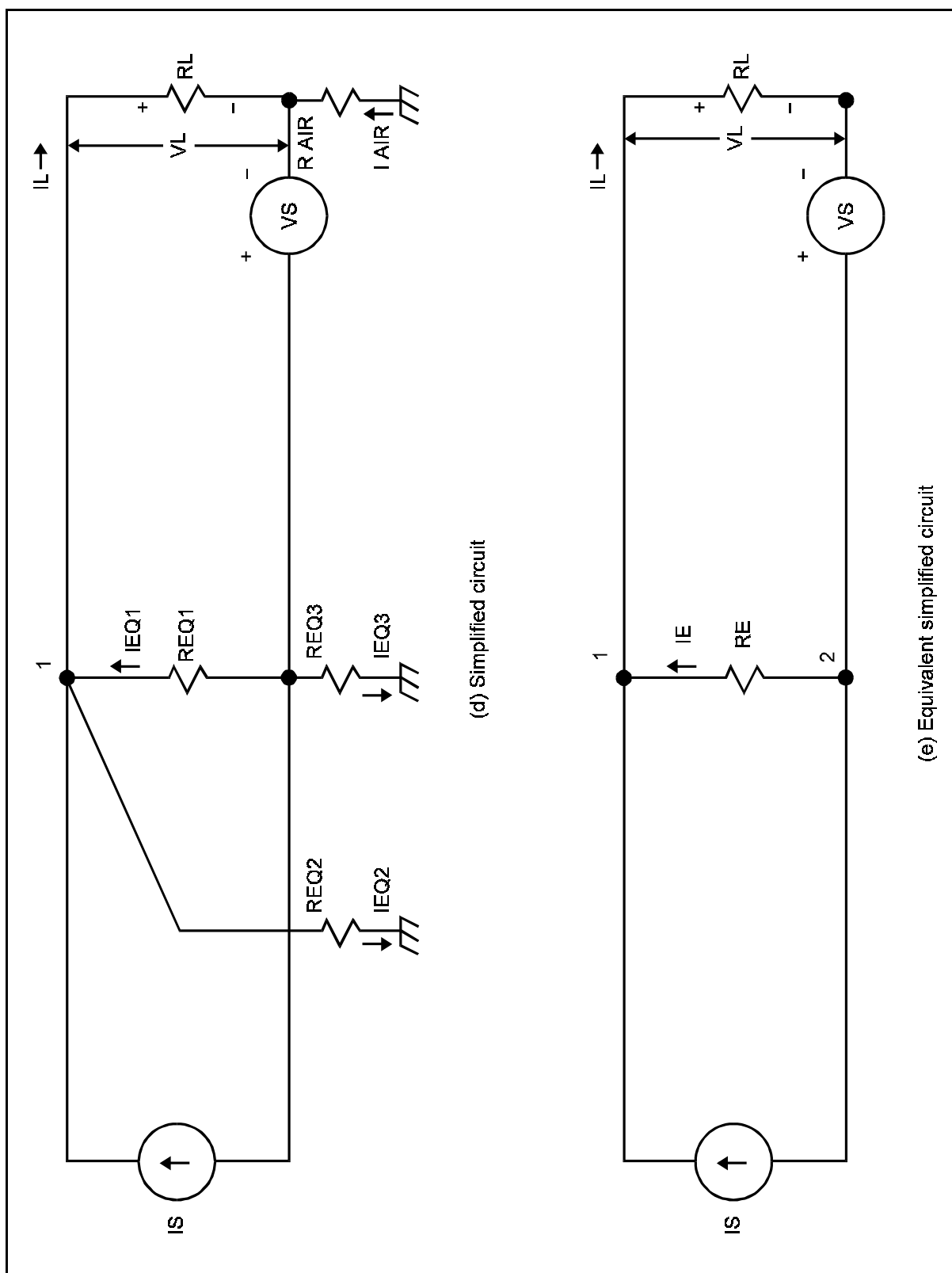


Figure D-1 (Cont'd). IR models for current loop

Appendix E: Plant specific as-found/as-left data

E.1 Overview

Instrument drift values for use in loop accuracy and setpoint calculations can be derived from manufacturer's specifications or from plant-specific calibration history, if available. Guidelines for determining the manufacturer's specification for drift and combining values for larger time intervals are provided in 6.2.7 of this recommended practice. This appendix provides guidelines for a data reduction methodology for plant specific as-found/as-left data to determine a value that can be used in this recommended practice. One approach is to substitute this value for the drift (DR) term in Equations 6.11a and 6.11b. Other approaches for the use of this value may be acceptable. The user is ultimately responsible for determining how to use the data.

It should be noted that the as-found/as-left data may include the combined effects of reference accuracy, inherent drift, measurement and test equipment, humidity, vibration, normal radiation, normal temperature, and power supply variations during the time period under surveillance. Additional terms may be included for a particular application as needed. A value for drift as obtained by this methodology is more conservative than the value of drift as defined in this recommended practice because it will include some or all of these other uncertainties.

E.2 Theory

For the purposes of this appendix, 95/95 values were chosen as the basis of the examples contained herein. 95/95 values will bound hardware performance with a 95% probability at a 95% confidence level. The probability value establishes the portion of the population that is included within the tolerance interval. This means that 95% of all past, present, and future values will be bounded by the 95/95 interval value.

The confidence level essentially establishes the repeatability of calculating a value that will fall within the estimated values. This means that, if the values were to be recalculated in the future, there is a 95% chance that the values would be bounded by the 95/95 interval values. Using 95/95 value means that we are 95% sure that 95% of all values will be less than the estimated values.

A statistical data base or spreadsheet package can be used instead of manual methods for large volumes of data. Statistical methods described in W.J. Beggs Reference provide guidelines for determining the maximum values for as-found/as-left data; the method described provides a 95/95 interval value for as-found/as-left data independent of the number of calibration intervals used in the determination.

Analysis of as-found/as-left data begins with establishing the scope of the analysis. Generally, this means identifying the types of equipment being used in the application of interest. Factors, such as process conditions, range, location, and environmental conditions, which may cause one device to behave differently from a duplicate, must be determined.

Once the scope has been established, the next step is to obtain the as-found and as-left calibration data. All as-found/as-left data available should be used to support the assumed distribution. This appendix describes two methods of analyzing as-found/as-left data. The first

method is based on the data being characterized as a normal distribution. The second method does not depend on any specific underlying distribution.

Generally, the data can be represented by a normal distribution. Verification of normality (utilizing more than 30 data points) should be performed, where possible. In order to avoid unnecessarily conservative values, when W.J. Beggs' Reference is used for determining K values, at least 8 data points are recommended.

For non-normal distribution, pass/fail criteria are established, and the resulting pass/fail data is analyzed assuming a binomial distribution. At least 100 data points are recommended to use this method. (See W.J. Beggs Reference.)

Once the calibration data has been recovered, the next step is to determine the changes over the interval of interest. All data should be converted to a common base (e.g., percent of span). The surveillance interval should be noted. The difference between the as-found data and previous as-left data should be determined. The data may be standardized to a common interval between readings by dividing the time interval between readings and then multiplying by a standardized time interval. This technique assumes a linear extrapolation of drift.

Once the as-found/as-left data are determined for individual devices, the data can be grouped by model and by groups with similar environmental conditions. When the groups have been established, the data can be analyzed. It is expected that most as-found/as-left data will be normally distributed. A method for analyzing this data for 95/95 interval values follows. If, in conducting this analysis, it is determined that the data is not normally distributed, an alternative is described for defining arbitrary pass/fail criteria to establish a binomial distribution.

E.3 Normal distribution of data

E.3.1 Treatment of outliers

An outlier is an observation that is significantly different from the rest of the sample. They usually result from mistakes or measuring device problems. To identify outliers, the T-Test described in W.J. Beggs' Reference can be used. The extreme studentized deviate is calculated as

$$T = \frac{|x_s - \bar{x}|}{s} \quad (\text{Eq. E.1})$$

where

T = the extreme studentized deviate;

x_s = the extreme observation;

$\bar{x}$ = the sample group mean;

s = the standard deviation of the sample group mean.

If T exceeds the critical value given in Table XVI of W.J. Beggs Reference at the 1% significance level; for example, the extreme observation is considered to be an outlier. Once the outlier is identified, it is removed from the data set. Removal of outliers should be done with care so as not to remove valid data points. Additional recommendation on the treatment of outliers is provided in ANSI/ASTM PTC 19.1, plus W.J. Beggs and K.V. Bury References.

E.3.2 Normality tests

Once the data has been edited and grouped, the Chi-Square Goodness of Fit Test can be used to assure that the underlying distribution can be represented by a normal distribution. (See

W.J. Beggs Reference.) This test assumes a normal distribution and, based on the sample mean and deviation, predicts the expected number of observations in each interval. The expected values are compared to the observed values. Since this test requires a rather large number of points, it should be applied only to groups with a large population of, say, 30 or more data points. See ANSI N15.15 and W.J. Beggs Reference.

E.3.3 Maximum expected value

A tolerance interval places bounds on the proportion of the sampled population contained within it. A 95/95 tolerance interval about the mean bounds 95% of the past, present, and future values. Determining the interval and adding it to the absolute value of the mean determines the maximum expected value.

The maximum values can be calculated as follows:

$$X_{MAX} = |\bar{x}| + Ks \quad (\text{Eq. E.2})$$

where

X_{MAX} = the maximum expected value;

$\bar{x}$ = the sample mean;

K = a value from W.J. Beggs Reference, Table VII(a), dependent on the sample size and confidence level;

s = the standard deviation of the sample.

E.4 Non-normal distribution of data

Methods are available for analyzing data when the underlying distribution cannot be demonstrated to be a normal distribution. Non-normal distributions can result when the value being measured is small with respect to the precision of the measurement.

E.4.1 Pass/fail criteria

To accommodate a non-normal distribution, arbitrary values for the data can be established that represent pass/fail criteria. The pass/fail criteria are established so that the data can be characterized by a binomial distribution and analyzed accordingly. The pass/fail criteria can be adjusted to obtain a 95/95 interval value.

E.4.2 Minimum pass probability

A binomial distribution is frequently used to characterize the probability that an item meets certain specifications. To analyze the data, a specification for each type of device is arbitrarily selected as a pass/fail criterion. The probability of the value falling outside this criterion can then be estimated by

$$P = x/n \quad (\text{Eq. E.3})$$

where

P = the probability of the value exceeding the pass/fail criterion;

x = the number of values outside the pass/fail criterion;

n = the number of data points.

Since P is an estimate of the probability that a data point will fall outside the pass/fail criterion, the confidence interval on this estimate must be determined. If n is sufficiently large (>100), a

confidence interval based on a normal distribution of the probabilities can be calculated as follows:

$$P_{u,1} = x/n \pm z\{(1/n)(x/n)[1 - (x/n)]\}^{1/2} \quad (\text{Eq. E.4})$$

where

$P_{u,1}$ = the minimum and maximum values of the probability that a data point will fall outside of the pass/fail criterion.

z = the standardized value from a normal distribution corresponding to the desired confidence level.

Once the maximum probability, at the desired confidence level, that a data point will fall outside the pass/fail criterion is determined, the minimum probability that a data point will fall within the pass/fail criterion can be determined by $(1 - P_u)$. This process is repeated until a pass/fail criterion is found, which results in the desired probability and confidence level that the data points will fall within the pass/fail criterion.

See W.J. Beggs Reference for the definition of statistical terms used within this appendix.

Appendix F: Line pressure loss/head pressure effects

The flow of liquids and gases through piping causes a drop in pressure from point A to point B (see Figure F-1) because of fluid friction. Many factors are involved including, for example, length and diameter of piping, fluid viscosity, and fluid velocity. If, for setpoint calculation purposes, the setpoint is based on pressure at a point in the system that is different from the point of measurement, the pressure drop effect between those points must be accounted for. The pressure drop effect should be calculated at flow conditions representative of conditions where protective action is required.

If, for example, protective action must be taken during an accident when the pressure at point A exceeds the analytical limit (AL = 2300 psig), the pressure switch setpoint needs to be adjusted to account for the line loss (30 psig) and channel equipment errors (10 psig). The sensing line head effect for the accident condition is assumed to be negligible.

$$\begin{aligned}\text{Setpoint} &= \text{AL} - (\text{Line loss}) - (\text{Total channel equipment uncertainty}) && (\text{Eq. F.1}) \\ &= 2300 - 30 - 10 \\ &= 2260 \text{ psig}\end{aligned}$$

Note that if the line loss had been neglected and the setpoint adjusted to the analytical limit minus equipment error (2290 psig), the resultant setpoint is nonconservative. In other words, when the trip occurred, the pressure at point A could be equal to $2290 + 30 = 2320$ psig, which nonconservatively exceeds the analytical limit. If the pipe had dropped down vertically to point B, the result would be a head effect plus line loss example. Assume that the head pressure exerted by the column of water in the vertical section of piping is 5 psig and the line loss from point A to B is still equal to 30 psig and the pressure at point A is not to drop below 1500 psig without trip action. The setpoint is then calculated by

$$\begin{aligned}\text{Setpoint} &= \text{AL} - (\text{Line loss}) + \text{Head} + (\text{Total channel equipment uncertainty}) && (\text{Eq. F.2}) \\ &= 1500 - 0 + 5 + 10 \\ &= 1515 \text{ psi}\end{aligned}$$

Line loss is neglected in Equation F.2 for conservatism. Since line loss is dependent on flow rate, it is conservative in this case to assume no flow and thus no line loss.

As treated here, the head effect/line loss terms are constant and handled as bias terms. Line loss/head pressure effects may already be accounted for in the calibration process and/or the safety analysis. If so, the setpoint adjustments shown above may not be necessary. Close review should be conducted to ensure appropriate treatment.

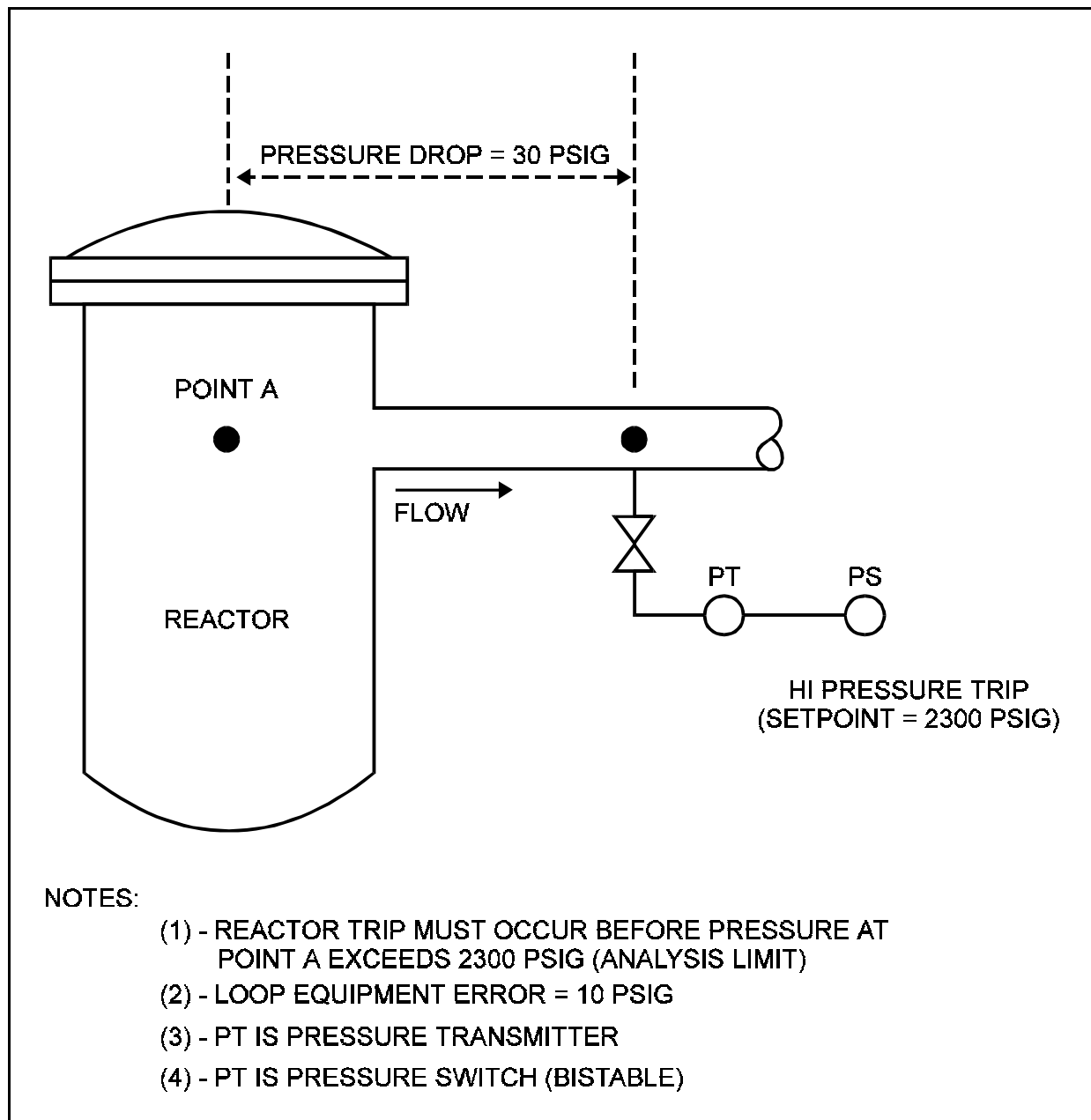


Figure F-1. Line pressure loss example

Appendix G: RTD accuracy confirmation

The accuracy of an RTD can be confirmed using several different approaches. The ease of use and feasibility of each is dependent on the type of RTD installation. The four approaches in common use today are

- a) comparison against a standard in a controlled environment; i.e., temperature bath;
- b) normalization against a standard in a semicontrolled environment; i.e., during significant plant temperature changes (heatup or cooldown);
- c) cross-calibration (or self-normalization) of a significant number of RTDs during plant temperature changes; and
- d) replacement of the RTDs with factory-calibrated units.

There may be a shift in the accuracy of the calibration curve of the device if a mechanical shock is received before or during installation. The accuracy of the platinum-lead RTDs generally used is based on a strain-free condition. Exposure to a mechanical shock severe enough to introduce a change in this condition can invalidate the assumption that the device is calibrated to a fine tolerance. Therefore, extreme care should be taken in the treatment of these devices to assure that the calibration curve determined at the factory before shipment is maintained. Approaches (b) and (c) minimize the handling of these devices and also gather data after installation. This allows the verification of the accuracy in situ. While approach (c) does not have an explicit comparison against a traceable standard, the accuracy may be reasonable for setpoint determination when a large enough sample is used.

In approach (b), replacement of one or more RTDs with factory-calibrated units allows the normalization of the remaining RTDs against the replacement units. The data is taken during a plant heatup or cooldown, resulting in a semicontrolled environment; i.e., the system temperature is known to the accuracy of the replacement units. The stability of the temperature during the gathering of data is a function of the plant equilibrium both from a real and a procedural point of view (allowed temperature drift during the data gathering and potential stratification if the RTDs are not all in the same orientation). This approach decreases the number of RTDs replaced when compared to approach (d) and results in a slightly higher uncertainty associated with verification of the calibration curve. Approaches (a) and (d) result in a low uncertainty concerning the accuracy of the devices, since they are calibrated under precise conditions. However, there is no in situ verification that the determined accuracy is valid after installation.

During the performance of RTD accuracy verification, the following items should be considered:

- a) While it is not necessary to have a 0°F rate of change as a function of time, it is recommended that the rate of change be constant during the gathering of data.
- b) Multiple data points for each RTD should be gathered at each temperature to reduce the uncertainty at that temperature.
- c) Multiple temperature points should be used to verify the calibration curve in the range of interest and to minimize extrapolation errors.
- d) Use a high accuracy readout device capable of compensating for lead wire imbalance.

- e) All RTD lead combinations should be utilized during the verification process to allow use of the combination (either two, three, or four leads depending on the resistance to voltage or resistance to current conversion used in the instrument channel), which minimizes lead imbalance uncertainties. Any thermal EMF generated (from different metals at the lead junctions) should be considered when connecting the RTD to the electronics.
- f) Leadwire resistance changes from environmental temperature variations should be considered for the two- and three-wire RTDs. This effect is a bias.

Appendix H: Uncertainties associated with digital signal processing

This appendix presents a discussion on digital signal processing and the uncertainties involved with respect to determining instrument channel setpoints for a digital system. [Figure H-1](#) presents a simplified block diagram of a digital processing system. The digital processor receives an analog input signal and provides an output in either digital or analog form. [Figure H-2](#) presents a block diagram for the typical operations performed in the digital processor. [Figure H-2](#) could be representative of process control computers, microcomputers, programmable controllers, etc.

The analog signal is received by the digital processor, filtered, digitized, manipulated, converted back into analog form, filtered again, and sent out. The digital processor is treated as a black box; therefore, the discussion that follows is applicable to many different types of digital processors. The digital processor is programmed to run a controlled algorithm. Basic functions performed are addition, subtraction, multiplication, and division as well as data storage. The digital processor is the most likely component to introduce rounding and truncation errors.

The analog input signal is first processed by a filter to reduce aliasing noise introduced by the signal frequencies that are high relative to the sampling rate. The filtered signal is sampled at a fixed rate and the amplitude of the signal held long enough to permit conversion to a digital word. The digital words are manipulated by the processor based on the controlled algorithm. The manipulated digital words are converted back to analog form, and the analog output signal is smoothed by a reconstruction filter to remove high frequency components.

Several factors affect the quality of the representation of analog signals by digitized signals. The sampling rate affects aliasing noise; the sampling pulse width affects analog reconstruction noise; the sampling stability affects jitter noise; and the digitizing accuracy affects the quantization noise.

H.1 Sampling rate uncertainty

If the sampling rate is higher than twice the analog signal bandwidth, the sampled signal is a good representation of the analog input signal and contains all of the significant information. If the analog signal contains frequencies that are too high with respect to the sampling rate, aliasing uncertainty will be introduced. Anti-aliasing band-limiting filters can be used to minimize the aliasing uncertainty or else it should be accounted for in setpoint calculations.

H.2 Signal reconstruction uncertainty

Some information is lost when the digitized signal is sampled and held for conversion back to analog form after digital manipulation. This uncertainty is typically linear and about $\pm 1/2$ least significant bit (LSB).

H.3 Jitter uncertainty

The samples of the input signal are taken at periodic intervals. If the sampling periods are not stable, an uncertainty corresponding to the sampled signal's rate-of-change will be introduced. The jitter uncertainty is insignificant if the clock is crystal-controlled, which it is in the majority of cases.

H.4 Digitizing uncertainty

When the input signal is sampled, a digital word is generated that represents the amplitude of the signal at that time. The signal voltage must be divided into a finite number of levels that can be defined by a digital word "n" bits long. This word will describe 2^n different voltage steps. The signal levels between these steps will go undetected. The digitizing uncertainty (also known as the quantizing uncertainty) can be expressed in terms of the total mean square error voltage between the exact and the quantized samples of the signal. An inherent digitizing uncertainty of $\pm 1/2$ LSB typically exists. The higher the number of bits in the conversion process, the smaller the digitizing uncertainty.

H.5 Miscellaneous uncertainties

Analog-to-digital converters also introduce offset uncertainty; i.e., the first transition may not occur at exactly $\pm 1/2$ LSB. Gain uncertainty is introduced when the difference between the values at which the first transition and the last transition occur is not equal. Linearity uncertainty is introduced when the differences between the transition values are not all equal.

For digital-to-analog conversion, the maximum linearity uncertainty occurs at full scale when all bits are in saturation. The linearity determines the relative accuracy of the converters. Deviations from linearity once the converters are calibrated is absolute uncertainty. Power supply effects may also be considered for unregulated power supplies.

H.6 Truncation and rounding uncertainties

The effect of truncation or rounding depends on whether fixed point or floating point arithmetic is used and how negative numbers are represented and should be considered as a possible uncertainty.

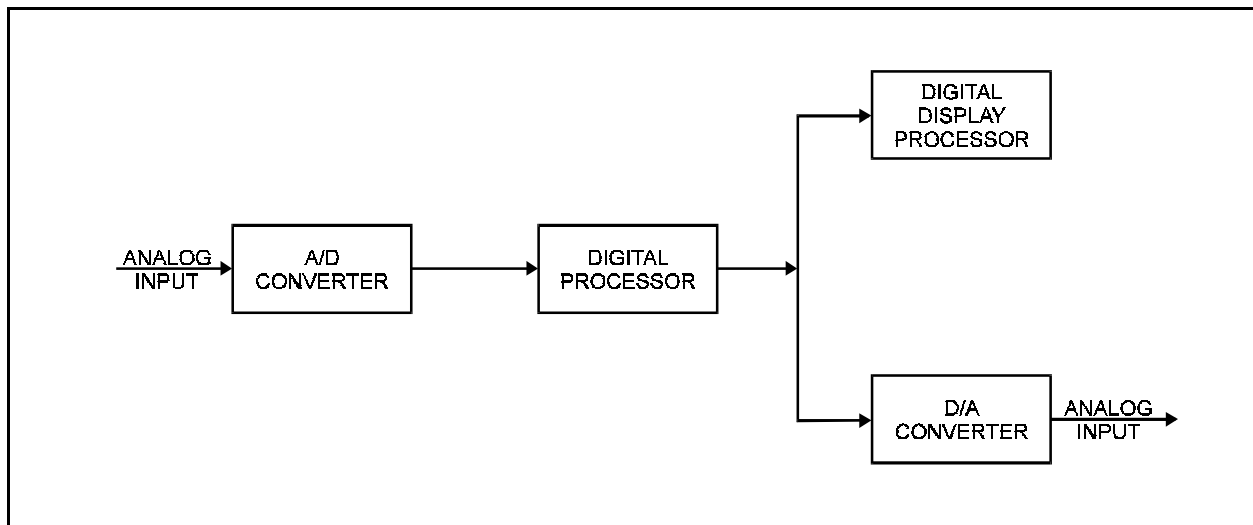


Figure H-1. Digital processing system simplified block diagram

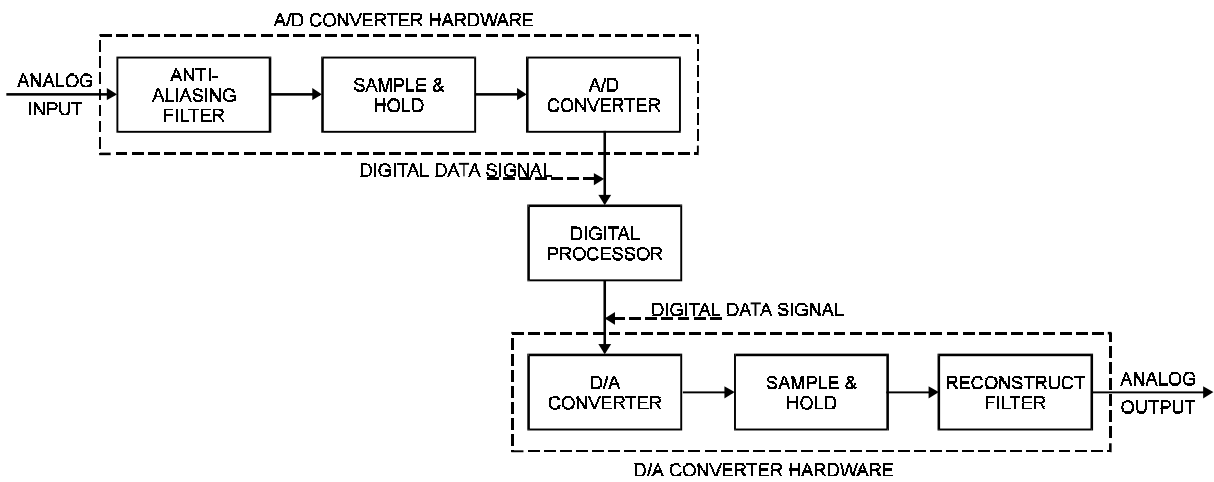


Figure H-2. Digital processor block diagram

Annex I: Recommendations for inclusion of instrument uncertainties during normal operation in the allowable value determination

ISA-S67.04, Part I, 4.3.2, and ISA-RP67.04, Part II, 7.3, allow the use of instrument calibration uncertainties, instrument uncertainties during normal operation, and instrument drift in the determination of the allowable value (AV). The instrument uncertainties during normal operation are listed in 4.3.1(b) of S67.04, Part I. However, it is not always appropriate to include all of these uncertainties in the allowance between the AV and the trip setpoint (TS). The following discussion provides recommendations for their inclusion in the determination of the AV.

Recall that the AV is a parameter to be used by the plant to verify channel performance at prescribed surveillance intervals. Therefore, of the uncertainties listed in S67.04, 4.3.1(b), only those associated with events expected to cause changes that would be discernible during those periodic surveillances (as opposed to cycle recalibrations) should be included in the allowance between the AV and the TS.

When using the methods described in 7.3 or RP67.04, Part II, excluding any of these parameters from the allowance between the AV and the TS is conservative since the difference between the AL and the AV will increase. Thus, decreasing the difference between the TS and AV results in a smaller allowance for drift for the channel being tested. The following items should be considered when determining whether or not to include the effects of each of these uncertainties in the allowance between the AV and TS (the numbers and titles refer to the associated paragraphs in S67.04, Part I):

4.3.1(b)1 - Reference accuracy

The "calibration accuracy" as described in RP67.04, Part II, 6.2.6, assumed the "tested" portion of the channel should be included in the allowance between the AV and TS. The various device "calibration accuracies" should be combined in the same fashion when determining AV as when the "total error" was determined.

4.3.1(b)2 and 3 - Power supply voltage and frequency changes

These may be included if it is determined that their effects are significant and are likely to be observed. Typically, however, these effects are small and are not usually measured, in which case, their inclusion in AV may be nonconservative.

4.3.1(b)4 - Temperature changes

If the temperature change expected to occur between periodic surveillances has a corresponding uncertainty that is significant, it may be included in the allowance between the AV and TS. However, if the temperature at the time of the surveillance is expected to be relatively constant with respect to the temperature change assumed in the setpoint calculation for the "tested" portion of the channel, the uncertainty due to temperature changes should not be included in this allowance.

EXAMPLE:

Suppose the temperature effects associated with the process electronics were assumed to be $\pm 1.0\%$ span based on an assumed ambient temperature of $80^{\circ}\text{F} \pm 30^{\circ}\text{F}$. If the process electronics are located in an environment where the temperature is expected to be maintained within a small band, $\pm 3^{\circ}\text{F}$ for instance, where the temperature effects are

negligible, it would not be necessary to include temperature effects in the allowance between the AV and TS. If, however, the process electronics were located in an uncontrolled environment, perhaps subject to swings in seasonal temperatures, and these swings were expected to be significant, it would then be appropriate to consider including uncertainties due to temperature effects when determining the allowance between the AV and TS.

4.3.1(b)5 - Humidity changes

See previous discussions on temperature.

4.3.1(b)6 - Pressure changes

See previous discussion on temperature.

4.3.1(b)7 - Vibration

Effects due to the in-service vibration, if expected to be significant between periodic surveillances, may be considered for inclusion in the allowance between the AV and TS.

Effects due to seismic vibration, however, should not be included since seismic vibration is not a normal occurrence between periodic surveillances.

4.3.1(b)8 - Radiation exposure

Effects due to radiation exposure during normal operation, if expected to be significant between periodic surveillances, may be considered for inclusion in the allowance between the AV and TS.

4.3.1(b)9 - Analog-to-digital conversion

If analog-to-digital conversion is part of the "tested" portion of the channel, uncertainties due to the A/D conversion should be included in the allowance between the AV and the TS.

Appendix J: Discussions concerning statistical analysis

J.1 Square root sum squares (SRSS) combination

The SRSS methodology for combining uncertainty terms that are random and independent is an established and accepted analytical technique. The SRSS methodology is a direct application of the central limit theorem, providing a method for determining the limits of a combination of independent and random terms. The probability that all the independent processes under consideration would simultaneously be at their maximum value in the same direction (i.e., + or -) is very small. The SRSS methodology provides a means to combine individual random uncertainty terms to establish a resultant net uncertainty term with the same level of probability as the individual terms. If an individual uncertainty term is known to consist of both random and bias components, the components should be separated to allow subsequent combination of like components. Bias components should not be mixed up with random components during SRSS addition.

Resultant net uncertainty terms should be determined from individual uncertainty terms based on a common probability level. In some cases individual uncertainty terms may need to be adjusted to the common probability level. Typically, a probability level that corresponds to two standard deviations (2 sigma) is used. Using probability levels that correspond to three or more standard deviations may be unnecessarily conservative, resulting in reduced operating margin. For example, if a reference accuracy for a 99% probability level (3 sigma) is given as ± 6 psig, the 95% probability level corresponds to ± 4 psig ($= 2/3 \times 6$).

The central limit theorems require that the variables to be combined must be random and independent. Some statements of the theorem allow individual variables to be either identically or arbitrarily distributed. Then, if the number of components, n , is large, the distribution of the sum will be approximately normal. (See K.V. Bury and P.L. Meyer References). "Large" has been interpreted as 10-30. (See J.M. Hammersley Reference.) Another statement of the theorem requires individual variables to be approximately normally distributed, and their variances about equal (none are dominant). If these conditions are met, the sum of the components will be approximately normally distributed even for a relatively small n . "Relatively small" has been interpreted as low as 4. (See H.H. Ku Reference.) In the limiting case, if two individual variables are exactly normal, their sum is exactly normal as well.

When a random variable represents the net effect of a large number of smaller, independent, unmeasurable causes, the variable can be expected to be approximately normally distributed. The approximation becomes better as the number of contributors increases. Empirical evidence suggests that the normal distribution provides a good representation of many physical variables, including instrument uncertainties. This observation is consistent with the fact that most instrument channels are composed of several parts that contribute independent, random uncertainties to the net sum. Even if the number of modules in a given instrument loop is relatively small, the number of elemental uncertainty sources within the modules can be much larger, making the SRSS summation justifiable.

It should be noted that some random variables cannot be reasonably considered as the sum of many small uncertainties and, consequently, should not be expected to be normally distributed. For example, the predominance of one non-normal uncertainty within a sum may not allow the

sum to approximate normality. For such a case, the non-normal uncertainty is called abnormally distributed and should be summed separately.

A different approach in the application of the SRSS technique is presented in ANSI/ASME PTC 19.1; the SRSS combination of biases is used and justified on the basis that all of the biases are random. The reader is cautioned that ANSI/ASME PTC 19.1 is intended for application to activities different from the purpose of this recommended practice. However, there may be situations involving the combination of significant numbers of random biases that could be treated by SRSS. The conditions for the use of the ANSI/ASME PTC 19.1 approach include the application of a bias concept that differs from this recommended practice and the calculation of an uncertainty coverage interval that differs from the confidence and tolerance intervals discussed in the next section.

J.2 Confidence and tolerance intervals

In the context of setpoint determination, nuclear plant engineering groups are likely to deal with the numerical intervals from different sources. These include the analysis of field data by plant personnel and the use of manufacturer's specifications.

Field measurements at a plant can form the database for statistical analysis using known techniques. Normality tests and knowledge of sample sizes allow determining the closeness of commonly used approximations. These include normality and the closeness of estimators with true population parameters. The parameters population mean (μ) and standard deviation (σ) are estimated by the sample mean ($\bar{x}$) and standard deviation (s). This approximation is made better as the sample size increases.

If these approximations are taken, it is sufficient to describe a probability interval as a range of values that includes (with a pre-assigned potential for occurrence called the confidence level) the true value of a population parameter. For a normal distribution, a $\pm 1.96 s$ interval (approximately $\pm 1.96 \sigma$) has a 95% probability of including the true parameter. Another common interpretation is that 95% of the population is contained in the interval.

If a sample population is known to be small, it may be difficult to justify the above approximations, and it is appropriate to establish uncertainty limits using statistical tolerance intervals. This approach requires the additional statement about the population proportion included in the interval.

It is frequently desired to describe a tolerance interval using the sample mean and the sample standard deviation such as $\bar{x} \pm Ks$. The value of K (tolerance factor) is a function of the sample size, the confidence level, the population proportion, and whether the distribution is one-sided or two-sided. Tables of K values are given in A.H. Bowker and H.H. Ku References.

Numerical intervals also originate from manufacturer's product specifications. The $\pm A$ specification may represent a confidence interval (with a specified confidence level and an implicit assumption that estimators closely agree with population parameters) or a tolerance interval (with specified confidence level, population proportion, and sample size). The correct interpretation often requires discussion with the instrument manufacturer.

Appendix K: Propagation of uncertainty through signal-conditioning modules

This appendix discusses techniques for determining the uncertainty of a module's output when the uncertainty of the input signal and the uncertainty associated with the module are known. Using these techniques, equations are developed to determine the output uncertainties for several common types of functional modules.

For brevity, error propagation equations will not be derived for all types of signal-processing modules. Equations for only the most important signal-processing functions will be developed. However, the methods discussed can be applied to functions not specifically addressed here. The equations derived are applicable to all signal conditioners of that type regardless of the manufacturer.

The techniques presented here are not used to calculate the inaccuracies of individual modules; they are used to calculate uncertainty of the output of a module when the module inaccuracy, input signal uncertainty, and module transfer function are known.

This section discusses only two classifications of errors or uncertainties: those that are random and independent and can be combined statistically, and those that are biases and must be combined algebraically. The methods discussed can be used for both random and biased uncertainty components.

It is important to note that the method of calibration or testing may directly affect the use of the information presented in this section. If, for example, all of the modules in the process electronics for a particular instrument channel are tested together, they may be considered one device. The uncertainty associated with the output of that device should be equal to or less than the uncertainty calculated by combining all of the individual modules.

K.1 Error propagation equations using partial derivatives and perturbation techniques

Several valid approaches for the derivation of equations express the effect of passing an input signal with an error component through a module that performs a mathematical operation on the signal. The approaches discussed here, which are recommended for use in developing error-propagation equations, are based on the use of partial derivatives (see C.S. Zalkind Reference) or perturbation techniques; i.e., changing the value of a signal by a small amount and evaluating the effect of the change on the output. Either technique is acceptable and the results, in most cases, are similar.

For simplicity, this discussion assumes that input errors consist of either all random or all biased uncertainty components. The more general case of uncertainties with both random and biased components is addressed later in this appendix.

K.2 Propagation of input errors through a summing function

The summing function is represented by the equation

$$c = k_1 * A + k_2 * B \quad (\text{Eq. K.1})$$

where k_1 and k_2 are constants that represent gain or attenuation of the input signals.

Accounting for input errors, the equation becomes

$$C + c = k_1 * (A + a) + k_2 * (B + b) \quad (\text{Eq. K.2})$$

where

A and B = inputs;
C = the output;
a, b, c = associated errors.

Subtracting Equation K.1 from Equation K.2 leaves

$$c = (k_1 * a) + (k_2 * b) \quad (\text{Eq. K.3})$$

This equation is appropriate for combining bias (systematic) errors.

If the errors are random; i.e., they can be combined by SRSS methods, the equation becomes

$$c(\text{SRSS}) = [(k_1 * a)^2 + (k_2 * b)^2]^{1/2} \quad (\text{Eq. K.4})$$

Using partial derivatives

$$\delta C / \delta A = \delta(k_1 * A) / \delta A + \delta(k_2 * B) / \delta A \quad (\text{Eq. K.5})$$

$$\delta C / \delta B = \delta(k_1 * A) / \delta B + \delta(k_2 * B) / \delta B \quad (\text{Eq. K.6})$$

which yields

$$\begin{aligned} \delta C &= (\delta C / \delta A) * \delta A + (\delta C / \delta B) * \delta B \\ &= k_1 * dA + k_2 * dB \end{aligned} \quad (\text{Eq. K.7})$$

If $\delta A = +a$, $\delta B = +b$, and $\delta C = +c$

$$c = + (k_1 * a) + (k_2 * b) \quad (\text{Eq. K.8})$$

Again, using SRSS methods

$$\delta C = \pm [[(\delta C / \delta A) * a]^2 + [(\delta C / \delta B) * b]^2]^{1/2} \quad (\text{Eq. K.9})$$

from which

$$c(\text{SRSS}) = \pm [(k_1 * a)^2 + (k_2 * b)^2]^{1/2} \quad (\text{Eq. K.10})$$

Notice that in this case the same error propagation equations are obtained using either partial derivatives or perturbation techniques.

K.3 Propagation of input errors through a multiplication function

The equation for a multiplier is

$$C = (k_1 * A) * (k_2 * B) \quad (\text{Eq. K.11})$$

where k_1 and k_2 are linear gains or attenuation of the input signals.

Adding error terms yields

$$C + c = k_1(A + a) * k_2(B + b) \quad (\text{Eq. K.12})$$

which expands to

$$C + c = (k_1 * A * k_2 * B) + (k_1 * A * k_2 * b) + (k_1 * a * k_2 * B) + (k_1 * a * k_2 * b) \quad (\text{Eq. K.13})$$

Subtracting Equation K.11 from Equation K.13 yields

$$c = (k_1 * A * k_2 * b) + (k_1 * a * k_2 * B) + (k_1 * a * k_2 * b)$$

or

$$c = k_1 * k_2 * [(A * b) + (a * B) + (a * b)] \quad (\text{Eq. K.14})$$

This is more precise than the equation obtained from partial derivatives

$$c = k_1 * k_2 * [(A * b) + (B * a)] \quad (\text{Eq. K.15})$$

The product of two or more error components; e.g., $a * b$, is small and may be ignored. They are included here to illustrate differences in the precision of calculations based on error propagation and calculations based on partial derivatives. In cases where there are many products of errors, it may be prudent to include them in the calculation and do the calculation on a computer.

Applying SRSS error combination to Equation K.14 yields

$$c(\text{SRSS}) = \pm k_1 * k_2 * [(A * b)^2 + (B * a)^2 + (a * b)^2]^{1/2} \quad (\text{Eq. K.16})$$

The term $(a * b)^2$ is extremely small and may be ignored. It is retained here for completeness.

Equation K.16 can be simplified further by expressing the errors in relative terms (c/C , a/A , b/B). The first order approximation of Equation K.16 is

$$c = \pm k_1 * k_2 * [\pm(A * b)^2 \pm (a * B)^2]^{1/2} \quad (\text{Eq. K.16a})$$

Squaring Equation K.16a and dividing by the square of Equation K.11 gives upon further reduction

$$c/C = [(a/A)^2 + (b/B)^2]^{1/2} \quad (\text{Eq. K.16b})$$

Several authors give simplified forms of error propagation equations for commonly used functions. (See ANSI/ASTM E 178.)

K.4 Error propagation through other functions

Table 1 shows equations for other functions derived by the same techniques. Note that these equations are useful only for determining the effect of a module on uncertainties in the input signal.

Using partial derivative techniques, suitable approximations can be derived from analytical descriptions (function f) of the transfer functions (or a Taylor series expansion) using the following general formula:

Random:

$$c = \pm[(\delta f / \delta a)^2 * a^2 + (\delta f / \delta b)^2 * b^2]^{1/2}$$

Bias (known sign):

$$c = (\delta f / \delta a) * a + (\delta f / \delta b) * b$$

Abnormal distribution or bias (unknown sign):

$$c = |(\delta f / \delta a) * a| + |(\delta f / \delta b) * b|$$

K.5 Accounting for module errors

K.5.1 Combining module errors with propagated input errors

So far we have dealt with the effects of a module's transfer function on inaccuracies or uncertainties present with the input signal. Besides affecting errors already present on input signals, each module contributes its own errors to the signals.

In the simplest case, where the module error can be represented by a single term, e_m , which is independent of module and configuration, the error at the module output becomes

$$e_o = \pm(e_{ip} + e_m) \quad (\text{Eq. K.17})$$

or

$$e_o(\text{SRSS}) = \pm(e_{ip}^2 + e_m^2)^{1/2} \quad (\text{Eq. K.18})$$

where

e_{ip} = propagated input error ([see Figure K-1](#)).

A more general case is illustrated in [Figure K-2](#). The output of this module without errors is

$$E_o = \{[(A) * (G_1) + (B)] (G_2)\} * (G_3) \quad (\text{Eq. K.19})$$

Considering input error propagation and device and adjustment errors within the module, the equation for the output becomes

$$E_o + e_o = \{[(A + a) * (G_1 + g_1) + (B + b)](G_2 + g_2) + e_z\} * (G_3 + g_3) + e_m \quad (\text{Eq. K.20})$$

Subtracting Equation K.19 from Equation K.20 yields

$$e_o = e_m + (A * G_1 + B) * (G_2 + g_2) * (G_3 + g_3) + \{[A * g_1 + (a) * (G_1 + g_1) + (b)] * (G_2 + g_2) + e_z\} * (G_3 + g_3) \quad (\text{Eq. K.21})$$

or

$$e_o(\text{SRSS}) = \pm (e_m^2 + (A * G_1 + B) * (G_2 + g_2) * (G_3 + g_3) + \{[A * g_1 + (a) * (G_1 + g_1) + (b)] * (G_2 + g_2) + e_z\} * (G_3 + g_3)^2)^{1/2} \quad (\text{Eq. K.22})$$

This error term would be the input signal error to the next module in the channel.

K.5.2 Quality of module error data

Error calculations are affected by how much module error data is available and by how it is presented. Ideally, the magnitude, nature (random or bias), and source (drift, temperature effect, linearity, etc.) of each error component should be available. Error data should be traceable to the hardware vendor or to the independent test documentation.

Although most error terms are random, it is not prudent to assume that errors induced by accident condition environments will not be systematic. Module errors may be estimated by analysis. One useful technique is the Monte Carlo simulation. Four requirements for successful simulation are (1) the determination of sensitive components; i.e., those that have the greatest influence on accuracy; (2) product approximation of error distributions (Gaussian is usually the most accurate; uniform distribution is slightly more conservative; unusual distributions should be accurately modeled); (3) generation of a sufficient number of simulated cases; and (4) verification of the analysis by adequate testing.

K.6 Accounting for bias (systematic) error components

Although it is expected that most error components will be random and can be combined using SRSS methods, bias error components must, at times, be dealt with. Perturbation techniques are well-suited to handling combinations of bias and random error components. Calculations using these techniques will be at least as accurate as calculations using partial derivatives.

Using the multiplication functions as an example, the equation without errors is

$$C = A * B \quad (\text{Eq. K.23})$$

With errors it becomes

$$C \pm c = (A \pm a) * (B \pm b) \quad (\text{Eq. K.24})$$

If the a and b terms each contain both random and bias components, the equation becomes

$$C \pm c = (A \pm a_r \pm a_b) * (B \pm b_r \pm b_b) \quad (\text{Eq. K.25})$$

where

a_r, b_r = random components;

a_b, b_b = bias components.

Subtracting Equation K.23 from Equation K.25

$$c = \pm A * b_r \pm B * a_r \pm a_r * b_r \pm a_r * b_b \pm a_b * b_r \pm A * b_b + B * a_b + a_b * b_b \quad (\text{Eq. K.26})$$

The first five terms can be considered random because at least one member of each term is a random error. These terms can be combined using SRSS. The last three terms consist only of constants and bias components and must be added algebraically. The final equation becomes

$$c = \pm [(A * b_r)^2 + (B * a_r)^2 + (a_r * b_r)^2 + (a_r * b_b)^2 + (a_b * b_r)^2]^{1/2} + A * b_b + B * a_b + a_b * b_b \quad (\text{Eq. K.27})$$

Assuming that the module error, which must be combined with the propagated input errors, also has random and bias components ($e_r + e_b$) and that the module error can be considered as being added at the module[†], the output error, e_o , is

$$e_o = \pm[(A * b_r)^2 + (B * a_r)^2 + (a_r * b_r)^2 + (a_r * b_b)^2 + (a_b * b_r)^2 + e_r^2]^{1/2} + A * b_b + B * a_b + a_b * b_b + e_b \quad (\text{Eq. K.28})$$

Terms involving the product of error terms are often so small that their exclusion does not significantly affect the result of the setpoint calculation.

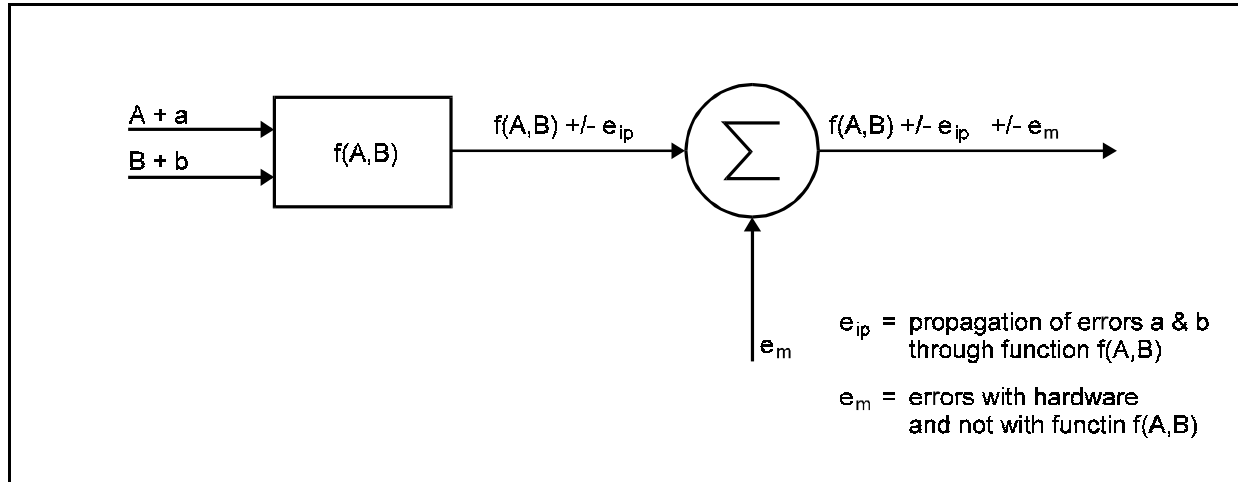


Figure K-1. Accounting for hardware errors

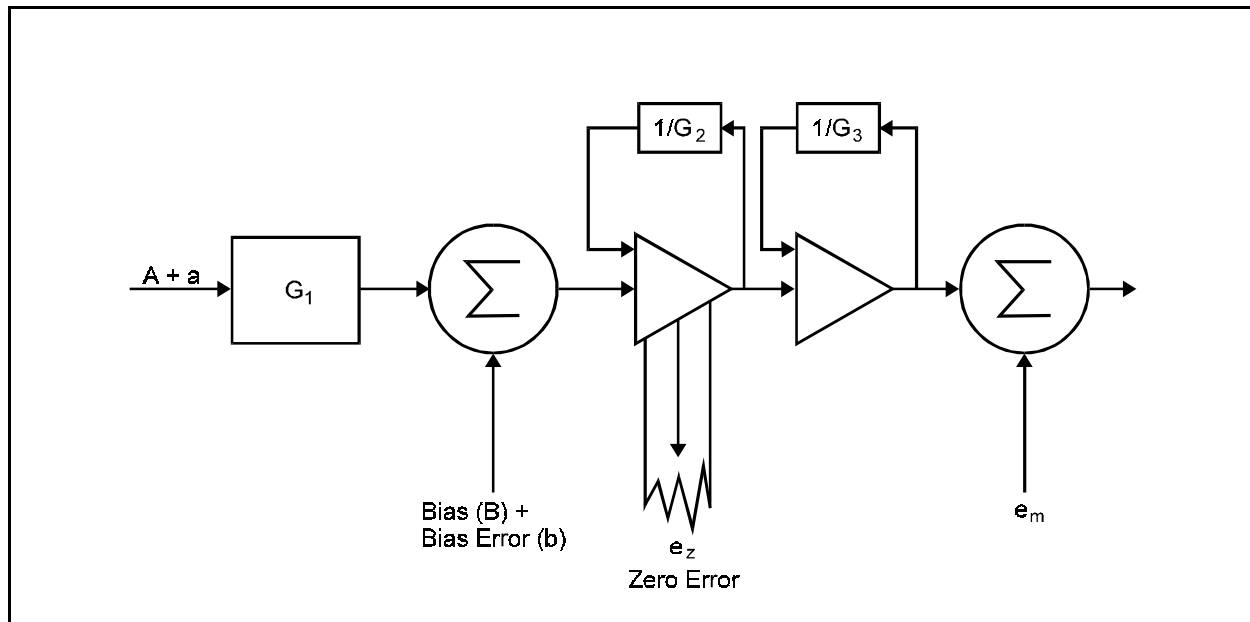


Figure K-2. Accounting for hardware errors (more typical case)

Appendix L: Example uncertainty/setpoint calculations

The following calculations are intended to illustrate selected concepts discussed in the RP and give practical examples of calculations that are consistent with the RP methodology. Four examples are provided.

CALCULATION	SPECIFIC CONCEPTS ILLUSTRATED
Pressure Trip	Applicable to several channels Assumptions to cover missing data One M&TE value for entire channel Check calculation
Flow Trip	Non-linear device Plant specific setpoint methodology used as reference Drift data extrapolation Independent and dependent M&TE
Level Trip	Multi-variable (temperature compensated) loop Accident condition errors IR losses Signal-conditioning module uncertainty propagation
Radiation Trip	Non-linear device Logarithmic error analysis Non-LSSS loop

Included in these examples are certain unique aspects that should not be construed as required for all similar calculations. Conversely, the terms deemed applicable for these examples should not be considered to be the only terms applicable to any similar calculation. The preparer of each calculation is responsible for including all terms necessary and appropriate to comply with the guidelines outlined in the RP.

Different calculation formats are used; these formats are used for illustrative purposes only and should not be construed as recommendations of this RP. The format of the error calculations, which sections are included, the sequence and title of the sections, and the content of the sections must be determined by the preparer of the calculation. In addition to these format issues, other specific administrative and technical content/approach requirements such as the level of justification(s) required for any non-obvious assumptions, acceptable "round-off" techniques, etc., should be governed by the user's quality assurance, design control programs, or other applicable administrative procedures related to preparation of calculations.

The calculations are supplemented by a "COMMENTS" column to the right of the page. These comments are not intended to be part of actual calculations; the comments are intended to provide additional information or appropriate references to the RP and to highlight unique aspects of each calculation.

EXAMPLE CALCULATION — PRESSURE TRIP

CALCULATION	COMMENTS
1.0 Purpose The purpose of this calculation is to determine if the setpoint that has been established as part of the NSSS Standard Technical Specifications (Reference 3.1) is appropriate for the specific application at Nuclear Plant Unit #2. The specific application included in this calculation is for the Containment High Pressure Trip into the Steamline Isolation Logic. This calculation is required since the equipment suppliers for these components for Nuclear Plant Unit #2 are different than the equipment suppliers assumed by the NSSS. This calculation is being prepared to comply with our commitments to Reg. Guide 1.105 (Reference 3.2) as outlined in FSAR Section 1.8 (Reference 3.3). In addition this calculation has been prepared to be consistent with the methodology outlined in ISA-S67.04 (Reference 3.4). 2.0 Assumptions 2.1 There are no known bias or dependent uncertainty for any of the modules involved in this application (based on review of References 3.8, 3.9, and 3.10). 2.2 M&TE uncertainty for applications similar to that outlined in this calculation have been standardized at $\pm 0.5\%$ of process span (based on Reference 3.7.f). 2.3 Final values of calculations will be rounded-off to achieve a consistent calculation degree of accuracy. 2.4 A margin of 1.0 psig has been applied to the total channel uncertainty (based on Reference 3.7.g). 2.5 A local temperature transient effect value for the pressure transmitter has been assumed to be $\pm 1.0\%$ U.R.L. (See Calculation Sections 7.0 and 11.0.) 3.0 References 3.1 NSSS Technical Report 1234, Revision B, "Standard Technical Specifications for Three-Loop Pressurized Water Reactors."	<i>Note: The following format is for illustrative purposes only. See RP Preface, Section 10, and Page 103.</i> <i>RP Sections 5.2 and 5.3 were reviewed to identify potentially applicable factors.</i> <i>See RP Section 6.2.6.</i> <i>See Page 105. In this example, the final value for Eq. 6 - Eq. 13 has been adjusted to the nearest 0.1 unit.</i> <i>See RP Section 9. Reflects interface with other organizations.</i>

CALCULATION**COMMENTS**

3.2 U.S. Nuclear Regulatory Commission, Regulatory Guide 1.105, Revision 2, February 1986, "Instrument Setpoints for Safety-Related Systems."

3.3 Nuclear Plant Unit, Final Safety Analysis Report, Revision O.

- a. Section 1.8, Conformance to NRC Regulatory Guides
- b. Section 3.11, Environmental Qualification of Mechanical and Electrical Equipment
- c. Section 6.2, Containment Systems
- d. Section 7.0, Instrumentation and Controls
- e. Section 15.0, Accident Analyses

3.4 ANSI/ISA-S67.04-1987, "Setpoints for Nuclear Safety-Related Instrumentation."

3.5 ISA-dRP67.04, Part II, Draft 7, "Methodologies for the Determination of Setpoints For Nuclear Safety-Related Instrumentation."

3.6 Nuclear Plant Unit #2, Drawings

- a. P&ID, P-01, Rev. 3
- b. Instrument Location, I-01, Rev. 2
- c. Electrical Loop Schematic, E-01, Rev. 4
- d. Plant Location, L-01, Rev. 1

3.7 Nuclear Plant #2 Documents

- a. Calibration Procedure C-01, Rev. 0., Safety-Related Pressure Loops
- b. Component Data Sheet (PT-MS-01), Issue 0
- c. Component Data Sheet (PSL-MS-01), Issue 0
- d. Test & Measurement Record, PI Serial #123
- e. Test & Measurement Record, DVM Serial #456
- f. Engineering Evaluation, EE-008, Rev. 0, "M&TE" Effects on Selected Applications
- g. PORC Meeting Minutes for 1/4/88

3.8 Precise Pressure Company Product Literature

- a. Pressure Transmitter Literature
- b. DVM Literature
- c. Pressure Gauge Literature

CALCULATION

COMMENTS

3.9 Excellent Electronics Company Product Literature

3.10 Terrific Testing Lab, Qualification Report Q-100, Issue 3, "Safety-Related Pressure Transmitters for Nuclear Plant Unit #2."

3.11 Letter, dated 2/29/88, P. Gage (President, Precise Pressure Company) to A. Manager (Senior V.P., Nuclear Plant Units 1 and 2), Subject: Environmental Qualification Testing.

4.0 Functional description

The containment high pressure trip is one of several inputs into the Steamline Isolation Logic to detect a high energy line break (MSLB or LOCA) inside containment. This trip condition is measured by means of redundant pressure transmitters as outlined in [Reference 3.3.c](#). The total application for this parameter consists of three sets of three pressure transmitters, loop power supplies, and bistables, each. This calculation applies to the following:

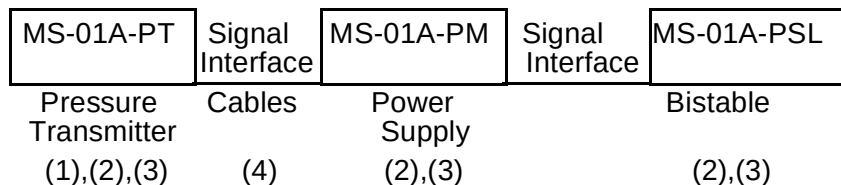
MS-01A-PT	MS-02A-PT	MS-03A-PT
MS-01B-PT	MS-02B-PT	MS-03B-PT
MS-01C-PT	MS-02C-PT	MS-03C-PT
MS-01A-PM	MS-02A-PM	MS-03A-PM
MS-01B-PM	MS-02B-PM	MS-03B-PM
MS-01C-PM	MS-02C-PM	MS-03C-PM
MS-01A-PSL	MS-02A-PSL	MS-03A-PSL
MS-01B-PSL	MS-02B-PSL	MS-03B-PSL
MS-01C-PSL	MS-02C-PSL	MS-03C-PSL

All these components are located outside the containment.

5.0 Block diagram

See [RP 5.2](#) and [Figure 1](#).

<_Auxiliary Building_|_Control Room Complex_>



Uncertainty Allowances to Address

- (1) Process Measurement Effects
- (2) Equipment Uncertainties
- (3) Calibration Uncertainties
- (4) Other Uncertainties

CALCULATION**COMMENTS****6.0 Determine uncertainty equations**

The following total channel uncertainty equations from [Reference 3.5](#) will be used as the basis for this calculation

$$CU^+ = + [PM^2 + PE^2 + e_1^2 + e_2^2 + \dots e_n^2]^{1/2} + B_T^+ \quad (\text{Eq. 1a})$$

See [RP 6.1](#) and [6.3](#).

Variation of RP Eq. 6.10a.

$$CU^- = - [PM^2 + PE^2 + e_1^2 + e_2^2 + \dots e_n^2]^{1/2} - B_T^- \quad (\text{Eq. 1b})$$

Variation of RP Eq. 6.10b.

where

CU = Channel Uncertainty (CU) at a specific point in the channel; the CU can be calculated for any point in a channel from Module 1 to Module n, as needed;

PM = Random uncertainties that exist in the channel's basic Process Measurement (PM);

PE = Random uncertainties that exist in a channel's Primary Element (PE), if it has one, such as the accuracy of a flowmeter table;

$e_{1,2,n}$ = Total random uncertainty of each module that makes up the loop from Module (e_1), through Module (e_n);

B_T^+ = The total of all positive biases associated with a channel; this would include any uncertainties from PM, PE, or the Modules that could not be combined as a random term (both true biases and arbitrarily distributed uncertainties);

B_T^- = The total of all negative biases associated with a channel.

The individual module random uncertainties are in themselves a statistical combination of uncertainties. Depending on the type of module, its location, and the specific factors that can affect its accuracy, the determination of the module uncertainty will vary. For example, the module uncertainty for a module may be calculated as follows:

$$e^+ = +[RA^2 + DR^2 + TE^2 + RE^2 + SE^2 + HE^2 + SP^2 + MTE^2]^{1/2} + B^+ \quad (\text{Eq. 2a})$$

See RP Eq. 6.11a.

$$e^- = -[RA^2 + DR^2 + TE^2 + RE^2 + SE^2 + HE^2 + SP^2 + MTE^2]^{1/2} - B^- \quad (\text{Eq. 2b})$$

See RP Eq. 6.11b.

where

e = Uncertainty of Module;

RA = Module Reference Accuracy specified by the manufacturer;

CALCULATION	COMMENTS
DR = Drift of the module over a specific period; TE = Temperature Effect for the module; the effect of ambient temperature variations on module accuracy; the TE may be a normal operating TE or an accident TE, as required; RE = Radiation Effect for the module; the effect of radiation exposure on module accuracy; the RE may be a normal operating RE, an accident RE, or time of trip RE as required; SE = Seismic Effect or vibration effect for the module; the effect of seismic or operational vibration on the module accuracy; HE = Humidity Effect for the module; the effect of changes in ambient humidity on module accuracy, if any; SP = Static Pressure effects for the module; the effect of changes in process static pressure on module accuracy; MTE = Maintenance and Test Equipment effect for the module; this accounts for the uncertainties in the equipment utilized for calibration of the module; B = Biases associated with the module, if any.	
The justification for including/excluding each of the above parameters is as follows:	
PM: Effects are not applicable to this configuration/application.	See RP 6.2.5.
PE: Effects are not applicable to this configuration/application.	
SP: Effects are not applicable to this configuration/application.	See RP 6.2.3.
MTE: Term will be handled on a loop basis rather than on a module basis (based on Assumption 2.2).	See RP 6.2.6.
Others: Insulation Resistance Effects are not applicable to this configuration/application since the cables are outside containment and are not directly exposed to any harsh environment that is created when the transmitters are required to function.	See RP 6.2.10 and Appendix D.
Therefore, the Channel Uncertainty for this application is reduced from Eq. 1a and 1b to	<i>This application consists of only linear devices; if it contained any non-linear devices, a different equation would be required.</i>
$CU^+ = + [e_1^2 + e_2^2 + MTE^2]^{1/2} + B^+_T \quad (\text{Eq. 3a})$	
$CU^- = - [e_1^2 + e_2^2 + MTE^2]^{1/2} - B^-_T \quad (\text{Eq. 3b})$	

CALCULATION

COMMENTS

7.0 Determine uncertainty data

The following applies to the pressure transmitter (MS-01A-PT), and all appropriate terms will be designated with a subscript of ₁; i.e., e_1 , RA_1 , etc.

$$RA_1 = \pm 1\% \text{ of Span (based on References 3.7.a and b)}$$

See [RP 6.2.6](#).

$$DR_1 = \pm 0.1\% \text{ of Upper Range Limit (based on References 3.7.a and b)}$$

See [RP 6.2.7](#).

$$TE_1, RE_1, SE_1, \text{ and } HE_1 =$$

See [RP 6.2.2 and 6.2.4](#).

Specific values are not provided by the manufacturer in [Reference 3.8.a](#). However, [References 3.8.a and 3.10](#) have established a conservative value of $\pm 5\%$ of Upper Range Limit that includes all these effects for post-accident conditions. Pressure transmitters for this application are located outside containment ([Reference 3.6](#)) and, therefore, are not subjected to the in-containment environment when required to operate. However, the $\pm 5\%$ value has been included as a conservative factor to account for any possible environmental effects of the high energy line break inside containment effecting these transmitters in the auxiliary building. For this calculation, the term will be designated as EE_1 . Correspondence with the manufacturer ([Reference 3.11](#)) confirms that the manufacturer did test a sufficient number of samples to justify that the $\pm 5\%$ value is a random term.

See [RP 6.2.4, 6.3.1, and Appendix J](#).

In addition to the terms outlined in Eq. 2, the transmitter can be affected by loop power supply variations. Therefore, a term (PS_1) is required.

See [RP 6.2.8](#).

$$PS_1 = \pm 0.01\% \text{ span per volt variation (based on References 3.7.b and 3.8.a).}$$

Maximum voltage variation = ± 2 volts (based on [Reference 3.9](#)).

$$B_1^+, B_1^- = 0 \text{ (based on Assumption 2.1).}$$

$$\text{Therefore, } e_1 = \pm [RA_1^2 + DR_1^2 + EE_1^2 + PS_1^2]^{1/2} \quad (\text{Eq. 4})$$

based on [Reference 3.7.b](#), span = 0 - 75 psig
U.R.L. = 100 psig

$$\begin{aligned} e_1 &= \pm [(0.01 \times 75)^2 + (0.001 \times 100)^2 + (0.05 \times 100)^2 \\ &\quad + (0.0001 \times 2 \times 75)^2]^{1/2} \text{ psig} = \pm [25.57]^{1/2} \\ &= \pm 5.06 \approx \pm 5.1 \text{ psig} \end{aligned} \quad (\text{Eq. 5})$$

CALCULATION**COMMENTS**

The following applies to the bistable (MS-01A-PSL) and all appropriate terms will be designated with a subscript of ₂; i.e., e_2 , RA_2 , etc.

$$RA_2 = \pm 0.25\% \text{ of span (based on References 3.7.c and 3.9).}$$

$$DR_2 = \pm 0.25\% \text{ of span (based on References 3.7.a and 3.9).}$$

$$TE_2 = \pm 0.02\% \text{ span per } 100^\circ\text{F (based on Reference 3.9).}$$

Temperature Change = 50°F (based on Reference 3.3.b).

RE_2 , SE_2 , & HE_2 : Effects are not applicable to this module (based on module location and Reference 3.3.b).

In addition to the terms outlined in Eq. 2, this module can be affected by loop power supply variations. Therefore, a term (PS_2) is required.

$$PS_2 = \pm 0.01\% \text{ span per Volt Variation (based on Reference 3.9).}$$

Maximum Voltage Variation = ± 2 Volts (based on Reference 3.9).

$$\text{Therefore, } e_2 = \pm [RA_2^2 + DR_2^2 + TE_2^2 + PS_2^2]^{1/2} \quad (\text{Eq. 6})$$

based on References 3.7.b and c,

Span = 0 - 75 psig.

$$e_2 = \pm [(0.0025 \times 75)^2 + (0.0025 \times 75)^2 + (0.0002 \times \{50/100\} \times 75)^2 + (0.0001 \times 2 \times 75)^2]^{1/2} \text{ psig}$$

$$e_2 = \pm [0.071]^{1/2} = \pm 0.27 \approx \pm 0.3 \text{ psig} \quad (\text{Eq. 7})$$

8.0 Calculate instrument channel uncertainty

See [RP 6.3](#).

Based on the justification and data outlined in Section 7.0; i.e., $B_T^+ = 0$ and $B_T^- = 0$, the Channel Uncertainty equations (Eq. 3a and 3b) for this calculation become

$$CU = \pm [e_1^2 + e_2^2 + MTE^2]^{1/2} \quad (\text{Eq. 8})$$

$$e_1 = \pm 5.1 \text{ psig (From Eq. 5)} \quad e_2 = \pm 0.3 \text{ psig (From Eq. 7)}$$

$$MTE = \pm 0.5\%$$

$$\text{Span} = \pm (0.005 \times 75) = \pm 0.375 \approx \pm 0.4 \text{ psig} \quad (\text{Eq. 9})$$

$$CU = \pm [(5.1)^2 + (0.3)^2 + (0.4)^2]^{1/2}$$

$$= \pm [26.26]^{1/2} = \pm 5.12 \approx \pm 5.1 \text{ psig} \quad (\text{Eq. 10})$$

9.0 Obtain Analytical Limit (AL)

Per [References 3.7.b and c](#), the loop range is 0-75 psig.

See [RP Section 7.0](#)

Per [References 3.3.c and e](#), Steamline Isolation is assumed to occur at 25 psig.

CALCULATION

COMMENTS

10.0 Determine setpoint (TS)

A nominal trip setpoint can be calculated as follows:

$$TS = AL \pm (CU + \text{Margin})$$

A Margin of 1.0 psig will be used (based on [Reference 3.7.g](#)).

$$\text{Therefore, } TS = 25 - (5.1 + 1.0) = 18.9 \text{ psig} \quad (\text{Eq. 11})$$

(Note: The positive value of CU is not used to determine TS for an increasing parameter, since the process is increasing towards the analytical limit.)

11.0 Determine allowable value (AV)

The uncertainties to be included in determining the Allowable Value are defined in [Reference 3.4](#), Section 4.3.2. For this calculation, the only uncertainty that would be excluded from the CU are the uncertainties associated with design-basis events. However, as outlined in [Section 7.0](#) of this calculation, a specific TE (for the transmitter) is not available from the manufacturer. Therefore, a value of $TE_1 = \pm 1.0\%$ U.R.L. will be used to account for possible uncertainty due to temperature effects during normal operation.

Therefore, an Allowable Value Trip Setpoint Margin (AVTSM) can be calculated by modifying Eq. 4 to replace EE_1 with TE_1 and then combining the result with Eq. 7 and the MTE uncertainty.

$$e_m = e_1 \text{ (modified)} = \pm [RA_1^2 + DR_1^2 + TE_1^2 + PS_1^2]^{1/2} \quad (\text{Eq. 12})$$

$$= \pm [(0.01 \times 75)^2 + (0.001 \times 100)^2 + (0.01 \times 100)^2 + (0.0001 \times 2 \times 75)^2]^{1/2} \text{ psig}$$

$$= \pm [1.57]^{1/2} = \pm 1.25 \approx \pm 1.3 \text{ psig}$$

$$\text{AVTSM} = \pm [e_m^2 + e_2^2 + \text{MTE}^2]^{1/2} \quad (\text{Eq. 13})$$

$$= \pm [(1.3)^2 + (0.3)^2 + (0.4)^2]^{1/2} \text{ psig}$$

$$= \pm [1.94]^{1/2} = \pm 1.39 \approx \pm 1.4 \text{ psig}$$

Based on Eq. 11 and Eq. 13,

$$AV = TS \pm \text{AVTSM} = 18.9 + 1.4 = 20.3 \text{ psig.} \quad (\text{Eq. 14})$$

(Note: Only the positive value of AVTSM is used to determine AV for an increasing parameter.)

See [RP Section 7.0](#)

See [RP 7.2](#) & [Eq. 7.1](#).

Margin established as part of Interfaces discussed in [RP Section 9](#).

See [RP Section 7](#) and [Appendix I](#).

See [RP 7.3](#).

See [RP 7.3](#).

CALCULATION

COMMENTS

12.0 Check calculation

A check calculation will be performed to assure that the difference between the allowable value and analytical limit is still large enough to account for those uncertainties not included in the test and to ensure that the safety limit is not exceeded by a worst case design-basis event.

$$AVALM1 = (CU^2 - AVTSM^2)^{1/2}$$

$$AVALM2 = |(AL - TS)| - |AVTSM|$$

where

AVALM1 = The required margin between the analytical limit and the allowable value;

AVALM2 = The available margin between the analytical limit and the allowable value;

AVTSM = Allowable value trip setpoint margin;

CU = Channel uncertainty;

AL = Analytical limit;

TS = Nominal trip setpoint.

Based on Eq. 10 and Eq. 13

$$AVALM1 = [(5.1)^2 - (1.4)^2]^{1/2} \text{ psig} = [24.05]^{1/2} = 4.9 \text{ psig} \quad (\text{Eq. 15})$$

Based on [Section 9.0](#), Eq. 11, and Eq. 13,

$$AVALM2 = |(25-18.9)| - |(1.4)| \text{ psig} = 4.7 \text{ psig} \quad (\text{Eq. 16})$$

AVALM1 > AVALM2; therefore, TS and AV will be recalculated (adjusted) as follows:

$$AV_{adj} = AL - AVALM1 \quad (\text{Eq. 17})$$

$$TS_{adj} = AV_{adj} - AVTSM \quad (\text{Eq. 18})$$

See [RP 7.3](#).

If RP7.3 Method 3 is used, performing a check calculation is suggested to confirm that sufficient allowance exists between the AL and AV. This section of the calculation illustrates this technique. The RP recommends that this check calculation be performed if your AV is determined by using an arithmetic (versus an SRSS) approach. If your AV is determined by using an SRSS approach, the check calculation is not needed and is optional since it only increases the level of conservatism.

If AVALM1 > AVALM2, then the allowable value is adjusted accordingly. Also, if the AVTSM is small (i.e., does not allow a realistic allowance for instrument drift), the nominal trip setpoint may be conservatively adjusted to minimize the chance of a Licensing Event Report (LER).

CALCULATION**COMMENTS**

Based on [Section 9.0](#) and Eq. 15, Eq. 17 becomes

$$AV_{adj} = (25) - (4.9) \text{ psig} = 20.1 \text{ psig}$$

Based on Eq. 17 and Eq. 13, Eq. 18 becomes

$$TS_{adj} = (20.1) - (1.4) \text{ psig} = 18.7 \text{ psig} \quad (\text{Eq. 19})$$

13.0 Summary

Table 3.5-4 of [Reference 3.1](#) outlines the following values for Containment High Pressure Trip for Steamline Isolation Logic.

Trip Setpoint: 18.5 psig

Allowable Value: 20 psig

Therefore, the use of [Reference 3.2 and 3.4](#) methodology for the specific components being used at Nuclear Plant Unit #2 confirms that this installation is consistent with the Standard Tech Spec values, and use of the Standard Tech Spec setpoint and allowable values is conservative.

EXAMPLE CALCULATION — FLOW TRIP

CALCULATION	COMMENTS
1.0 Purpose To calculate a setpoint for the feedwater flow isolation trip. This calculation will support the installation of the components listed in Section 5 during the December 1990 refueling outage per Design Change Package 90-01. 2.0 Assumptions and clarifications 2.1 The calculation will assume all components perform as designed. This assumption leads to the following results: in a current loop series, components do not affect loop current, since current is constant at all points in a current loop. 2.2 In the operating ranges of interest (450° to 480°F and 400 to 450 psig) changes in water density due to changes in temperature and pressure are too small to affect channel accuracy. 2.3 Plant Procedure STD-0001, Methodology for Calculating Setpoints, is the basis for the uncertainty combinations and setpoint determinations in this calculation. 2.4 Drift is extended from the tested interval to the calibration interval using a SRSS technique, such that the drift is multiplied by the square root of the ratio of the calibration interval to the test interval. 2.5 Some manufacturer data is given in percent reading. This will be conservatively increased to percent full span to simplify the calculation, since in this application the process span is the same as the loop span. 2.6 The accuracy assigned to the flow element includes the effects of the installed piping configuration and effects of flow element degradation.	<i>NOTE: The following format is for illustrative purposes only. See RP Preface, Section 10, and Page 105.</i> <i>RP 5.2 and 5.3 were reviewed to identify potentially applicable factors.</i> <i>Addresses RP Appendix C concerns.</i> <i>Addresses RP/Appendix C concerns.</i>

CALCULATION**COMMENTS**

2.7 Reference accuracy is the accuracy of the component under reference (ideal) conditions. Calibration accuracy is the accuracy to which the component is calibrated. This calculation will use the largest of the two values.

2.8 All loop components are located in areas where the environments are not affected by any accident. Therefore, no IR or other harsh environment effects are applicable. Also, based on References 3.4 - 3.7 and 3.10, the normal operating environmental variations are within the components specification values.

3.0 References

3.1 Station Drawing 1234567 Rev 8

3.2 Calibration Procedure CAL-001 for FW-01-F Feedwater Flow Loop, Revision 2, dated 6/6/89

3.3 (flow orifice product literature)

3.4 (dP transmitter product literature)

3.5 (power supply product literature)

3.6 (square root extractor product literature)

3.7 (bistable product literature)

3.8 (pressure gauge product literature)

3.9 (DVM product literature)

3.10 (Environmental levels for instrument locations)

3.11 STD-0001, Methodology for Calculating Setpoints

3.12 FSAR Table 1.1, Feedwater System Design Criteria

3.13 FSAR Table 1.2, Vital Bus Design Criteria

3.14 Feedwater System Design Criteria Document, Revision 0

3.15 Change Notice 123, Feedwater Transmitter Replacement

Line Pressure Loss/Head Pressure effects addressed in [RP Appendix F](#) are not applicable since point of measurement and point of concern are the same, and the flow element is installed in a horizontal section of pipe (Based on [Reference 3.17](#)).

Insulation Resistance Effects addressed in [RP Appendix D](#) were determined not to be applicable based on [Reference 3.16](#).

CALCULATION

COMMENTS

3.16 Engineering Evaluation EQ-0012, Revision 3, Insulation Resistance Effects on Feedwater Flow Transmitters

3.17 Piping Drawing 1234567-1, Revision B

3.18 Master Setpoint List, Revision 43

4.0 Loop functional description

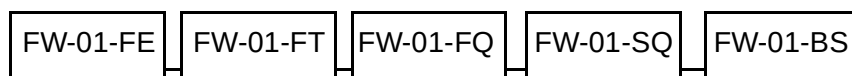
The feedwater flow isolation trip monitors feedwater flow by means of a flow orifice and dP transmitter. When flow exceeds a preset value, a feedwater line break is assumed to have occurred and feedwater line isolation is initiated.

5.0 Block Diagram

This calculation is being performed for the following components:

FW-01-FE	Flow Element
FW-01-FT	Flow Transmitter
FW-01-FQ	Loop Power Supply
FW-01-SQ	Square Root Extractor
FW-01-BS	Bistable

[Reference 3.1](#) shows the complete configuration summarized below.



6.0 Determine uncertainty equations

6.1 Loop uncertainty equations

Per [Reference 3.11](#), the loop uncertainty equation is developed by cascading the uncertainty equations of each module. The module uncertainty equations are to be developed from perturbation techniques. Therefore, use IN for "Input" and OUT for "Output."

For the Flow Element,

$$\text{OUT} = (\text{IN}/10)^2$$

$$\text{OUT} \pm \text{OUT (error)} = \{ [\text{IN} \pm \text{IN(error)}]/10 \}^2 \pm \text{FE (error)}$$

IN (error) for the flow element is 0, since the flow is the measured parameter.

$$\text{OUT(error)} = \pm \text{FE(error)}$$

See [RP 5.2](#) and [Figure 1](#).

See [RP 6.1](#).

See [RP 6.1](#).

CALCULATION	COMMENTS
For the dP Transmitter, $\text{OUT} = \text{IN}$ $\text{OUT} \pm \text{OUT (error)} = \text{IN} \pm \text{IN (error)} \pm \text{DP (error)}$ $\text{OUT (error)} = \pm \text{IN (error)} \pm \text{DP (error)}$ $= \pm \text{FE (error)} \pm \text{DP (error)}$ The square root extractor input MTE error will be carried as a separate term: SQ-IN-MTE (error) For the Square Root Extractor, $\text{OUT} = +10 * \text{SQRT} [\text{IN}]$ $\text{OUT} \pm \text{OUT(error)} = +10 * \text{SQRT} [\text{IN} \pm \text{IN (error)}]$ $\pm \text{SQ (error)}$ $\text{OUT(error)} = +\text{OUT} - 10 * \text{SQRT} [\text{IN} \pm \text{IN (error)}]$ $+ \text{SQ (error)}$ $= \text{OUT} - 10 * \text{SQRT} [\text{IN} \pm \text{FE (error)}]$ $\pm \text{DP (error)} \pm \text{SQ-IN-MTE (error)}$ $\pm \text{SQ (error)}$ Since for the Square Root Extractor $\text{OUT} = \text{FLOW} = 10 * \text{SQRT}[\text{DP}] \text{ and } \text{IN} = \text{DP},$ $\text{OUT (error)} = +10 * \text{SQRT} [\text{DP}] - 10 * \text{SQRT} [\text{DP} \pm \text{FE (error)} \pm \text{DP (error)}]$ $\pm \text{SQ-IN-MTE (error)} + \text{SQ (error)}$ For the analog portion of the Bistable, $\text{OUT} = +\text{SETPOINT} - \text{IN}$ $\text{OUT} \pm \text{OUT(error)} = +\text{SETPOINT} \pm \text{SETPOINT (error)}$ $- \text{IN} \pm \text{IN (error)} \pm \text{BISTABLE (error)}$ $\text{OUT(error)} = \pm \text{SETPOINT (error)}$ $\pm \text{IN (error)} \pm \text{BISTABLE (error)}$ $= \pm \text{SETPOINT (error)} + 10 * \text{SQRT}[\text{DP}]$ $- 10 * \text{SQRT} [\text{DP} \pm \text{FE (error)} \pm \text{DP (error)}]$ $\pm \text{SQ-IN-MTE (error)}] \pm \text{SQ (error)}$ $\pm \text{BISTABLE (error)}$	See RP 6.3.1.

CALCULATION**COMMENTS**

Since the bistable is the last loop element, the bistable output uncertainty is the loop uncertainty.

$$\begin{aligned} \text{CAVU} &= \pm \text{SETPOINT (error)} \\ &\pm (10 * \text{SQRT [DP]} \\ &- 10 * \text{SQRT [DP} \pm \text{FE (error)} \pm \text{DP (error)]}) \\ &\pm \text{SQ (error)} \pm \text{BISTABLE (error)} \end{aligned}$$

See [RP 6.1](#), Eq. 6.1; and 6.3, Eq. 6.10 a & b.

Per [Reference 3.11](#), the random part of these terms may be combined by a SRSS technique, while the non-random part of these terms must be combined linearly. Therefore, both random and non-random components of each term will be determined.

6.2 Module Uncertainty Equations

Per [Reference 3.11](#), the module uncertainty will address accuracy, ambient temperature effects, power supply variation effects, drift, and measurement and test equipment inaccuracy. In addition, module-unique effects should also be addressed.

Again, the random part of these terms may be combined by a SRSS technique, while the non-random part of these terms must be combined linearly. Therefore, both random and non-random components of each term will be determined.

7.0 Determine Uncertainty Data**7.1 Flow Element**

Tag Number:	FW-01-FE	Reference 3.1
Manufacturer:	Ozzie Orifice Company	Reference 3.3
Model:	ORF-001	
Reference Accuracy:	± 1.0 % of dp	Reference 3.3
Temperature Effect:	0	Assumption 2.2
Pressure Effect:	0	Assumption 2.2
Power Supply Effect:	n/a	
Drift:	n/a	
M&TE:	n/a	

See [RP 6.2](#).

Since there is only one non-zero term, FE (error) = ± 1.0 % span

7.2 Flow Transmitter

Tag Number:	FW-01-FT	Reference 3.1
Manufacturer:	Tommy Transmitter Co.	Reference 3.4
Model:	FT-001	
Upper Range Limit:	1000 inches H ₂ O	Reference 3.4
Span:	800 inches H ₂ O	Reference 3.2

See [RP 6.2.6](#).

CALCULATION			COMMENTS
Calibration Accuracy:	± 0.50 % span	Reference 3.2	See <i>RP 6.2.2 & 6.2.4.</i>
Reference Accuracy:	± 0.25 % span	Reference 3.4	
Temperature Effect:	± 0.75 % URL / 100°F	Reference 3.4	
Temperature Variation:	± 55 °F	Reference 3.10	
Temperature Effect:	$\pm [(0.75) (1000/800) (55/100)]$		See <i>RP 6.2.3.</i>
Temperature Effect:	± 0.52 % span		
Pressure Effect:	± 0.20 % URL / 1000 psi	Reference 3.4	
System Pressure:	425 psig	Reference 3.12	
Pressure Effect:	$\pm (0.2) (1000/800) (425/1000)$		See <i>RP 6.2.8.</i>
Pressure Effect:	± 0.11 % span		
Power Supply Effect:	± 0.005 % span per volt	Reference 3.4	
Voltage Variation:	± 1.0 volt	Reference 3.5	
Power Supply Effect:	(0.005) (1)		See <i>RP 6.2.7.</i>
Power Supply Effect:	± 0.005 % span		
Drift:	± 0.20 % URL / 6 months	Reference 3.4	
Drift:	$\pm (0.20) (1000/800) / 6$ months		
Drift:	± 0.250 % span / 6 months		See <i>RP 6.2.7.</i>
Cal Frequency:	18 months	Reference 3.2	
Drift:	$\pm 0.250 * \text{SQRT} [18/6]$		
Drift:	± 0.433 % span		
M&TE:	$\text{SQRT} [\text{Gage Error}^2 + \text{DVM Error}^2]$		<i>M&TE uncertainties of gage and I assumed random.</i>
Gage Error:	± 0.1 % gage span	Reference 3.8	See <i>RP 6.2.6.</i>
Gage Span:	1000 inches H ₂ O	Reference 3.8	
Gage Error:	$\pm (0.1) (1000/800)$		
Gage Error:	± 0.125 % span		
DVM Error:	± 0.02 % reading	Reference 3.9	
DVM Error:	± 0.02 % span	Assumption 2.5	
M&TE:	$\text{SQRT} [(0.125)^2 + (0.02)^2]$		
M&TE:	± 0.127 % span		
Since all the uncertainties are random, they can be combined by SRSS:			
$\text{DP (error)} = \pm \text{SQRT} [(0.5)^2 + (0.52)^2 + (0.11)^2 + (0.005)^2 + (0.433)^2 + (0.127)^2]$			
DP (error) = ± 0.858 % span			

CALCULATION**COMMENTS****7.3 Square root extractor input mte error**

M&TE:

Input DVM Error: ± 0.02 % span [Reference 3.9](#)Input DVM Range: 20 volts [Reference 3.9](#)Input: 5 volts [Reference 3.2](#)Input DVM Error: $\pm (.02)$ (20/5)Input DVM Error: ± 0.08 % span**7.4 Square root extractor**Tag Number: FW-01-SQ [Reference 3.1](#)Manufacturer: Sammie SQRT Company [Reference 3.6](#)

Model: SQRT-001

Calibration Accuracy: ± 0.65 % span [Reference 3.2](#)Reference Accuracy: ± 0.50 % span [Reference 3.6](#)Temperature Effect: $\pm 0.05\%$ span per 100°F [Reference 3.6](#)Temperature Variation: $\pm 20^\circ\text{F}$ [Reference 3.10](#)Temperature Effect: $\pm (.05)$ (20/100)Temperature Effect: ± 0.01 % span

Pressure Effect: n/a

Power Supply Effect: ± 0.002 % span per % variation[Reference 3.6](#)Voltage Variation: 118 ± 2 vac[Reference 3.13](#)Voltage Variation: ± 1.7 %Power Supply Effect: $\pm (.002)$ (1.7)Power Supply Effect: ± 0.004 % span*Final value of 0.004% is conservative round-off of actual value of 0.0034%.*Drift: ± 0.5 % per 18 months [Reference 3.6](#)Cal Frequency: 18 months [Reference 3.2](#)Drift: ± 0.5 % spanOutput DVM Error: ± 0.02 % span [Reference 3.9](#)Output DVM Range: 20 volts [Reference 3.9](#)Output: 10 volts [Reference 3.2](#)Output DVM Error: $\pm (.02)$ (20/10)Output DVM Error: ± 0.04 % span

Since all the uncertainties are random, they can be combined by SRSS.

$$\text{SQ(error)} = \pm \text{SQRT} [(0.65)^2 + (0.01)^2 + (0.004)^2 + (0.5)^2 + (0.04)^2]$$

$$\text{SQ(error)} = \pm 0.821 \text{ % span}$$

CALCULATION**COMMENTS****7.5 Bistable**

Tag Number: FW-01-BS [Reference 3.1](#)
Manufacturer: Billie Bistable Company [Reference 3.7](#)
Model: BIS-001

Calibration Accuracy: ± 0.1 % span [Reference 3.2](#)
Reference Accuracy: ± 0.1 % span [Reference 3.7](#)

Temperature Effect: $\pm 0.02\%$ span per 100°F [Reference 3.7](#)
Temperature Variation: $\pm 20^\circ\text{F}$ [Reference 3.10](#)

Temperature Effect: $\pm (.02)$ (20/100)
Temperature Effect: ± 0.004 % span

Pressure Effect: n/a

Power Supply Effect: ± 0.001 % span per % variation [Reference 3.7](#)
Voltage Variation: 118 ± 2 vac [Reference 3.13](#)

Voltage Variation: $\pm 1.7\%$
Power Supply Effect: $\pm (.001)$ (1.7)
Power Supply Effect: ± 0.002 % span

Drift: ± 0.25 % per 18 months [Reference 3.6](#)
Cal Frequency: 18 months [Reference 3.2](#)
Drift: ± 0.25 % span

Input M&TE: Input DVM Error
Input DVM Error: ± 0.02 % span [Reference 3.9](#)
Input DVM Range: 20 volts [Reference 3.9](#)
Input: 10 volts [Reference 3.2](#)
Input DVM Error: $\pm (.02)$ (20/10)
Input M&TE Error: ± 0.04 % span

Since all the uncertainties are random, they can be combined by SRSS.

$$\text{BISTABLE (error)} = \pm \text{SQRT}[(0.1)^2 + (0.004)^2 + (0.002)^2 + (0.25)^2 + (0.04)^2]$$

$$\text{BISTABLE (error)} = \pm 0.272 \text{ % span}$$

7.6 Bistable setpoint

Calibration Accuracy: ± 0.10 % span
Reference Accuracy: ± 0.05 % span

Temperature Effect: (included in bistable error)

Pressure Effect: n/a

Power Supply Effect: (included in bistable error)

CALCULATION**COMMENTS**

Stability (Drift): ± 0.02 % span/18 months [Reference 3.7](#)
 Calibration Period: 18 months [Reference 3.2](#)
 Stability: ± 0.02 % span
 M&TE Error: Setpoint DVM Error
 DVM Error: ± 0.02 % input [Reference 3.9](#)
 DVM Range: 20 volts [Reference 3.9](#)
 Stpt Range: 10 volts [Reference 3.2](#)
 M&TE Error: $\pm (.02)$ (20/10)
 M&TE Error: ± 0.04 % span

Since all the uncertainties are random, they can be combined by SRSS.

$$\text{SETPOINT (error)} = \pm \text{SQRT} [(0.1)^2 + (0.02)^2 + (0.04)^2]$$

$$\text{SETPOINT (error)} = \pm 0.110 \text{ % span}$$

8.0 Calculate instrument channel uncertainty

See [RP 6.3](#).

From [Section 7.0](#):

FE(error) = ± 1.000 % span
 DP(error) = ± 0.858 % span
 SQ-IN-MTE (error) = ± 0.08 % span
 SQ(error) = ± 0.829 % span
 BISTABLE(error) = ± 0.272 % span
 SETPOINT(error) = ± 0.110 % span

From [Section 6.0](#):

$$\begin{aligned} \text{CAVU} = & \pm \text{SETPOINT (error)} + 10 * \text{SQRT [DP]} \\ & - 10 * \text{SQRT [DP } \pm \text{ FE (error) } \pm \text{ DP (error) } \\ & \pm \text{ SQ-IN-MTE (error)] } \pm \text{ SQ (error) } \\ & \pm \text{ BISTABLE (error) } \end{aligned}$$

Since the four terms

- (1) SETPOINT (error);
- (2) $10 * \text{SQRT [DP]} - 10 * \text{SQRT [DP } \pm \text{ FE (error) } \pm \text{ DP (error) } \pm \text{ SQ-IN-MTE (error)]}$;
- (3) SQ(error); and
- (4) BISTABLE (error)

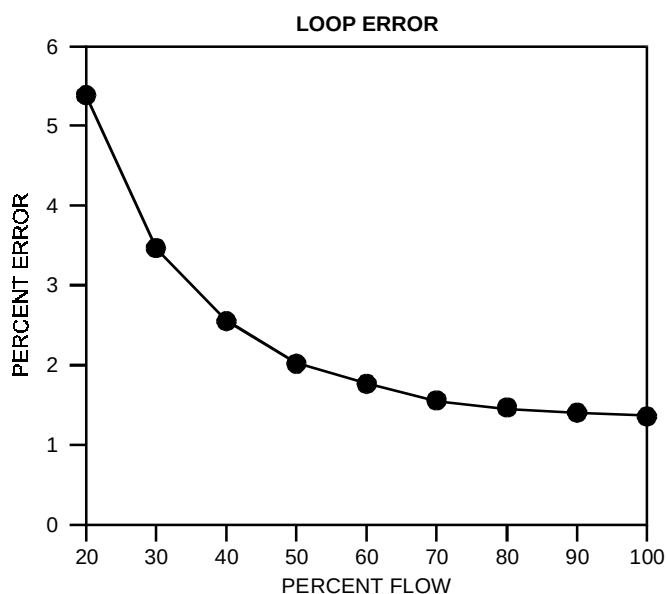
are random and independent, they can be combined by an SRSS technique per [Reference 3.11](#). For conservatism, FE (error), DP (error), and SQ-IN-MTE (error) will be added, although they could also be combined by an SRSS technique.

CALCULATION**COMMENTS**

Showing only the results of worst case choices of sign in the second term and recalling that $dp = (\text{flow}/10)^2$, for various values of input flow

XMTR INPUT (FLOW)	XMTR OUTPUT (DP)	LOOP ERROR
% FLOW SPAN	% DP SPAN	% FLOW SPAN
20	4	5.708
30	9	3.537
40	16	2.651
50	25	2.164
60	36	1.859
70	49	1.652
80	64	1.504
90	81	1.395
100	100	1.312

This data describes an uncertainty that varies as flow varies, as expected for a non-linear element. Specifically, the uncertainty increases as flow decreases. Therefore, the uncertainty at the point of interest must be used in determining the setpoint.



CALCULATION**COMMENTS****9.0 Obtain analytical limit**

Per [Reference 3.2](#), the loop range is 0 - 8000 gpm.

Per [Reference 3.14](#), the maximum required feedwater flow during normal operation is 5000 gpm, and the maximum required feedwater flow during abnormal events and transients is 6500 gpm.

Per [Reference 3.14](#), the pump run out flow rate (to atmosphere) is 8000 gpm.

See [RP Section 7](#).

10.0 Determine setpoint

6500 gpm is approximately 80% flow. From the above, the loop uncertainty at 80% flow is approximately ± 1.5 % span or 120 gpm.

Minimum setpoint is 6500 gpm + 120 gpm = 6620 gpm.

8000 gpm is 100% flow. From the above, the loop uncertainty at 100% flow is approximately ± 1.3 % span or 104 gpm.

Maximum setpoint is 8000 gpm - 104 gpm = 7896 gpm.

Per [Reference 3.18](#), the existing in-plant setpoint is 7500 gpm. This is within the minimum and maximum bounds. Therefore, no change to the existing setpoint of 7500 gpm is recommended.

See [RP Section 7 and Appendix I](#).

11.0 Determine allowable value

Per [Reference 3.11](#), the allowable value is an estimate of loop performance including accuracy, drift, normal environmental effects, and M&TE, but not including harsh environmental effects. For this application, the allowable value will include accuracy, power supply effects, drift, and M&TE effects. Temperature and pressure are assumed to be at or very near calibration conditions.

The loop uncertainty equation does not change.

$$\begin{aligned} \text{CAVU} = & \pm \text{SETPOINT (error)} \\ & \pm (10 * \text{SQRT [DP]} - 10 * \text{SQRT [DP } \pm \text{ FE (error)} \\ & \pm \text{ DP (error)] }) \pm \text{SQ (error)} \pm \text{BISTABLE (error)} \end{aligned}$$

The module uncertainties become

FE (error)	=	± 1.000 % span
DP (error)	=	± 0.674 % span
SQ-IN-MTE (error)	=	± 0.08 % span
SQ (error)	=	± 0.829 % span
BISTABLE (error)	=	± 0.272 % span
SETPOINT (error)	=	± 0.110 % span

CALCULATION**COMMENTS**

Again, an SRSS technique can be used. The loop allowable values are

XMTR INPUT (FLOW)	XMTR OUTPUT (DP)	LOOP ERROR
% FLOW SPAN	% DP SPAN	% FLOW SPAN
20	4	5.090
30	9	3.205
40	16	2.421
50	25	1.991
60	36	1.721
70	49	1.540
80	64	1.411
90	81	1.317
100	100	1.245

$$\begin{aligned}AV &= TS \pm CAVU \\&= 7500 \pm 1.245\% \\&= 7500 \pm 100 \\&= 7600, 7400 \text{ gpm}\end{aligned}$$

12.0 Summary

The feedwater flow isolation trip has a channel uncertainty that varies inversely with flow, approximately equal to

$$\begin{aligned}&\pm 105 \text{ gpm at } 8000 \text{ gpm,} \\&\pm 173 \text{ gpm at } 4000 \text{ gpm,}\end{aligned}$$

and continuing to increase below 4000 gpm.

The feedwater isolation trip setpoint has a fairly broad range of acceptable values, bounded by 6620 gpm on the low side and 7896 gpm on the high side. The existing setpoint value of 7500 gpm is adequate and should be retained. The allowable values for the setpoint of 7500 gpm are 7400 gpm and 7600 gpm.

Consistent with approach outlined in [RP 7.3](#), Method 3.

EXAMPLE CALCULATION - LEVEL TRIP

CALCULATION	COMMENTS
1.0 Purpose This calculation will determine the instrumentation loop accuracies for the temperature-compensated pressurizer level reactor trip. This trip is required to operate for the first 15 minutes of a design-basis Main Stream Line Break (MSLB). 2.0 Assumptions 2.1 The safety analyses show that the MSLB will produce little or no core damage. Therefore, the total integrated radiation dose to the cables and pressure transmitters in the first fifteen minutes will be small and will not affect their performance in this application. 2.2 Based on analyses contained in Reference 3.1, the pressurizer remains at saturation conditions throughout the MSLB accident scenario. 2.3 M&TE errors are bounded by plant requirements to be no greater than one-quarter (1/4) of the reference accuracy of the equipment being tested. 2.4 Loop power supply is regulated to maintain voltage within the most limiting loop device's limitations. 2.5 There are no known dependencies between loop component error contributions. Therefore, all random uncertainties are treated as statistically independent. 2.6 Based on Reference 3.13: a. Effects of vessel growth/contraction due to temperature changes are not included as they are estimated to be insignificant to this application. b. Changes in height of the reference leg due to vessel growth contraction are not included as they are estimated to be insignificant to this application. 3.0 References 3.1 East Fork Nuclear Generating Station UFSAR, Amendment 53. 3.2 East Fork Nuclear Generating Station Technical Specifications, Revision 12.	<i>NOTE: The following format is for illustrative purposes only. See RP Preface, Section 10, and Page 105.</i> <i>RP 5.3 was reviewed to identify potentially applicable design parameters and sources of uncertainty.</i> <i>See RP 6.2.6.</i>

CALCULATION	COMMENTS
3.3 East Fork Nuclear Generating Station Drawings Control Loop Diagram RC-L001A, Revision 01 Process Protection Cable 1 1974-1000, Sheet 1, Revision 16 Process Instrument Cable 1 1974-1001, Sheet 2, Revision 11 Process Protection Cable 2 1974-1002, Sheet 1, Revision 13 Process Instrument Cable 2 1974-1003, Sheet 1, Revision 11 RCS Flow Diagram 1974-G-1020, Revision 27 Pressurizer Level Control Wiring Diagram B100-009, Revision 10 Pressurizer Level Control Wiring Diagram B100-010, Revision 13 Pressurizer Level Control Wiring Diagram B100-011, Revision 09 3.4 Delta-P Instrument Technical Manual #456789, Revision 2 3.5 ACME Engineering Specification for Class IE Transmitters, 1974-S395.15 3.6 ACME Engineering Specification for Process Analog Control System, 1974-S349.10 3.7 Instrument List, 1974-IL459, Revision 32 3.8 NSSS Owner's Group Report No. 0100, 100-101-3595, Revision 4 3.9 Cable Insulation Resistance Degradation Calculation EC-425-85, Revision 0 3.10 Pressurizer Level Transmitter Calibration Data Analysis 1974-6896, Revision 0 3.11 ANSI/ISA-S67.04, Setpoints for Nuclear Safety-Related Instrumentation, 1987 3.12 ISA-67.04, Part II, Methodologies for the Determination of Setpoints for Nuclear Safety-Related Instrumentation 3.13 RCS Measurement Channel Uncertainties Analysis, 1974-6867, Revision 00 4.0 Design Input Data 4.1 The Process Analog Control System cabinet components calibration uncertainty is ± 2.5 % span based on a calibration tolerance of ± 0.10 volts and a span of 4 volts. (Reference 3.8)	

CALCULATION**COMMENTS**

4.2 The Process Analog Control System bistable drift is $\pm 0.227\%$ span for 39 days, based on a maximum expected drift of ± 0.007 volts for 30 days, a linear extrapolation to 39 days, and a span of 4 volts. ([Reference 3.8](#))

4.3 A seismic event coincident with a MSLB is not within the design basis for this plant. ([Reference 3.1](#))

4.4 Throughout this calculation, the terms "error" and "uncertainty" are used interchangeably.

4.5 Normal operation conditions are

Pressurizer Level - 120 to 180 inches

Pressurizer Temperature - 650°F

Pressurizer Press - 2200 psia

RCS Tavg - 600°F

During the first fifteen minutes of MSLB, the primary system conditions will be bounded by

Pressurizer Level - 50 to 250 inches

Pressurizer Temperature - 250° to 700°F

Pressurizer Press - 30 to 2500 psia

RCS Tavg - 200° to 600°F

(See [Reference 3.1](#), Chapter 15.)

4.6 The Pressurizer Level Transmitter is calibrated to read level at saturation conditions of 2200 psia, 650°F. The compensation function generator produces a correction factor that approximates the ratio of the saturated water density at calibration conditions to the saturated water density at actual conditions. Therefore, the correction factor varies as follows:

PRESSURIZER TEMPERATURE	CALIBRATION DENSITY	ACTUAL DENSITY	CORRECTION FACTOR
700	37.40	27.05	1.38
650	37.40	37.40	1.00
550	37.40	45.96	0.81
450	37.40	51.47	0.73
350	37.40	55.59	0.67
250	37.40	58.80	0.64

These conditions envelop the conditions of interest for this calculation. ([Reference 3.1](#))

4.7 Process Measurement (PM) errors for the Pressurizer Level Transmitter arise due to two causes:

- 1) the change in steam water density due to static pressure changes during a MSLB; and

See [RP Appendix B](#).

See [RP Appendix B](#).

CALCULATION

COMMENTS

2) changes in reference leg density due to the reference leg heatup during a MSLB.

The change in static pressure during a MSLB. As noted above, Pressurizer pressure can shift from its nominal value of 2200 psia up to 2500 psia and down to 30 psia. These maximum changes of +300 psia and -2170 psia will cause errors of -0.15% process span and a +1.08% process span, respectively.

The reference leg heatup during the first 15 minutes of a MSLB will cause a +2.85% span error. ([Reference 3.13](#))

Therefore, the PM for the Pressurizer Level Transmitter is +3.93% span, -0.15% span.

$$PM_P = (+1.08 + 2.85) \text{ percent process span}$$

$$PM_N = -0.15\% \text{ process span}$$

4.8 PM error for the Pressurizer temperature RTD arises from temperature stratification in the pressurizer. To compensate for this effect, the Pressurizer temperature RTD was located at 80 inches, approximately halfway up the normal water column. Due to the dynamic changes occurring in the pressurizer because of pressure changes and temperature changes throughout the RCS, PM for the Pressurizer temperature RTD will be set to 0.0% span. ([Reference 3.13](#))

5.0 Functional block diagram

See [RP 5.2](#) and [Figure 1](#).

5.1 Per [References 3.3](#) and [3.4](#), this calculation applies to the following channels:

	<u>Train A</u>	<u>Train B</u>
Module 1	RC-LT-100A	RC-LT-100B
Cable 2	243459	243423
Module 3	RC-XFUN-100A	RC-XFUN-100B
Module 4	RC-LA200A	RC-LA200B
Module 5	RC-TE-100A	RC-TE-100B
Cable 6	243462	243407
Module 7	RC-TT-100A	RC-TT-100B
Module 8	RC-XFUN-101A	RC-XFUN-101B

Note: Each module is given a number for later reference.

CALCULATION

COMMENTS

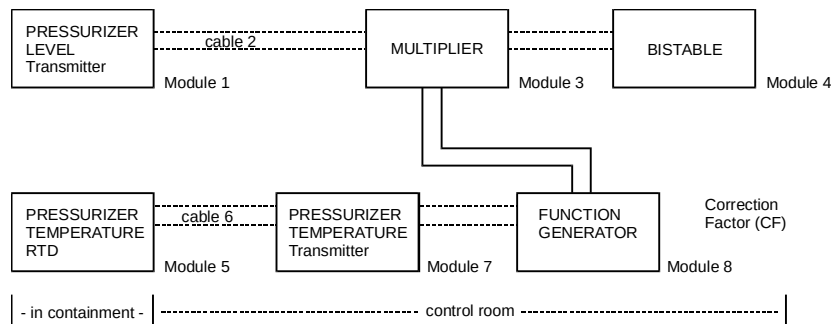
5.2 The temperature-compensated pressurizer level signal is developed by measuring pressurizer level (0 to 300 inches H₂O span) and compensating for density changes. The compensation factor is based on pressurizer temperature (250-700°F span).

5.3 When the compensated level (CL) signal is less than the level setpoint, a reactor trip is initiated. (CL = CF * Level)

5.4 All loop components except the level transmitter (LT) and temperature element (TE) are installed in environmentally mild locations.

5.5 Cables 2 and 6 are routed through environmentally harsh locations as described in [Reference 3.9](#).

Functional Block Diagram



6.0 Develop uncertainty equations

Linear error equations will be developed for the entire channel. The possibilities for statistical combination or error terms will be discussed later. The term "e" will be used to denote errors. The "e" will be followed by one or more numbers or letters that refer to the module and cable numbers and letters given in Section 5.0. Multiple numbers and letters will indicate that the error listed encompasses several modules or cables.

6.1 Level input to multiplier

The Pressurizer Level Transmitter and cable are linear devices, so their errors add linearly.

$$e_{12} = + e_1 + e_2 \quad (\text{Eq. 1})$$

See [RP 6.1](#) and [6.3](#).

The decision on applicability (or non-applicability) for treating each module as a linear device is an important factor on which equations are appropriate. See [RP 6.3.1](#) and [6.2.11](#).

CALCULATION**COMMENTS****6.2 Pressurizer temperature input to function generator #1**

The Pressurizer temperature RTD, cable, and Pressurizer temperature transmitter are linear devices, so their errors add linearly

$$e_{567} = + e_5 + e_6 + e_7 \quad (\text{Eq. 2})$$

While temperature devices may not be "pure" linear devices, they are often sufficiently linear over the area of interest to allow the temperature devices to be treated as "linear."

6.3 Function generator #1 input to multiplier

Function Generator #1 is a non-linear device that converts temperature to a correction factor. This will effectively multiply the temperature error by the slope of the correction factor curve at the point of interest.

$$e_{5678} = + \text{slope} * (e_{567}) + e_8 \quad (\text{Eq. 3})$$

Per Section 4.5, the slope changes with actual temperature, so the error of the function generator output also changes with slope.

See [RP 6.3.1](#), [Table 1](#), and [Appendix K](#).

6.4 Multiplier output

The multiplier is a non-linear device. Per [Reference 3.12](#), Table 6-1, the output error is

$$e_{1235678} = (\text{LEVEL} * e_{5678}) + (\text{CF} * e_{12}) + (e_{5678} * e_{12}) + e_3 \quad (\text{Eq. 4})$$

where LEVEL is the uncompensated level, and CF is the actual correction factor. [Reference 3.12](#) also notes that the third term, consisting of the product of two very small numbers, is insignificantly small and may be neglected. Therefore

See [RP Appendix K](#) (Eq. K-15, K-16).

$$e_{1235678} = (\text{LEVEL} * e_{5678}) + (\text{CF} * e_{12}) + e_3 \quad (\text{Eq. 5})$$

6.5 Bistable output error

The analog portion of the bistable compares the multiplier output to a fixed setpoint.

$$e_{12345678} = + e_{1235678} * e_4 \quad (\text{Eq. 6})$$

6.6 Channel uncertainty

The channel uncertainty, CU, is the bistable output error.

$$\text{CU} = e_{12345678} \quad (\text{Eq. 7})$$

This is an alternative representation to RP Equations 6.10 a & b.

CALCULATION**COMMENTS**

Combining terms from [Sections 6.1 through 6.5](#) yields

$$\begin{aligned} \text{CU} = & + \text{LEVEL} * [\text{slope} * (\text{e5} + \text{e6} + \text{e7}) + \text{e8}] \\ & + \text{CF} * (\text{e1} + \text{e2}) + \text{e3} + \text{e4} \end{aligned} \quad (\text{Eq. 8})$$

6.7 Statistical combination of channel uncertainties

Each of the error terms in [Section 6.6](#) potentially consists of random and non-random (bias) parts. Random parts may be combined statistically to account for the low probability that all random errors will peak at the same time. Per [Reference 3.12](#), a square-root-sum-of-the-squares, or SRSS, technique is appropriate.

The following convention will be used: random errors will be subscripted with an "R"; positive bias errors will be subscripted with a "P"; and negative bias errors will be subscripted with an "N".

Therefore

e1_R is the random part of the Pressurizer Level Transmitter error.

e1_P is the positive bias part of the Pressurizer Level Transmitter error.

e1_N is the negative bias part of the Pressurizer Level Transmitter error.

Using this convention, the random channel uncertainty becomes

$$\begin{aligned} \text{CU}_R^2 = & + [\text{LEVEL} * \text{slope} * (\text{e5}_R + \text{e6}_R + \text{e7}_R)]^2 \\ & + (\text{LEVEL} * \text{e8}_R)^2 \\ & + [\text{CF} * (\text{e1}_R + \text{e2}_R)]^2 + \text{e3}_R^2 + \text{e4}_R^2 \end{aligned} \quad (\text{Eq. 9})$$

Similarly, the positive bias channel uncertainty becomes

$$\begin{aligned} \text{CU}_P = & + \text{LEVEL} * \text{slope} * (\text{e5}_P + \text{e6}_P + \text{e7}_P) \\ & + \text{LEVEL} * \text{e8}_P \\ & + \text{CF} * (\text{e1}_P + \text{e2}_P) + \text{e3}_P + \text{e4}_P \end{aligned} \quad (\text{Eq. 10})$$

And the negative bias channel uncertainty becomes

$$\begin{aligned} \text{CU}_N = & - \text{LEVEL} * \text{slope} * (\text{e5}_N + \text{e6}_N + \text{e7}_N) \\ & - \text{LEVEL} * \text{e8}_N \\ & - \text{CF} * (\text{e1}_N + \text{e2}_N - \text{e3}_N - \text{e4}_N) \end{aligned} \quad (\text{Eq. 11})$$

The multiplication of random and bias uncertainties in module 3 produces additional compound random terms. Since these terms are the product of two small numbers, they themselves are smaller and insignificant. Using this approximation allows propagating the random and bias uncertainties independently until final summation. See [RP Appendix K](#) and Equations K-27 and K-28.

This is an alternative representation to RP Equations 6.10 a & b.

CALCULATION**COMMENTS****7.0 Determine uncertainty data**See [RP 6.2](#).**7.1 Module uncertainties**

The following uncertainty components will be addressed:

PM = Process Measurement effects.

Note: PM applies to the primary element only.

RA = Module Reference Accuracy specified by the manufacturer.

DR = Drift of the module over a specific time period.

TE = Temperature effect for the module. Although the temperature effects occur due to a common cause, they are random in sign and magnitude and are therefore considered independent.

MTE = Measurement and Test Equipment effect. [See 4.3.3](#).

MSLBE = Main Stream Line Break Effect.

Radiation effect will not be addressed per Assumption 2.1.

Seismic effect will not be addressed per 4.3.

Changes in static pressure do not affect any equipment in this channel and will not be addressed further.

The effects of changes in power supply voltages have been accounted for in module reference accuracy and will not be addressed separately.

There are no primary element effects since no separate primary elements are used in this channel.

Therefore, the module error equation to be used is

$$e = PM + RA + DR + TE + MTE + MSLBE \quad (\text{Eq. 12})$$

As discussed under the channel uncertainty, these terms may contain both random and bias parts. The random parts of these terms may be combined using an SRSS technique, while the bias parts must be combined in accordance with their sign. Using the same sign conventions as above, this results in the following three equations:

$$e_R^2 = + PM^2 + RA_R^2 + DR_R^2 + TE_R^2 + MTE_R^2 + MSLBE_R^2 \quad (\text{Eq. 13})$$

$$e_P = + PM_P + RA_P + DR_P + TE_P + MTE_P + MSLBE_P \quad (\text{Eq. 14})$$

$$e_N = + PM_N + RA_N + DR_N + TE_N + MTE_N + MSLBE_N \quad (\text{Eq. 15})$$

CALCULATION**COMMENTS****7.2 Pressurizer level transmitter - Module 1**

PM = -0.15% span, +3.93% span
RA = ±0.25% span

Section 4.7
Reference 3.4, 3.6

This application requires treating the transmitter channel as a "direct-acting" signal. This may not always be appropriate; i.e., as many applications would require compensation for a "reverse-acting" signal.

Reference Accuracy (RA) value, in this application, includes a "Setting Tolerance."

DR = ±1.10% span
TE = ±0.30% span
MTE = ±0.06% span
MSLBE = +6.80% span

Reference 3.10
Reference 3.4, 3.6
Section 2.3
Reference 3.4, 3.6

Therefore, the module errors are

$$e1_R = [0.25^2 + 1.1^2 + 0.3^2 + 0.06^2]^{1/2} \\ = \pm 1.17\% \text{ span}$$

$$e1_P = +3.93 + 6.80 \\ = +10.73\% \text{ span}$$

$$e1_N = -0.15\% \text{ span}$$

7.3 Level transmitter to multiplier cable - Module 2

PM = N/A
RA = N/A
DR = N/A
TE = N/A
MTE = N/A
MSLBE = +0.98% span

Reference 3.9

See RP 6.2.10 and Appendix D.

Therefore, the module errors are

$$e2_R = \pm 0.0\% \text{ span}$$

$$e2_P = \pm 0.98\% \text{ span}$$

$$e2_N = \pm 0.0\% \text{ span}$$

7.4 Multiplier - Module 3

PM = N/A
RA = ±0.10% span
DR = ±0.30% span
TE = ±0.03% span
MTE = ±0.025% span
MSLBE = N/A

Reference 3.6
Reference 3.6
Reference 3.6
Section 2.3

CALCULATION**COMMENTS**

Therefore, the module errors are

$$\begin{aligned} e_{3R} &= \pm[0.10^2 + 0.30^2 + 0.03^2 + 0.025^2]^{1/2} \\ &= \pm 0.32\% \text{ span} \end{aligned}$$

$$e_{3P} = \pm 0.0\% \text{ span}$$

$$e_{3N} = \pm 0.0\% \text{ span}$$

7.5 Bistable - Module 4

$$PM = \text{N/A}$$

$$RA = \pm 0.15\% \text{ span}$$

[Reference 3.6](#)

$$DR = \pm 0.227\% \text{ span}$$

Section 4.2

$$TE = \pm 0.03\% \text{ span}$$

[Reference 3.6](#)

$$MTE = \pm 0.04\% \text{ span}$$

Section 2.3

$$MSLBE = \text{N/A}$$

Therefore, the module errors are

$$\begin{aligned} e_{4R} &= \pm[0.15^2 + 0.227^2 + 0.03^2 + 0.04^2]^{1/2} \\ &= \pm 0.28\% \text{ span} \end{aligned}$$

$$e_{4P} = +0.0\% \text{ span}$$

$$e_{4N} = -0.0\% \text{ span}$$

7.6 Pressurizer temperature RTD - Module 5

$$PM = \text{N/A}$$

Section 4.8

$$RA = \pm 0.15\% \text{ span}$$

[Reference 3.8](#)

$$DR = \pm 0.75\% \text{ span}$$

[Reference 3.8](#)

$$TE = \text{N/A}$$

$$MTE = \pm 0.04\% \text{ span}$$

Section 2.3

$$MSLBE = \pm 0.00\% \text{ span}$$

[Reference 3.8](#)

Therefore, the module errors are

$$\begin{aligned} e_{5R} &= \pm[0.15^2 + 0.75^2 + 0.04^2]^{1/2} \\ &= \pm 0.77\% \text{ span} \end{aligned}$$

$$e_{5P} = +0.0\% \text{ span}$$

$$e_{5N} = -0.0\% \text{ span}$$

7.7 RTD to temperature transmitter cable - Module 6

$$PM = \text{N/A}$$

$$RA = \text{N/A}$$

$$DR = \text{N/A}$$

$$TE = \text{N/A}$$

$$MTE = \text{N/A}$$

$$MSLBE = +0.08\% \text{ span}$$

[Reference 3.9](#)

CALCULATION**COMMENTS**

Therefore, the module errors are

$$e6_R = \pm 0.0\% \text{ span}$$

$$e6_P = +0.08\% \text{ span}$$

$$e6_N = -0.0\% \text{ span}$$

7.8 Pressurizer temperature transmitter - Module 7

$$PM = N/A$$

$$RA = \pm 0.20\% \text{ span}$$

[Reference 3.6](#)

$$DR = \pm 0.35\% \text{ span}$$

[Reference 3.6](#)

$$TE = \pm 0.03\% \text{ span}$$

[Reference 3.6](#)

$$MTE = \pm 0.05\% \text{ span}$$

Section 2.3

$$MSLBE = N/A$$

Therefore, the module errors are

$$e7_R = \pm [0.20^2 + 0.35^2 + 0.03^2 + 0.05^2]^{1/2}$$

$$= \pm 0.41\% \text{ span}$$

$$e7_P = +0.0\% \text{ span}$$

$$e7_N = -0.0\% \text{ span}$$

7.9 Function generator - Module 8

$$PM = N/A$$

$$RA = \pm 0.53\% \text{ span}$$

[Reference 3.6](#)

$$DR = \pm 0.05\% \text{ span}$$

[Reference 3.6](#)

$$TE = \pm 0.10\% \text{ span}$$

[Reference 3.6](#)

$$MTE = \pm 0.13\% \text{ span}$$

Section 2.3

$$MSLBE = N/A$$

Therefore, the module errors are

$$e8_R = \pm [0.53^2 + 0.05^2 + 0.10^2 + 0.13^2]^{1/2}$$

$$= \pm 0.56\% \text{ span}$$

$$e8_P = +0.0\% \text{ span}$$

$$e8_N = -0.0\% \text{ span}$$

8.0 Calculate channel uncertainty

See [RP 6.3](#).

8.1 Random channel uncertainty

From 6.7 (Eq. 9), the random channel uncertainty is

$$\begin{aligned} CU_R^2 = & + [LEVEL * slope * (e5_R + e6_R + e7_R)]^2 \\ & + (LEVEL * e8_R)^2 \\ & + [CF * (e1_R + e2_R)]^2 \\ & + e3_R^2 \\ & + e4_R^2 \end{aligned}$$

(Eq. 9)

CALCULATION**COMMENTS**

Substituting in the values obtained in Section 7.0,

$$\begin{aligned} \text{CU}_R^2 = & + [\text{LEVEL} * \text{slope} * (0.77 + 0.0 + 0.41)]^2 \\ & + (\text{LEVEL} * 0.56)^2 \\ & + [\text{CF} * (1.17 + 0.00)]^2 \\ & + 0.32^2 \\ & + 0.28^2 \end{aligned}$$

$$\text{CU}_R = \pm [(1.18 * \text{LEVEL} * \text{slope})^2 + (0.56 * \text{LEVEL})^2 + (1.17 * \text{CF})^2 + 0.18]^{1/2}$$

The MSLB is an overcooling transient, causing a contraction of the RCS. This contraction causes Pressurizer level to decrease below its normal range, which then initiates a reactor trip. The channel error increases with increasing LEVEL. A LEVEL of 50% (150 inches) will be used to conservatively estimate the channel error, in that any required reactor trip will occur below 50% span.

The Correction Factor is 1.0 at normal conditions and decreases as Pressurizer temperature decreases. Channel error increases with CF, so use of a large CF is conservative. The MSLB is an overcooling transient, so CF will decrease during the transient. A CF of 1.0 will be used to conservatively estimate the channel error.

The channel error increases with increasing slope. Slope increases with increasing CF. The slope at CF = 1 will be used to conservatively estimate channel error. This slope is 0.324 per 100°F or 0.00324 per °F.

Note that the first term, 1.18 * LEVEL * slope, needs careful attention to units. The percent temperature span is ±1.18; the percent level span is 0.5; and slope is (°F)⁻¹. The simplest way to resolve this is to convert ±1.18% temperature span into (0.0118 * 450) = ±5.31°F and then carry out the multiplication.

$$\begin{aligned} \text{CU}_R &= \pm [(5.31 * 0.5 * 0.00324)^2 + (0.56 * 0.5)^2 \\ &\quad + (1.17 * 1.0)^2 + 0.18]^{1/2} \\ &= \pm [0.0086^2 + 0.28^2 + 1.17^2 + 0.18]^{1/2} \\ &= \pm 1.28\% \text{ span} \end{aligned}$$

8.2 Positive bias channel uncertainty

The positive bias channel uncertainty equation (Eq. 10) is

$$\begin{aligned} \text{CU}_P = & + \text{LEVEL} * \text{slope} * (\text{e5}_P + \text{e6}_P + \text{e7}_P) \\ & + \text{LEVEL} * \text{e8}_P \\ & + \text{CF} * (\text{e1}_P + \text{e2}_P) + \text{e3}_P + \text{e4}_P \end{aligned} \quad (\text{Eq. 10})$$

CALCULATION**COMMENTS**

Inserting the values from [Section 7.0](#) and using the same development as in [8.1](#), the positive bias channel uncertainty becomes

$$\begin{aligned}CU_P &= + 0.5 * 0.00324 * [0 + .08 * (450/100) + 0] \\&\quad + 0.5 * 0 \\&\quad + 1.0 * (10.73 + 0.98) + 0 + 0 \\CU_P &= + 0.00058 + 11.71 = + 11.71\% \text{ span}\end{aligned}$$

8.3 Negative bias channel uncertainty

The negative bias channel uncertainty equation (Eq. 11) is

$$\begin{aligned}CU_N &= - \text{LEVEL} * \text{slope} * (e5_N + e6_N + e7_N) \\&\quad - \text{LEVEL} * e8_N \\&\quad - CF * (e1_N + e2_N) - e3_N - e4_N\end{aligned}\tag{Eq. 11}$$

Inserting the values from [Section 7.0](#) and using the same development as in [8.1](#), the positive bias channel uncertainty becomes

$$\begin{aligned}CU_N &= - 0.5 * 0.00324 * (0 + 0 + 0) \\&\quad - 0.5 * 0 \\&\quad - 1.0 * (0.15 + 0) - 0 - 0 \\CU_N &= - 0.15\% \text{ span}\end{aligned}$$

8.4 Total channel uncertainty

Therefore, the total channel uncertainty under 15 minutes of MSLB conditions is

$$CU = +12.99\% \text{ span}, -1.43\% \text{ span}$$

9.0 Obtain the analytical limit

From Reference 3.1, the MSLB accident analysis requires that a reactor trip be initiated before Pressurizer level drops below 75 inches.

10.0 Determine the setpoint

The trip setpoint (TS) will be the analytical limit + the channel error + the margin.

The analytical limit is 75 inches.

The channel error applicable to low trip is +12.99% span, or 39 inches.

See [RP Section 7.0](#)

See [RP Section 7.0](#)

CALCULATION**COMMENTS**

The normal operating band of Pressurizer level varies with power level, being 120 inches at zero power and 180 inches at full power. The minimum trip setpoint is $(75 + 39) = 114$ inches. Although this provides adequate operating margin versus the nominal Pressurizer level at full power, no additional margin will be added due to the small operating margin at zero power.

$$\begin{aligned}\text{TS} &= \text{Analytical Limit} + \text{CU} + \text{margin} && (\text{Eq. 16}) \\ &= 75 + 39 + 0 \text{ inches} \\ &= 114 \text{ inches}\end{aligned}$$

11.0 Allowable Value

To compute the allowable value for the Pressurizer level trip setpoint, the channel error as a result of conditions present during the surveillance test must be determined.

11.1 Channel Allowable Value Equations

The channel error equations for determination of the allowable value (Eqs. 9, 10, and 11) are the same as those given for the determination of channel uncertainty. However, all bias terms in this calculation arose from MSLB conditions, so only the random channel uncertainty equation is needed to determine channel allowable value uncertainty.

$$\begin{aligned}\text{CAVU}_R^2 &= + [\text{LEVEL} * \text{slope} * e_{5R} + e_{6R} + e_{7R}]^2 \\ &+ (\text{LEVEL} * e_{8R})^2 \\ &+ [\text{CF} * (e_{1R} + e_{2R})]^2 \\ &+ e_{3R}^2 \\ &+ e_{4R}^2 && (\text{Eq. 17})\end{aligned}$$

11.2 Module Allowable Value Equations

The module error equations for determination of the allowable value are similar to those given for the determination of channel uncertainty (Eqs. 9, 10, and 11) but reflect those error components that would be present in non-MSLB conditions. Again, the only bias errors in this calculation arose from MSLB conditions, so only the random module error equation is needed to determine the module allowable value error. Using "av" to indicate a module allowable value error, the module error equation becomes

$$\text{av}_R^2 = + \text{RA}_R^2 + \text{DR}_R^2 + \text{TE}_R^2 + \text{MTE}_R^2 \quad (\text{Eq. 18})$$

See [RP 7.0 and Appendix I](#).

CALCULATION**COMMENTS****11.3 Channel Allowable Value Uncertainty**

Using Eq. 18, the module allowable value errors are

$$av1 = e1_R = \pm 1.17\% \text{ span}$$

$$av2 = 0$$

$$av3 = e3_R = \pm 0.32\% \text{ span}$$

$$av4 = e4_R = \pm 0.28\% \text{ span}$$

$$av5 = e5_R = \pm 0.77\% \text{ span}$$

$$av6 = 0$$

$$av7 = e7_R = \pm 0.41\% \text{ span}$$

$$av8 = e8_R = \pm 0.56\% \text{ span}$$

Substituting these values into Equation 13 gives

$$\begin{aligned} \text{CAVU}_R^2 = & + [\text{LEVEL} * \text{slope} * (0.77 + 0.0 + 0.41)]^2 \\ & + (\text{LEVEL} * 0.56)^2 \\ & + [\text{CF} * (1.17 + 0.0)]^2 \\ & + 0.32^2 \\ & + 0.28^2 \end{aligned}$$

$$\begin{aligned} \text{CAVU}_R = & \pm [(\text{LEVEL} * \text{slope})^2 + (0.56 * \text{LEVEL})^2 \\ & + (1.17 * \text{CF})^2 + 0.18]^{1/2} \end{aligned}$$

Calibration is performed once a refueling at zero power. Therefore, LEVEL is 120 inches; CF is 0.64; and slope is .03/100°F, or .0003/°F. Substituting

$$\begin{aligned} \text{CAVU}_R = & \pm [(5.31 * .4 * 0.0003)^2 + (0.56 * .4)^2 \\ & + (1.17 * 0.64)^2 + 0.18]^{1/2} \end{aligned}$$

$$\text{CAVU}_R = \pm 0.89\% \text{ span}$$

11.4 Channel Allowable Value

Per Section 10.0, the nominal trip setpoint is 114 inches. The channel allowable value error is $\pm 0.89\%$ span, or ± 2.7 inches. Therefore, the channel allowable value is

$$\begin{aligned} \text{AV} &= \text{TS} - \text{CAVU} & (\text{Eq. 19}) \\ &= 114 - 2.7 \text{ inches} \\ &= 111.3 \text{ inches} \end{aligned}$$

Consistent with [RP 7.3](#), Method 3.

CALCULATION**COMMENTS****12.0 Summary**

The Pressurizer level reactor trip is required for 15 minutes into a MSLB. Under these conditions, the worst-case channel error is +39 inches, -4.3 inches.

To assure a reactor trip before actual level reaches 80 inches, the trip setpoint should be set at 114 inches.

When performing surveillance testing at zero power, the channel error is expected to be ± 2.7 inches. The channel is operable if it trips at no less than 111.3 inches.

EXAMPLE CALCULATION - RADIATION TRIP

CALCULATION

COMMENTS

1.0 Purpose

The purpose of this calculation is to establish instrument setpoints for the Reactor Building Exhaust Plenum Monitors (RIS-410 A,B). The HIGH trip setpoint is established by the ODCM ([Reference 3.5](#)) and maintained by plant Technical Specifications ([Reference 3.4](#)).

This calculation determines instrument bistable settings for both LOW (INOPERATIVE) and HIGH (ISOLATION) trip setpoints based upon instrument errors, process measurement uncertainties, and analytic limits taken from [Reference 3.5](#).

2.0 Assumptions

2.1 M&TE uncertainty is significantly less than the reference accuracies of the installed equipment. The accuracy of a 4½-digit digital voltmeter (typically ±0.03%) is much less than 0.1 times the reference accuracy of the ratemeter (±3.0%). Similarly, the accuracy of the frequency counter used to calibrate the ratemeter (±10 ppm time base accuracy) greatly exceeds the ratemeter accuracy. Thus, these terms make no significant contributions to total channel uncertainty and are not present in the uncertainty formulas. Also, since digital sources and meter are used exclusively, any calibration technique errors due to misreading of the instruments would have an imperceivable impact on this calculation.

2.2 The setting adjustment potentiometers are precision, multiple turn devices with a rated resolution of ±0.1 % SPAN. For the reasons in 2.1 above, the adjustment device does not contribute significantly to the final setting.

2.3 Since equipment specifications are given in percent equivalent linear full scale (% ELFS), this will be used as the common unit. To convert between process units (cpm, logarithmic) and % ELFS, the following conversion is used:

FACTOR = $10^{[(\% \text{ ELFS})(6)]}$ where 6 is the number of decades for this application, % ELFS is the reference accuracy of the linear scale.

NOTE: The following format is for illustrative purposes only. See RP Preface, Section 10, and [Page 105](#).

RP 5.2 and 5.3 were reviewed to identify potentially applicable factors.

[See RP 6.2.6.](#)

[See last paragraph of RP 6.3.3.](#)

CALCULATION

COMMENTS

This transformation does not allow exact mapping of symmetric intervals. For example, a symmetric $\pm 1\%$ ELFS interval transforms to a factor of 1.15 (or $1 \div 1.15 = 0.87$). For this application using relatively small values, the positive interval (+ 15%) is approximately equal to the negative interval (-13%). For conservatism, all non-symmetric intervals are expanded to include symmetric limits (i.e., +15% and -13% are expanded to $\pm 15\%$.)

2.4 The radioactive half-life of the installed check source is long compared to the surveillance interval (1.5 years).

If the check source half-life were not long compared to the surveillance interval, the low (inoperative) trip setpoint may require adjustment (lowering) to maintain the separation between the alarm point and the average value of the check source. Alternatively, the check source can be replaced.

3.0 References

3.1 Piping & Instrument Drawing M240

3.2 Analog Loop Diagram E62.4

3.3 Technical Manual NQ406-3, Radiation Monitoring System

3.4 Nuclear Unit One (NUO) Technical Specification

3.5 NUO Off-Site Dose Calculation Manual (ODCM)

3.6 Nuclear Radiation Detection, W. J. Price, McGraw-Hill

3.7 ANSI N13.10-1974, Continuous Monitored Effluent Radioactivity Instrumentation

3.8 Reg. Guide 1.105, Instrument Setpoints for Safety-Related Systems

3.9 ISA-S67.04, Setpoints for Nuclear Safety-Related Instrumentation

3.10 Telephone Conversation 89-1-17, from A. C. Smith to J. Parry (Radiation Monitoring, Inc., dated March 3, 1989)

CALCULATION

COMMENTS

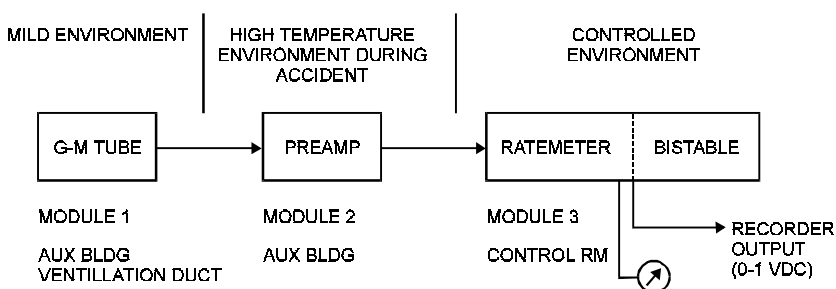
4.0 Functional description

The Reactor Building Exhaust Plenum Radiation Monitors (RIS-410 A,B) sense radioactivity in the reactor building ventilation exhaust. In the event of a spent fuel handling accident, fission product gases will migrate to the exhaust plenum detectors (RE-410, A,B). When the immersion dose rate equivalent exceeds 50,000 cpm (from Reference 3.5), the HIGH level trip actuates the automatic isolation of the reactor building ventilation system, thus securing the effluent discharge.

A LOW level trip monitors the dose rate provided by an installed check source. An INOPERATIVE alarm is tripped when the count rate falls below a preset level.

The pre-amplifier circuit contains an "anti-jam" feature that maintains a 10^7 cpm count rate to prevent loss of signal during detector saturation conditions.

5.0 Block diagram



6.0 Determining uncertainty equations

The general equation for channel uncertainty (CU) is

$$CU^+ = [PM^2 + PE^2 + e_1^2 + e_2^2 + e_3^2]^{1/2} + B_T^+ + |\pm RB_T|$$

$$CU^- = [PM^2 + PE^2 + e_1^2 + e_2^2 + e_3^2]^{1/2} - B_T^- - |\pm RB_T|$$

where

PM = random component of the process measurement uncertainty;

PE = random component of the primary element uncertainty;

e_n = RSS of all random components of uncertainty associated with a module n;

Note that in this application, the check source performs a "keep-alive" function and is not used for instrument calibration.

See RP 5.2 and Figure 1.

See RP 6.3.

Modified version of RP Eq. 6.10a.

Modified version of RP Eq. 6.10b.

CALCULATION**COMMENTS**

B_T^+ = Algebraic sum of all bias estimates for all positive biases in a channel;

B_T^- = Algebraic sum of all bias estimates for all negative biases in a channel;

RB_T = sum of the absolute value of all random bias (and arbitrary distribution) estimates in a channel.

The general equation for a module uncertainty is

$$e^+ = + [RA^2 + DR^2 + TE^2 + RE^2 + SE^2 + HE^2 + SP^2 + MTE^2]^{1/2} + B^+ + |\pm RB|$$

Modified version of RP Eq. 6.11a.

$$e^- = - [RA^2 + DR^2 + TE^2 + RE^2 + SE^2 + HE^2 + SP^2 + MTE^2]^{1/2} - B^- - |\pm RB|$$

Modified version of RP Eq. 6.11b.

where

e = module total uncertainty;

RA = module reference accuracy;

DR = module drift over a specified period;

TE = module temperature effect;

RE = module radiation effect;

SE = module seismic (vibration) effect;

HE = module humidity effect;

SP = module static pressure effect;

MTE = maintenance and test equipment used during module calibration;

B = bias uncertainty estimates associated with module;

RB = sum of absolute values of all random biases or abnormally distributed uncertainties for the module.

Note that this general form assumes that all uncertainties within the radical are random and approximately normally distributed.

7.0 Determine uncertainty data

See RP 6.2.

The following discussion develops the uncertainty terms for each of the modules in the instrument channel. Any general equation terms that are not discussed are not relevant to this instrument channel.

According to the manufacturer, ([Reference 3.10](#)), the specified accuracies of the ratemeter and preamp modules include normal power supply variations, as well as normal environmental, temperature, and humidity effects.

CALCULATION**COMMENTS**

Static pressure effects do not apply to any modules in this calculation. Also, these instruments are not required to perform during or after a design-basis earthquake (DBE) or any other design-basis accident (DBA) that creates a hostile environment other than the accident described in [Section 4.0](#).

7.1 Process measurement (PM)

For the LOW alarm setpoint (lowest decade), the integrating circuit time constant is two seconds ([Reference 3.3](#)). For the HIGH alarm (trip) setpoint, a value of 0.02 seconds is given ([Reference 3.3](#)).

For the 60 cpm check source ($r_{\text{true}} = 1 \text{ cps}$), the uncertainty is random and approximately normally distributed. The 95% probability limit is

$$2\sigma = \pm (2r \div RC)^{1/2} \quad \text{Reference 3.6}$$

where

r = signal count rate (cps);

RC = circuit time constant (sec).

For the LOW setpoint (1cps),

$$PM_{\text{LOW}} = \pm [2 (1) \div 2]^{1/2} = \pm 1 \text{ cps}$$

$$\begin{aligned} \text{(Error) Factor} &= (r_{\text{true}} + r_{\text{error}}) \div r_{\text{true}} = (1 + 1) \div 1 = 2.0 \\ &\text{(100\% relative error)} \end{aligned}$$

Converting to linear uncertainty units (see assumption 2.3),

$$2.0 = 10^{6X}; X = 5.0\% \text{ ELFS}$$

For the HIGH setpoint (50,000 cpm = 833 cps) from [Reference 3.5](#),

$$PM_{\text{HIGH}} = \pm [2(833) \div 0.02]^{1/2} = \pm 289 \text{ cps}$$

$$\text{Factor} = (839 + 289) \div 839 = 1.35$$

$$1.35 = 10^{6X}; X = 2.2\% \text{ ELFS}$$

$$PM_{\text{HIGH}} = \pm 2.2\% \text{ ELFS}$$

See [RP 6.2.5](#).

The random nature of the radioactive decay process causes a statistical uncertainty that depends upon the rate (cps) and the instrument time constant (RC). Analog rate-meters are typically designed for minimizing this uncertainty, yet must provide adequate response time.

CALCULATION

COMMENTS

7.2 Primary element (PE)

There is no primary element. The Geiger-Muller (G-M) tube is treated as a sensor and designated as Module 1. The 2π geometry immersion dose to the sensors in the ventilation duct and the detector energy response are accounted for by the ODCM ([Reference 3.5](#)).

Note that this instrument setpoint calculation does not address the isotopic calibration of the sensors (G-M tubes). These effects are included in [Reference 3.5](#).

7.3 G-M tube (Module 1)

For this application, the background noise is < 0.1 cps and has a negligible effect on the setpoint determination.

Noise can be generated by operating the G-M tube at an elevated temperature. For this application, the operating temperature range in the ventilation duct is too low to cause any temperature effect (TE) bias.

The G-M tube is basically an event counting device with an efficiency that is energy dependent and accounted for in the isotopic calibration process (detector efficiency calculation). Thus, there is no reference accuracy associated with the tube. However, there are unique effects to be considered. For low count rates, noise as well as background radiation may contribute significant bias errors.

The fill gas in the G-M tube is subject to long-term leakage, resulting in a gradual reduction in sensitivity (efficiency). This drift is very small and considered negligible over the 18-month-calibration interval ([Reference 3.3](#)).

For cases where background represents a significant fraction of the indicated count rate, average background values should be subtracted (as a constant correction) from the indicated count rate to obtain the process variable (true) count rate.

For the setpoint of 50,000 cpm (833 cps), the pulse, resolution effect is negligible. The formula for dead time correction is given in [Reference 3.6, page 127](#) as

For very high count rates, there is a pulse resolution time associated with the G-M counter (and system). Typically, this effect becomes visible at $> 10^5$ cps and is caused by overlapping or near coincident pulses. It is a bias error, since indicated counts will always underestimate the true count rate.

CALCULATION**COMMENTS**

$$n = m \div (1 - m\tau)$$

where n = true count rate (cps)

m = indicated count rate (cps)

τ = dead time (sec)

7.4 Pre-Amplifier (Module 2)

From the specification sheet in [Reference 3.3](#), a temperature-noise effect of 100 cps for temperatures up to 150°F ambient to the pre-amp is used. As discussed earlier, noise addition is a positive bias (indicated value exceeds actual value).

$$TE = +100 \text{ cps (estimate limit of error)}$$

This temperature effect is present only during accident (high temperature) conditions.

Converting to linear units,

$$\text{FACTOR} = (833 + 100) \div 833 = 1.12$$

$$1.12 = 10^{6X}; X = +0.8\% \text{ ELFS}$$

NOTE: This positive bias is an uncertainty estimate that may or may not be present. Although it is conservative for an increasing parameter (actual value < indicated value), accounting for the effect in this calculation assumes that the effect would always be present. If the effect was absent, its absence would result in a non-conservative condition (i.e., actual value > indicated value). Therefore, taking credit for this conservatism in this application is deemed imprudent. This term will not be included in the subsequent channel uncertainty equations.

7.5 Analog ratemeter (Module 3)

The analog ratemeter converts the 6 decades of input count rate into a linear output. It also includes electronic bistables that are set to trip at the desired values. [Reference 3.3](#) gives the reference accuracy as $\pm 3\%$ ELFS (OUTPUT). Since the analog panel meter is small (3½ inches), the recorder output voltage is the output to which the $\pm 3\%$ ELFS applies. Significant additional uncertainties must be accounted for if analog panel meters are used ([Reference 3.7](#)).

See [RP 6.2.2](#).

The electronic pre-amplifier performs the necessary signal conditioning to drive the cable feed to the ratemeter. Although the output pulse height from the G-M tube is relatively large, the source impedance needs to be matched for the relatively long signal path to the ratemeter. The pre-amp is also a digital device that is capable of introducing electronic noise and contributing to pulse resolution time.

See [RP 6.2.6.4](#).

CALCULATION**COMMENTS**

The ratemeter converter stability (drift) is given in [Reference 3.3](#) as $\pm 0.5\%$ ELFS for a 12-month period. Using the drift extension technique of linear extrapolation, one obtains

$$DR = \pm 0.75\% \text{ ELFS for an 18-month interval.}$$

This value will be treated as a random bias, since

- 1) The manufacturer does not have data to characterize a specific individual instrument ([Reference 3.10](#)); and
- 2) For simplicity, this single calculation applies to both instrumentation channels.

8.0 Calculate instrument channel uncertainty and trip setpoints

Since this is a calculation for a non-LSSS variable, RP Section 7.04 does not specifically apply.

Given the sources of module and process uncertainty developed in [Section 7.0](#), the general equation of [Section 6.0](#) is reduced to

HIGH SETPOINT:

$$\begin{aligned} CU &= \pm [PM^2 + RA_3^2]^{1/2} \pm |\pm RB_3| \\ &= \pm [(2.2)^2 + (3.0)^2]^{1/2} \pm |\pm 0.75| \\ &= \pm 4.47\% \text{ ELFS} \end{aligned}$$

$$\text{From 2.3, FACTOR} = 10^{6(\pm 0.0447)} = (1.85)^{\pm 1}$$

$$\begin{aligned} SP_{HI} &= (AL) (\text{FACTOR}) \\ &= (50,000 \text{ cpm}) (1.85)^{-1} = 27,027 \text{ cpm} \\ &\quad (\text{SET FOR TRIP ABOVE THIS VALUE}) \end{aligned}$$

LOW SETPOINT:

$$\begin{aligned} CU &= \pm [PM^2 + RA_3^2]^{1/2} \pm |\pm RB_3| \\ &= \pm [(5.0)^2 + (3.0)^2]^{1/2} \pm |\pm 0.75| = \pm 6.58\% \text{ ELFS} \end{aligned}$$

Converting back to a Factor,

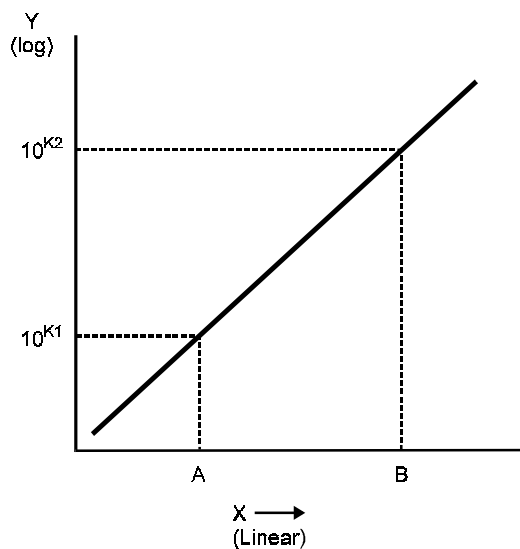
$$\text{FACTOR} = 10^{6(\pm 0.0658)} = (2.48)^{\pm 1}$$

$$\begin{aligned} SP_{LO} &= (AL)(\text{FACTOR}) \\ &= (60 \text{ cpm})(2.48)^{-1} = 24.2 \text{ cpm} \\ &\quad (\text{SET FOR TRIP BELOW THIS VALUE}) \end{aligned}$$

In order to obtain accurate values the instrument bistable settings, the ratemeter setpoints will be set using the linear output (recorder) voltage. The transformation used is derived below.

CALCULATION

COMMENTS



$$Y = 10^{\left[\frac{X(K_2 - K_1) - AK_2 + BK_1}{B - A} \right]} = 10^{\left[\frac{6X - 0 + 1}{1} \right]} = 10^{(6X + 1)}$$

$$X = \frac{(B - A) \text{ LOG } Y + AK_2 - BK_1}{K_2 - K_1} = \frac{\text{LOG } Y + 0 - 1}{6}$$

$$= \frac{\text{LOG } Y - 1}{6}$$

For the 6 decade analog ratemeter ($K_2 = 7$, $K_1 = 1$) with a 0 - 1 (A = 0, B = 1) VDC linear output, the values are summarized below.

POINT	LOG VALUE (CPM)	LINEAR VALUE (VOLTS)
LOWEST SCALE MARK	10	0.000
LOW TRIP	24.2	0.064
CHECK SOURCE	60	0.130
HIGH TRIP	27,027	0.572
HIGHEST SCALE MARK	10^7	1.000

CALCULATION**COMMENTS****9.0 Determining the allowable value**

Since the instruments are not contained in the LSSS Table in [Reference 3.4](#), there are no Allowable Values.

10.0 Summary

The low bistable shall be set at 0.064 VDC using a digital voltmeter (DVM) connected to the recorder output. This value is significantly less than the 0.130 VDC check source average value and significantly greater than the 0.000 volt level at low scale. Similarly, the 0.572 VDC is significantly separated from the check source level and the high scale mark. Thus, the setpoint placements have a high probability of (1) tripping before reaching upper scale limits, and (2) avoiding false trips.

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